Magnetosphere Modeling

Heliophysics Summer School

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Overview

- Part 1
 - Why MHD?
 - How to build a global magnetosphere (MHD) model
 - Beyond MHD
- Part 2

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- Dungey cycle, convection, particle acceleration
- Convection and bubbles
- Magnetosphere-ionosphere coupling
- Cool recent projects



Part 1

- Why MHD?
- How to build a global MHD model?
 - Flux Corrected Transport (FCT)
 - Constrained transport
 - Grids
 - External boundary condition
 - Inner boundary condition
 - Conductance modeling
- Beyond MHD



Before global MHD

"... despite its weakness, the interplanetary magnetic field has the important effect of causing the solar wind to behave as a continuous fluid... Thus it seems that we should treat the interaction between the solar wind and the magnetosphere in terms of continuum flow rather than free molecular flow..."

Axford, JGR, (1962)



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Meridional cut

"... even for weak magnetic fields, the cyclotron period is still shorter than any macroscopic period, and the plasma does have a two-dimensional consistency perpendicular to the magnetic field. This restores the possibility of a fluid theory to a limited extent and is the basis for the guiding center description of a plasma..."

Kulsrud, Handbook of plasma physics (1983)

Global MHD

Underlying equations assuming isotropy

For single fluid, the ideal MHD equations are solved:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0$$
$$\frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot \left(\rho \mathbf{u} \mathbf{u} + P\mathbf{I} + \frac{B^2}{8\pi}\mathbf{I} - \frac{\mathbf{B}\mathbf{B}}{4\pi}\right) = 0$$
$$\frac{\partial E}{\partial t} + \nabla \cdot \left(\mathbf{u}(\mathbf{E} + \mathbf{P})\right) + \mathbf{u} \cdot \mathbf{j} \times \mathbf{B} = 0$$
$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \times \mathbf{u} \times \mathbf{B} = 0$$

where

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$$E = \frac{1}{2}\rho u^2 + \frac{P}{\gamma - 1}$$

Birn & Hesse, Ann. Geophys., (2005) doi: 10.5194/angeo-23-3365-2005.

For multiple fluids (equations still ideal): $\frac{\partial \rho_{\alpha}}{\partial t} + \nabla \cdot (\rho_{\alpha} \mathbf{u}_{\alpha}) = 0$ $\frac{\partial \rho_{\alpha} \mathbf{u}_{\alpha}}{\partial t} + \nabla \cdot (\rho_{\alpha} \mathbf{u}_{\alpha} \mathbf{u}_{\alpha} + P_{\alpha} \mathbf{I}) + F_{\alpha}^{d} + n_{\alpha} q_{\alpha} E_{||} = 0$ $\frac{\partial E_{\alpha}}{\partial t} + \nabla \cdot \left(\mathbf{u}_{\alpha} (\mathbf{E}_{\alpha} + \mathbf{P}_{\alpha}) \right) + \mathbf{u}_{\alpha} \cdot \left(F_{\alpha}^{d} + n_{\alpha} q_{\alpha} E_{||} \right) = 0$ $\frac{\partial \mathbf{B}}{\partial t} + \nabla \times \mathbf{u} \times \mathbf{B} = 0$ where

$$E_{\alpha} = \frac{1}{2}\rho_{\alpha}u_{\alpha}^{2} + \frac{P_{\alpha}}{\gamma - 1}, E_{||} = -\mathbf{b}\mathbf{b} \cdot \frac{\nabla P_{e}}{ne}$$

$$F_{\alpha}^{d} = \mathbf{b} \times \begin{bmatrix} \rho_{\alpha} \mathbf{u}_{\alpha} \cdot \nabla \mathbf{u}_{\alpha} + \nabla P_{\alpha} + \frac{\rho_{\alpha} (\mathbf{u} - \mathbf{u}_{\alpha}) \cdot \mathbf{b}}{B} \frac{\partial \mathbf{B}}{\partial t} \\ -\frac{\rho_{\alpha}}{\rho} \left(\sum_{\beta} (\rho_{\beta} \mathbf{u}_{\beta} \cdot \nabla \mathbf{u}_{\beta} + \nabla P_{\beta}) + \nabla P_{e} - \mathbf{j} \times \mathbf{B} \right) \end{bmatrix} \times \mathbf{b}$$

and total momentum equation solved for bulk fluid:

