# Solar Data

Heliophysics Summer School, August 3rd 2022

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# Solar Astronomy 101

Most Salient Observational Features about the Sun

- It rotates, but not as a solid body. The equator rotates faster than the poles (use helioseismology to probe the interior).
- It has sunspots. The number of sunspots waxes and wanes with an eleven year cycle.
- Magnetic fields pervade the entire Sun.
- The Sun is a panchromatic astrophysical object.









from White [1977].







# THE ELECTROMAGNETIC SPECTRUM





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- Magnetic fields pervade the entire Sun.
- The Sun is a panchromatic astrophysical object.
- The hot corona consists of loops anchored at/near sunspots.
- Total eclipses are awesome (partial eclipses less so). 😂



Eclipse above Oregon on Aug 21st 2017 Credit: Miroslav Druckmüller, Peter Aniol, Shadia Habbal



Upcoming PUNCH mission measures polarized Thomson-scattered light





# un./Noon.You!

APRIL SOLAR ECLIPSE TOTAL SOLAR ECLIPSE





0.2 g/cm<sup>3</sup>

20 g/cm<sup>3</sup>

150 g/cm<sup>3</sup>

The Solar Interior

#### convective zone

2 million K

tachocline

radiative zone

7 million K

core

15.7 million K

Credit: Kelvinsong



0.0000002 g/cm³

0.2 g/cm<sup>3</sup>

The Solar Interior



5700 K

#### convective zone

2 million K

tachocline

radiative zone

Credit: Kelvinsong







0.0000002 g/cm<sup>3</sup>

neutrino

2.3 seconds

photon

10,000-170,000 years

### The Solar Interior



-the solar interior-

layers drawn to scale

#### corona

#### Chromosphere?

photosphere

5700 K

convective zone

Credit: Kelvinsong

Credit: Solar Dynamics Observatory / Stanford

-





#### THE MAGNETIC POLARITY OF SUN-SPOTS<sup>1</sup> By George E. Hale, Ferdinand Ellerman, S. B. Nicholson, and A. H. Joy

Whirling storms in the earth's atmosphere, whether cyclones or tornadoes, follow a well-known law which is said to have no exceptions: the direction of whirl in the Northern Hemisphere is lefthanded or counterclockwise, while in the Southern Hemisphere it is right-handed or clockwise. The theory of terrestrial cyclones is still very obscure, but the direction of whirl is evidently determined by the increase in linear velocity of the air from pole to equator, due to the earth's rotation. The question naturally arises whether storms in the solar atmosphere are also whirlwinds, and, if so, what law governs their direction of whirl in the Northern and Southern hemispheres.

The first definite evidence bearing on this question was obtained with the spectroheliograph in 1908.<sup>2</sup> Photographs of the hydrogen flocculi made with the Ha line showed clearly marked vortical structure in regions centering in sun-spots. This structure was found to be repeated in hundreds of spots, leaving no doubt as to the generality of the phenomenon. Furthermore, photographs were obtained showing masses of hydrogen in the act of being drawn from a great distance toward the center of sun-spots, as though sucked into a vortex.

These photographs suggested the hypothesis that a sun-spot is a vortex, in which electrified particles, produced by ionization in the solar atmosphere, are whirled at high velocity. This might give rise to magnetic fields in sun-spots, regarded as electric vortices. A search for the Zeeman effect led to its immediate detec-

# George Ellery Hale

Credit: Caltech Archives



# Sunspots are like planet-sized MRI machines



Penumbra 0.1 - 0.2 Tesla

Credit: Swedish Solar Telescope

Umbra 0.3 Tesla











Credit: Solar Dynamics Observatory / Stanford

1

-











1400 B = 0.00 Field strength (G) 1200 1000  $\gamma = 0$ . Inclination angle (deg) 800  $\varphi = 0$ . Azimuth angle (deg)  $^{\circ}$ æ 600 400 200 1508 1000 à 500 500 1000 1500 8.