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$$\frac{\partial \rho_{\alpha} \boldsymbol{u}}{\partial t} + \nabla \cdot (\rho_{\alpha} \boldsymbol{u}_{\alpha} \boldsymbol{u}_{\alpha} + P_{\alpha} \mathbf{I}) - \nabla P_{e} + \mathbf{j} \times \mathbf{B} = 0$$

Beginnings of global MHD codes

2D and 2.5D simulations



Leboeuf et al., GRL, 5(7), 1978

"The magnetosphere contains a number of discontinuities [both shocks and contact discontinuities] - which must be modelled as accurately as possible to retain the real physics of the situation. Such discontinuities lead to a numerical dillema. If a high accuracy dissipationless algorithm is used, numerical dispersion leads to nonphysical waves being propagated away from the discontinuity... If enough dissipation is added to remove the waves or "ripples" in the solution, the accuracy of the result suffers by the action of what amounts to a numerical diffusion or resistivity."

Lyon et al., GRL, 1980

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Lyon et al., PRL, 1981

One of the first applications of the Flux Corrected Transport (FCT) methods in multiple dimensions.

Flux corrected transport

Linear advection is a tough problem



- FCT algorithms apply >1 order, lower-diffusion scheme outside of sharp boundaries, and introduce minimal diffusion (via flux limiting) at sharp boundaries to suppress spurious extrema
- Many different algorithms exist with flux or *slope* limiting (FCT, TVD, WENO) but the idea is roughly the same
- The quality of the result depends strongly on the choice of limiter and other details (e.g., order of reconstruction)

Flux corrected transport

• Key methods developed by Boris, Book and Hain at NRL (Boris & Book, 1973; Book, Boris & Hain, 1975; Boris & Book, 1976)



Movie by Bin Zhang

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1-D advection

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Comparison of different schemes



2-D advection

Slotted cylinder test



- In 3-D, 2nd order calculation is ~8⁴ x more expensive than 7th order
- If time of execution is of essence and computer resources are not infinite, highorder calculation is highly desirable
- Above some limit, lower-order calculations become prohibitive

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The need for highorder reconstruction

Formal convergence isn't everything

- Significant reduction in overall error when going to high-order
- Reconstruct both physical variables and geometry

High-order reconstruction





Finite volume discretization

Keeping the **B** field solenoidal



The general update scheme is

$$\mathbf{U}^{t+\Delta t} = \mathbf{U}^{t} - \Delta t \cdot \oint \mathbf{F} \left(\mathbf{U}^{t+\Delta t/2} \right) \cdot d\vec{\mathbf{S}}$$

Where F is the mass, momentum and energy flux at cell faces

The Bi, Bj, Bk are magnetic fluxes through the i,j,k faces, respectively:

$$\frac{\partial}{\partial t} \int \mathbf{B} \cdot d\mathbf{S} = \frac{\partial}{\partial t} \Phi_{i,j,k} = -\oint \mathbf{E} \cdot d\mathbf{I}$$
$$\Phi^{t+\Delta t} = \Phi^{t} - \Delta t \cdot \oint \mathbf{E}^{t+\Delta t/2} \cdot d\mathbf{I}$$

Constrained transport (Yee-mesh) ensures $\nabla \cdot \mathbf{B} = 0$

(Evans & Hawley, ApJ, 1988)

Choice of a grid Grid used in the (c) (a) (b) **GAMERA** code 50 -100(e) [50 SM-X [Re] (d) Fig. 1. Several common choices for numerical grids: (a) a uniform Cartesian grid, (b) a stretched Cartesian grid, (c) a non-Cartesian grid with Cartesian topology, (d) a structured adaptive grid, (e) a unstructured grid

(Raeder, Global Magnetohydrodynamics – A Tutorial, 2003)

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Typical model input

From basic MHD to global magnetosphere

External boundary conditions



Use L1 measurements (1 point time series) as input in a global 3D model





External boundary conditions: Caveats



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al frame.

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Inner boundary condition: lonosphere



Inner boundary condition: lonosphere



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Additional reading:

Inner boundary condition: Ionosphere



We've built it, now what?

How far have we gone over ~40 years



Lyon et al. PRL (1981), 50x40



Wiltberger, Merkin & Lyon (2016), 212x196x256

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GAMERA: A reinvention of LFM

Good numerics lead to good physics

- Solves MHD equations on arbitrary hexahedral grids (non-orthogonal/singular coordinates)
- Modern Fortran, multiple layers of heterogeneous parallelism
- Standard (Athena) MHD tests published (Zhang et al., ApJS 2019)
- Multiple space plasma applications (Earth, Venus, Jupiter, Mercury, heliosphere)
- Enables simulations that would be prohibitive unless high-order numerics and an adapted grid were used

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140°W

Geographic latitude

71°N

70°N

69°N

68°N

136°W

Forbes





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NASA press release, May 2021 "Mystery of auroral beads resolved"

Going beyond MHD

Modern geospace models are frameworks coupling different physics-based models





The MAGE Vision

Multiscale Atmosphere-Geospace Environment





GAMERA+RCM+TIEGCM = MAGE 1.0

- Target high resolution:
 - 600 km in central plasma sheet
 - 0.625°×0.625° in ionosphere/thermosphere





Conductance: Auroral precipitation in MAGE

Glean as much information as we can from both first-principles and data (Dong Lin @ NCAR/HAO & Shanshan Bao @ Rice)

- RCM coupling was completely rewritten: uses hybrid parallelism, very efficient FL tracer on the native curvilinear grid
- The auroral model combines MHD-based mono-energetic electron precipitation and driftinformed diffuse electron precipitation.
- Precipitation fluxes are informed by MHD field-aligned current and thermal plasma.
- Scattering is informed by data-driven inner magnetosphere wave properties.



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Diffuse electron precipitation modulated by statistical wave models

Glean as much information as we can from both first-principles and data (Shanshan Bao @ Rice U)

JS





- The precipitating electrons are selected by the local waves.
- Low energy electrons (Ek<1keV) barely precipitate.
- High energy electrons (Ek > 100keV) precipitation is suppressed.
- Energy flux distribution shows strong dependence on MLT.
- The precipitation at the plasmaspheric plume is suppressed.



See J. Dorelli GEM 2022 Tutorial

- The magnetospheric modeling community is exploring a number of different approaches for incorporating microscale physics into global models:
 - Hall MHD (XM3) -- Bard and Dorelli, Ann. Geophys., 30, 2021.
 - Multi-fluid/moment (**OpenGGCM/Gkeyll**) Wang et al., J. Geophys. Res., 123, 2018
 - Hybrid (HYPERS) Omelchenko et al., J. Atm. Sol. Terr. Phys., 215, 2021.
 - Hybrid (ANGIE3D) Lin et al., J. Geophys. Res., 119, 2014.
 - Vlasov (Vlasiator) von Alfthan et al., J. Atm. Sol. Terr. Phys., 120, 2014.
 - o Hall MHD/embedded PIC (MHD-EPIC) Tóth et al., J. Geophys. Res., 121, 2016.
 - Hall MHD/embedded Spectral Plasma Solver (SPS) Delzanno *et al.* (under development, LWSSC)
 - Collisionless Hall MHD (MARBLE) Dorelli et al. (under development, LWSSC)
- It is not yet clear which approach will emerge as the new GGCM spine (maybe there will be a diverse ecosystem), but the next decade will be an exciting time to be a magnetospheric model developer:
 - We'll get to explore crazy new approaches (including machine learning) and deploy them on exascale computers
 - We'll learn new things about how collisionless plasmas work in very large systems
 - We'll gain new insights about old problems in magnetospheric physics

https://firebasestorage.googleapis.com/v0/b/vgem2022.appspot.com/o/talks%2Fplenary%2FGSM%20TutorialJohn%20Dorelli?alt=media&token=97760105-0ef9-4f1e-a431-84993b03e984

Part 2

Convection and bubbles

- Importance for ring current build-up and global geospace effects
- Magnetosphere-ionosphere coupling
- Effects in the ionosphere
- Effects on the substorm current wedge

Cool recent projects

- CGS
- EZIE



Transport in the magnetosphere

Classical picture

Dungey cycle (1961)

- Southward IMF/terrestrial field lines merge on dayside
- Open lines swept over poles and reconnect in magnetotail
- Nightside reconnection drives Earthward return flow



Particle transport and acceleration

- Seed particles moved Earthward w/ return flow
- Shorter/stronger fields => Fermi/betatron acceleration
- Increasingly energetic particles are more dominated by curvature/gradient drift



Transport in the magnetosphere

Slow and steady doesn't win the race

Pressure balance inconsistency

• FTE = Flux-tube entropy = PV^{γ}

• $V = \int ds/B$ (Birn+'09, 10.1029/2008JA014015)

- Uniform convection and entropy conservation predict a constant profile of FTE
- Instead find FTE decreases Earthward (Erickson & Wolf '80, Kaufmann+ '04)

Bursty, Bulk Flows (BBFs)

- Earthward convection is observed to be "bursty" (Baumjohann+ 90, Angelopoulos+ 92)
- Average ~ few km/s, mostly comes in bursts of 100's km/s
- Typically dipolarizing: Bz¹ and Bx¹
- Typical sizes, 1-3 RE (Nakamura+ 04, Liu+ 13)

Bubbles!