Borrero & Ichimoto (Living Reviews in Solar Physics 2011) Note:  $IQUV(\varphi) = IQUV(\varphi + 180 \text{ deg})$ , known as the 180 deg ambiguity.







https://sot.lmsal.com/Data\_new.html

Hinode/Solar Optical Telescope Continuum





https://sot.lmsal.com/Data\_new.html

Hinode/Solar Optical Telescope Blos





https://sot.lmsal.com/Data\_new.html

Hinode/Solar Optical Telescope Btrans



# 2011/02/12 00:00:00

HMI vector magnetogram sequence of NOAA AR 11158 Credit: Keiji Hayashi (HMI)







0.0000002 g/cm<sup>3</sup>

neutrino

2.3 seconds

photon

10,000-170,000 years

### The Solar Interior



-the solar interior-

layers drawn to scale

#### corona

#### Chromosphere?

photosphere

5700 K

convective zone

Credit: Kelvinsong



#### Vernazza, Avrett & Loeser (1981)







### Leenaarts (Living Reviews in Solar Physics, 2020): "Net radiative cooling in the 1D semi-empirical VAL3C model atmosphere. The cooling between z=700 km and z=2120 km in this model is dominated by five lines from Call and two lines from Mg II. At larger heights H I Ly $\alpha$ alone is the dominant radiative cooling agent."



#### Wedemeyer-Böhm et al. 2012

THE INTERNATIONAL WEEKLY JOURNAL OF SCIENCE

How supertornadoes up the temperature in the Sun's outer atmosphere



#### H5N1 – FIVE BIG OUESTIONS What it will take to size up the threat MEE 458

AGREGATIONE PIGS WEANED OFF DRUGS Danish farmers cut dependence on antibiotics

MGE 485

ESCIENCE FIGHTON ARCHITECT OF THE FUTURE David Brin celebrates Ray Bradbury's staton MEEAN DENATURE COMMATURE No. American Vel. 485, No. 7404







Wedemeyer-Böhm et al. 2009







## IRIS raster scan of an EFR: Mg II k and Mg II triplet

Scanning from the wing to the k3 (core), one sees the transition from reversed granulation to arch filaments / fibrils.

2808







## IRIS raster scan of an EFR: Mg II k and Mg II triplet

Scanning from the wing to the k3 (core), one sees the transition from reversed granulation to arch filaments / fibrils.







# IRIS raster scan of an EFR: Mg II k and Mg II triplet

Scanning to the Mg II triplet, one sees different structure in the chromosphere (seemingly lower lying loops).



Large sparse 64-step raster 63x120 64s Deep x 4 Spatial x 2, Spectral x 2 Duration: 329.8 s OBS ID:3860106092 Date obs:2015-08-19T07:48 Blue wing Near k2v

2795

IRIS Mg II rasters of an emerging active region @ 330s cadence Mg II triplet lines are a diagnostics for low chromospheric heating (Pereira et al. 2015)

#### iris.lmsal.com



#### Mg II triplet Near k2r







### Courtesy: L. Rouppe van der Voort / RoCS / SST

Daniel K Inouye Solar Telescope on Haleakalā, Maui, HI





### Courtesy: NSF/NSO/AURA DKIST/VBI red channel ~7058 Å

# 10,000 km 6,200 miles




#### Courtesy: NSF/NSO/AURA DKIST VBI red channel ~7058 Å

12 Dec. 2019 19:24:31 UT 37







One of these images is a DKIST observation, the other is a synthetic image from a radiative MHD simulation (Rempel 2014). Which is which?



# The Coronal Heating Conundrum

- There is lots of energy available.
- The solar atmosphere is strongly stratified.
- Radiative flux at photosphere ~  $6 \times 10^{10}$  erg cm<sup>-2</sup> s<sup>-1</sup>
- Power required to sustain the corona ~  $10^{5-7}$  erg cm<sup>-2</sup> s<sup>-1</sup>
- But that doesn't mean the coronal heating conundrum is uninteresting. Analogy: Food supply in the world.

15 million K	Temperature	1 million K			
150 g cm <sup>-3</sup>	Mass Density	1x10 <sup>-15</sup> g cm <sup>-3</sup>			
2x10 <sup>17</sup> erg cm <sup>-3</sup>	Internal Energy Density/Pressure	0.1 erg cm <sup>-3</sup>			
	39				





SDO images the sun's surface, atmosphere and interior. The mission generates 2 TBs worth of science data everyday. 

....



3 instruments monitoring the Sun all the time since May 2010.

- <u>Atmospheric Imaging Assembly:</u> visible, UV, and EUV full disk images of the photosphere, chromosphere, transition region and corona at 4096x4096 pixels.
- <u>Helioseismic & Magnetic Imager:</u> visible light full disk dopplergrams and magnetograms at 4096x4096 pixels.
- <u>EUV Variability Experiment</u>: disk-integrated EUV irradiance spectra at 1 Å resolution.