- Non-ideal process that can locally reduce FTE solves both!
 - Pontius & Wolf '90, Chen & Wolf '93
- Flux-tube volume "surgery" during reconnection can create bubbles
 - Birn+ '09 showed FTE nearly conserved in reconnection



Transport in the magnetosphere

Bubbles, bursts, and buoyancy

Dubyagin+ 11

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Modern picture of transport

- Azimuthally-localized reconnection effects create depleted flux-tubes w/ low FTE (bubbles)
- Bubbles are (non-gravitationally) buoyant, move Earthward to matching background FTE (+/- overshoot & oscillations)
- Modeling: See this in global/regional MHD, hybrid, and PIC
- Data: Spacecraft-inferred FTE best predictor of penetration depth



'ime: 14910.0 [s]

Why Does Convection Matter ... To the full geospace system?

RBSP-A RBSP-B

Because it transports ...



- is the bridge that connects the stretched magnetotail to the nearly-dipolar inner magnetosphere
- <u>Major modeling challenge!</u>

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Transforming the understanding and predictability of space weather

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EMPOWER

DISCOVER

The grand challenge of space weather modeling:

- Treat geospace holistically
- Resolve mesoscale processes
- Couple to the lower atmosphere

* CGS is one of the three NASA DRIVE Centers selected for Phase II



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Multiscale Atmosphere-Geospace Environment

Treating and resolving critical mesoscale processes to discover, understand and quantify emergent cross-scale dynamics

Magnetosphere

-Atmosphere

lonosphere

Solar Wind

Expanded View of lonosphere/Atmosphere



MAGE fulfills three key requirements:

- Describes
 - geospace as a whole
- Resolves critical mesoscale processes in all
 - relevant domains
- Couples
 geospace and
 lower
 atmosphere



<u>cgs.jhuapl.edu/</u> <u>Models</u>

Pressure

Magnetic Field

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Why Does Convection Matter ... To the full geospace system?

RBSP-A RBSP-B

Because it transports



• See talks and discussions at 1st and 2nd CGS Workshops ('20 & '21): cgs.jhuapl.edu/workshop

nearly-dipolar inner magnetosphere

• <u>Major modeling challenge!</u>

3D MHD+TH

Why Does Mesoscale Convection Matter?

Many different kinds of transport can be mesoscale

Convection surge

- Increase in the earthward flow/azimuthal E-field
- Thermal ions ExB drift towards Earth and adiabatically accelerated due to
 an increase in the ambient magnetic field
- Acceleration/transport continues until ions drift out of the flow due to the gradient-curvature drift

Magnetic gradient trapping

- Inverse magnetic field gradients associated with a dipolarization front form magnetic islands that can trap ions on the guiding center trajectories circling the front
- Trapping enables ions to propagate with the front earthward over multiple Earth radii producing efficient ion acceleration
- Ukhorskiy+ 17,18 (see also Gabrielse+ 17, Sorathia+ 18)

Other mechanisms

- Surfratron: Artemyev+ 12, Ukhorskiy+ 13
- Reflection: Zhou+ 10,11
- Betatron: Birn+ 12

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3D MHD+TP LFM+CHIMP

K₀ = [2,100] keV PA = [70°,100°]



Bubbles Matter For ...

Plasma and flux transport into the inner magnetosphere

Global (fluid) models can study bubble formation in a self-consistent(-ish) way

- Cramer+ 17 used OpenGGCM+RCM event survey to confirm critical role of bubbles seen in IMAG-only models
- Merkin+ 19 used LFM to show localized bursts are responsible for global dipolarization (see also Birn+ 19)
- Spacetime plots: "MLT" vs. time





But global (MHD+inner mag) models don't have ...