# SDO in a Nutshell







## Coronal mass ejection (CME) and flare in SDO/AIA













#### 2011-09-25T07:59:49





Szenicer, Fouhey et al. (Science Advances, 2019)







T. Woods

Woods et al. 2011 (ApJ) on late phase flares: "there is typically 40% more energy from this type of flare when including its EUV late phase contribution. "



https://lasp.colorado.edu/eve/data\_access/index.html

Time on 2010-May-5 (UT hours)



### 4096x4096 pixel images from SDO's Atmospheric Imaging Assembly (AIA) instrument

SDO/AIA- 94 2013/09/04 22:46:13

SDO/AIA- 131 2013/09,

SDO/AIA- 193 2013/09/04 22:46:06

SDO/AIA- 211 2013/09/04 22:46:11



SDO/AIA- 171 2013/09/04 22:46:11

SDO/AIA- 335 2013/09/04 22:46:14

Retrieval of temperature "Emission Measure" (EM) maps is an compressed sensing problem.





6.5 5.0 5.5 6.0 Cheung et al. Log10 [T<sub>e</sub> / K] (Astrophysical Journal, 2015)

7.5 7.0

**Problem Statement** 

 $\mathbf{x} = \mathbf{K}\mathbf{m} = \mathbf{K}\mathbf{D}\mathbf{y}$ rows of  $\mathbf{K}$  = response of wavelength channel

x = detector counts

 $\mathbf{m} = \mathbf{D}\mathbf{y},$ cols. of D = basis funcs

m = emission measure (EM) in temperature bins

EM = line-of-sight integral of electron density squared















Fraction of total emissio Ion  $T_{\rm p}^{\rm a}$ λ Å Κ QS AR CH FI 94 Å Mg viii 94.07 5.9 0.03 Fexx 93.78 7.0 0. 6.85 Fe xviii 93.93 0.74 0. 94.01 6.05 0.63 0.72 0.05 Fex 93.47 5.6 0.04 Fe vIII 93.62 5.6 0.05 Fe vIII 0.12 0.17 0.11 Cont. 131 Å O VI 129.87 5.45 0.04 0.05 7.15 Fe xxIII 132.91 0. 128.75 7.05 0. Fexu 0.09 Fe viii 130.94 5.6 0.30 0.25 Fe viii 131.24 5.6 0.39 0.33 0.13 0.11 0.20 0.54 Cont. 0. 171 Å Ni xiv 171.37 6.35 0.04 \_ 174.53 6.05 Fex 0.03 \_ 171.07 5.85 0.95 0.92 0.80 Feix 0. Cont. 0. 193 Å O v 0.03 192.90 5.35 192.85 6.75 Ca xvII 0. 193.87 6.55 0.04 Ca xiv 192.03 7.25 0. Fe xxiv 195.12 6.2 0.17 0.08 0.18 Fe xII 193.51 6.2 0.19 0.17 0.09 Fe xII 192.39 6.2 0.09 0.08 0.04 Fe xII 188.23 6.15 0.04 0.09 0.10 Fe xı Fe xı 192.83 6.15 0.05 0.06 0.04 Fe xı 188.30 6.15 0.04 0.04 Fex 190.04 6.05 0.06 189.94 Feix 5.85 0.06 5.85 0.07 Feix 188.50 0.05 Cont.

 Table 1. Predicted AIA count rates.

### Major EUV Lines in SDO/AIA passbands

n	211 Å	Cr IX	210.61	5.95	0.07	_	-	_
		Ca xvı	208.60	6.7	-	-	-	0.09
		Fexvii	204.67	6.6	-	-	-	0.07
		Fe xiv	211.32	6.3	-	0.13	0.39	0.12
10		Fe xIII	202.04	6.25	-	0.05	_	-
85		Fe xIII	203.83	6.25	-	-	0.07	-
		Fe xIII	209.62	6.25	-	0.05	0.05	-
		Fexi	209.78	6.15	0.11	0.12	-	-
		Fex	207.45	6.05	0.05	0.03	_	-
		Ni xi	207.92	6.1	0.03	-	_	-
		Cont.			0.08	0.04	0.07	0.41
07	304 Å	Неп	303.786	4.7	0.33	0.32	0.27	0.29
83		Неп	303.781	4.7	0.66	0.65	0.54	0.58
		Ca xviii	302.19	6.85	-	-	-	0.05
		Si xi	303.33	6.2	-	-	0.11	-
04		Cont.			-	-	-	-
	335 Å	Alx	332.79	6.1	0.05	0.11	-	-
		Mg viii	335.23	5.9	0.11	0.06	-	-
54		Mg viii	338.98	5.9	0.11	0.06	_	-
23		Six	341.95	6.05	0.03	0.03	_	-
		Si viii	319.84	5.95	0.04	-	-	-
00		Fexvi	335.41	6.45	-	-	0.86	0.81
U8		Fexiv	334.18	6.3	-	0.04	0.04	-
01		Fex	184.54	6.05	0.13	0.15	-	-
81		Cont.			0.08	0.05	_	0.06

O'Dwyer, Del Zanna, Mason & Weber (A&A 2010), using the CHIANTI atomic package

0.04 50

## Geometrical Interpretation of Problem $\mathbf{D} = \mathbf{KB}$

Х



We seek to build a column vector **x** by linear combinations of columns of the matrix **D=KB**. y<sub>i</sub> are the coefficients of the linear combination. More columns of **KB** from which to chose than components of x.

→ underdetermined problem. Do basis pursuit by minimizing L1 norm of y. (Chen, Donoho & Saunders, SIAM Review, 2001) We are seeking to solve for y



# Sparse Inversion by Basis Pursuit

Choose a `simple' solution.

- 1) It tends not to overfit (consistent with the principle of parsimony, i.e. Ockham's Razor).
- 2) It ensures positivity of the solution (if solutions exist). 3) It is an L1-norm minimization problem, so we can use standard techniques from compressed sensing (see works by Donoho, Candes
- and Tao).
  - BTW the L1-norm of a vector  $y = \Sigma |y_i|$
- 4) Speed: O(10<sup>4</sup>) solutions / sec with single thread running the IDL package.

## Cheung et al. (2015), <u>http://tinyurl.com/aiadem</u>

- $\chi$ **2** minimization methods:
- **Parameterization:** e.g. Guennou et al (2012a,b), Cheng et al (2012) **Regularization:** e.g. Hannah & Kontar (2012), Plowman et al. (2013) See Aschwanden et al. (2015, Sol Phys, 290, 2, 2733) for comparisons between methods.







Sec

#### Hinode/XRT





#### AIA DEM -> Mock XRT

Synthesized from AIA 1x1 binned EM

2D histograms 3.5 AIA EM -> XRT [Log10 DN / XRT pixel] 0.5 0.0 3.5 0.0 1.0 1.5 2.0 3.0 200 300 0.5 100 2.5 XRT Counts [Log10 DN / XRT pixel] x [arcsec] Synthesized from AIA 1x1 binned EM 3.5 3.0 AIA EM -> XRT [Log10 DN / XRT pixel] 2.5 2.0 1.5 0.5 3.5 0.0 3.0 100 0.5 1.0 1.5 2.0 2.5 200 300 XRT Counts [Log10 DN / XRT pixel] x [arcsec]

Also, see Su et al. (2018) for validation against RHESSI.



## Flares: Models vs Observations

# A fluid view of MHD

Magnetohydrodynamics (MHD) captures the following physical principles:

- Mass conservation
- Momentum conservation,  $\varrho \frac{D \mathbf{v}}{D t} = \nabla \cdot \underline{\sigma} + \varrho \mathbf{g},$
- Energy conservation
- Faraday's law of induction. (next slide)

n, 
$$\frac{D\varrho}{Dt} + \varrho \nabla \cdot \mathbf{v} = 0$$
,

$$\sigma_{ij} = -p\delta_{ij} + M_{ij},$$
$$M_{ij} = -\frac{B^2}{8\pi}\delta_{ij} + \frac{B_i B_j}{4\pi}.$$

ion, 
$$\varrho \frac{Ds}{Dt} = \frac{Q}{T}$$
,

\*Assumptions about material properties





# Faraday's Induction Equation

Faraday's induction equation is

where  $\mathbf{E}$  is the electric field and c is the speed of light. In the regime of ideal MHD where the plasma is a perfect electrical conductor the electric field  $\mathbf{E}'$  in the co-moving inertial frame of the plasma vanishes. Assuming the plasma velocity v has speed  $|v| \ll c$ , a Lorentz transformation to the 'lab' frame leads to