- Transition region physics (self-consistent drifts + fastflows)
- Ion kinetic effects critical to substorm onset (e.g. thin current sheets, see Stephens+ 19)
- Self-consistent (or any) anisotropy (see Lin+ 21)
- Wave acceleration: KAW's (Cheng+ 20), broadband (Chaston+ 14)

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GAMERA+RCM sim of Merkin+ 19 event

Bubbles are ...

Unavoidably kinetic

Self-consistent ion kinetic physics

- Particle ions and fluid electrons
- Demonstrated formation of bubbles (Lin+ 17,Lin+ 21)
 - Bubbles created via reconnection, reduction in FTV
 - Pressure is anisotropic and varying along field line
 - Flow-braking and anisotropy generation w/ coupled IMAG model (CIMI)
- Non-MHD wave acceleration, KAW (Cheng+ 20)
 - E// is effective for particle acceleration

But

- Computationally very demanding, typical sims are ~hrs
- Important multi-day geospace effects, e.g. storms





 $\chi(R_{\rm B})$

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• 2x energy density delivered to inner

magnetosphere in higher res run

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Injection depth is critical

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- Long-term trapping requires sufficient penetration depth
- Depth set by FTE depletion and background



Only see numerical stability of BBFs at high

resolution

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Key points

It's a great time to be a modeler!

Huge challenges ahead for crossscale global kinetic modeling!



Complex landscape to navigate

- Algorithmically complex, massively-coupled models
- Increasingly exotic supercomputing tech
- More observational data to assimilate/ingest
- Learning how to learn from massive simulation data sets
- How do we leverage machine learning while still doing human learning?



Plenty of opportunities for young people in modeling!

Students/Early-career: It's a great time to be a young modeler

- Why? Lots of opportunities to build new models, find clever new approaches, extend existing models
- How? Take interdisciplinary classes (math/computer science), become a killer coder, and start modeling
- Always have a lucrative tech job as a fall back option





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We are hiring

- Postdoc positions @ JHU/APL (modeling & data analytics)
- Postdoc @ UCLA (Ionosphere/plasmasphere modeling, Prof. Roger Varney)
- Graduate students @
 - VT (Profs. Mike Ruohoniemi & Lenny Smith)
 - Rice U (Prof. Toffoletto)

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Post Doctoral Fellow - Space Plasmas Theory and S...

careers.jhuapl.edu

Bursty bulk flows drive mesoscale currents into the ionosphere

CGS

Intense localized ionospheric currents and thermosphere heating

- Localized current "wedgelets"
- Intense auroral zone closure currents in the ionosphere (~100 km scale size)
- Cumulative effect on geomagnetically induced currents (GICs) is unknown



Bursty bulk flows drive mesoscale currents into the ionosphere

Intense localized ionospheric currents and thermosphere heating

High resolution is key (again!)



Smoothing and attenuation of magnetic perturbations with altitude

Ground magnetometers may not be sufficient!



GAMERA simulation by Sorathia et al. (2020)

Electrojet Zeeman Imaging Explorer (EZIE): A CubeSat Mission to Visualize Electrical Currents in Space

"EZIE is a cost-effective" multi-CubeSat mission that visualizes, for the first time with innovative instrumentation, the electrojets, the electric currents flowing at altitudes of ~100– 130 km, which are notoriously difficult to explore. EZIE resolves mysteries of these electrojets and paves the way for better predictions of space weather."





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The Auroral Electrojets Are Part of a Vast Electrical Current System



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Primary Science Question 2: Large-Scale vs. Wedgelets Impact





Primary Science Question 2: Large-Scale Electrojet vs. Wedgelets

The models differ in scale size and lifetime





How Can We Make Better Mesoscale Data-Model Comparisons?

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And this time it's not the fault of modelers!

We need more mesoscale-resolving data to compare to!

- Data paucity makes it difficult to perform quantitative multi-scale validation
- Some conjunctions (e.g. Turner+ 17) can use >12 spacecraft to shed light on the mesoscale picture but these are rare
- TWINS ENA mesoscale imaging (e.g., Keesee+ 21)

How do we solve the data paucity problem?

- More missions! Ideally: constellation of in-situ probes in the plasmasheet (e.g. MagCon) and simultaneous auroral and ENA imaging
- Different ways of using data
 - Comparing w/ DM/ML models trained on in situ data (e.g. Stephens+ 19)
 - Comparing w/ information theory e.g. conditional mutual information (e.g. Wing & Johnson 19)
 - Gets at core question, "Will we learn the same thing from models and data?"