This yields the familiar Eulerian form o

In Lagrangian form, this equation becomes

Fluid expansion / compression

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times$$

$$\frac{D\mathbf{B}}{Dt} = -\mathbf{B}(\nabla \cdot$$

$$\mathbf{E}=-c^{-}$$

### $\frac{\partial \mathbf{B}}{\partial t} = -c\nabla \times \mathbf{E},$

 $^{-1}\mathbf{v} \times \mathbf{B}$ .

al MHD induction equation

 $\times (\mathbf{v} \times \mathbf{B})$ . (10)

 $\mathbf{v}$ ) + ( $\mathbf{B} \cdot \nabla$ ) $\mathbf{v}$ .

(11)

(8)

(9)

Stretching flow along magnetic field lines intensifies B

\*Assumptions about material <u>properties</u>





Yokoyama & Shibata (1998) •2D MHD model of flare reconnection.

•The efficient transport of energy released by reconnection is modeled as thermal conduction carried by electrons streaming along field lines.

 Energy dumped into the chromosphere leads to dense upflows (humps): "chromospheric evaporation"

•The model predicts density enhancement in the termination region.









#### M7.7 limb flare

Patsourakos, Vourlidas
 & Stenborg, 2013, ApJ,
 764, 125

- •Wei Liu, Chen & Petrosian, 2013, ApJ, 767, 168
- •<u>Rui Liu, 2013, MNRAS,</u> <u>**434**, 1309</u>
- •<u>Krücker & Battaglia</u>, 2014, ApJ, **780**, 107
- •<u>Sun, Cheng & Ding,</u> 2014, ApJ, **786**, 73





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#### **Chromospheric evaporation (hump)**

Downward mass pumping from reconnection outflow (blob)

2012-07-19T05:02

Dashed contours: Total EM =10<sup>29</sup> cm<sup>-5</sup> Solid contours: Total EM =10<sup>30</sup> cm<sup>-5</sup>





MHD Simulation of a Solar Flare (Cheung, Rempel et al. 2019)





#### Log Emission Measure [cm<sup>\*</sup>]

#### 26.00 27.00 AR 12017 @ 2014-03-28T15:20:13

#### EM in log T/K=[5.75,6.05]

EM in log T/K=[6.05,6.35]

EM in log T/K=[6.35,6.65]





### **NOAA AR 12017:**

one X-class ("Best Observed X-flare"), 3 M-class, and about two dozen C-class flares

Sunquake: Judge et al. (2014) Filament Eruption before X-flare: Kleint et al. (2015) IRIS Fe XXI FUV spectra: Young et al. (2015)Chromospheric Evaporation: Li et al. (2015)

## Synthetic GOES X-ray Light Curves GOES 15 X-ray Flux

Х

Μ

С

B



**C4** flare if measured by detectors on GOES 15. The free magnetic energy (actual minus potential field) dropped by ~5x10<sup>30</sup> erg (~10%) over 5 minutes.

# A Disk-center view overlaid on magnetogram

## Limb view Emission measure for T > 10 MK





Using using thermal bremsstrahlung, the model yields power law-like shapes for the X-ray spectrum (eg. RHESSI).

The multi-thermal nature of the magnetic structure gives rise to the apparent non-thermal behavior.

Above-the-loop-top harder X-ray sources (> 25 keV) are located above softer loop sources.



Hard x-rays  $\geq 25$  keV 6  $\leq$  Soft x-rays  $\leq 12$  keV



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#### AIA 131 Å

Expanded Owens Valley Solar Array (EOVSA)

EOVSA 10.2 GHz 10-Sep-2020 20:00 UT





the following suite of observing capabilities:



Coordinated observations are an integral part of the MUSE investigation. Coordination of MUSE with EUVST+Ground Based Observatories (GBOs such as DKIST) will address multiple NGSPM science objectives (see De Pontieu et al. 2022; Cheung et al. 2022).

# Next Generation Solar Physics Mission (NGSPM) The NSGPM is a mission concept developed by a panel of solar physics experts designated by NASA, ESA and JAXA. The NGSPM report prioritizes a mission with



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# Take home message



## Go for the Total Eclipse

Great

American

Eclipse

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## Other references

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Solar Irradiances, Kopp, 2017 <u>https://heliophysics.ucar.edu/sites/default/files/heliophysics/resources/</u>

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