<u>Large-scale Dynamics of the</u> <u>Solar Interior</u>

Nick Featherstone

Department of Space Studies, Southwest Research Institute

&

Department of Applied Mathematics, University of Colorado, Boulder

NASA & UCAR/CPAESS Heliophysics Summer School June 21, 2021

Long-Term Collaborators

- Bradley Hindman (CU Boulder)
- Keith Julien (CU Boulder)
- Benjamin Brown (CU Boulder)
- Geoff Vasil (Univ. Sydney)
- Michael Calkins (CU Boulder)
- Jon Aurnou (UCLA)
- Mark Miesch (UCAR)

Who are we? Why are we here?



The operation of the solar dynamo remains an outstanding problem in astrophysics.

This presentation will provide an introduction to the study of solar interior dynamics, and in particular to outstanding questions regarding the Sun's interior convection, which underpins the dynamo.

<u>Outline</u>

- Motivation
- Helioseismology
- Convection fundamentals
- Convection in the Sun
- Rotating Convection
- Dynamo Implications
- Moving forward

- Slide 4
- Slide 10
- Slide 17
- Slide 27
- Slide 41
- Slide 60
- Slide 72

Motivation



Detailed sunspot records from 1600s onward (Galileo Galilei, 1612)

Naked-eye observations from China since 23 BCE





Detailed sunspot records from 1600s onward (Galileo Galilei, 1612)

Naked-eye observations from China since 23 BCE

2021 Heliophysics Summer School

The Sun's Magnetic Cycle



- Magnetic activity increases with sunspot area
- Mean magnetic polarity reverses every 11 years

Sunspots: A Closer Look



Swedish Solar Telescope (visible; 430 nm)

MHD Induction: What is v?



To understand **B**, we must understand **v** and how it interacts with rotation!

<u>Helioseismology</u>



The Sound of Granulation

Solar Granulation Movie Swedish Solar Telescope Wavelength: 395 nm Duration: 1 hour





Helioseismology: Key Results





- Radiative Interior
- Outer 1/3 is convecting (2 x 10⁶ K temperature contrast)
- Home to the dynamo?

- Rotates differentially
- 24-day period equator
- 30-day period poles





Convection Zone Bulk

Temperature:14,400KDensity: $2x10^{-6}$ g cm⁻³

Temperature: Density: 2.3 million K 0.2 g cm⁻³

- 11 density scaleheights
- 17 pressure scaleheights
- Reynolds Number $\approx 10^{12} 10^{14}$
- Rayleigh Number $\approx 10^{22} 10^{24}$
- Magnetic Prandtl Number ≈ 0.01
- Prandtl Number $\approx 10^{-7}$
- Ekman Number $\approx 10^{-15}$

Convection Zone Bulk

	Temperature:	14,400K
Given that we know the	properties of	2x10 ⁻⁶ g cm ⁻³
this region, and given the should be convecting w	hat we know it	2.3 million K
should be convecting, what might we		0.2 g cm °
expect in terms of the flows?		scaleheights
		scaleheights
What is convection anyway?		umber $\approx 10^{12} - 10^{14}$
		mber $\approx 10^{22} - 10^{24}$
	• Magnetic Prandtl Number ≈ 0.01	
	• Prandtl Number $\approx 10^{-7}$	
	• Ekman Number $\approx 10^{-15}$	

A Few Convection Fundamentals

Convection 101 abbreviated fluid equations Density Pressure $\rho = \rho' + \rho_0 \qquad P = P' + P_0$ $\rho_0 g = \nabla P_0$ Hydrostatic Background

$$\frac{\partial \boldsymbol{v}}{\partial t} + \boldsymbol{v} \cdot \boldsymbol{\nabla} \boldsymbol{v} = -\boldsymbol{\nabla} P' - \frac{\rho'}{\rho_0} g \hat{\boldsymbol{r}} + v \boldsymbol{\nabla}^2 v$$

perturbations drive dynamics









Convective Mixing



- As fluid rises and sinks, the tendency is to mix temperature (or entropy)
- Efficient convection can modify the background thermal profile
- What determines the efficiency as Summer School

The Competition: Diffusion

• The momentum equation has a diffusion term:

$$\frac{\partial \boldsymbol{v}}{\partial t} = \dots + \boldsymbol{v} \nabla^2 \boldsymbol{v} \qquad \qquad \text{``nu'': kinematic viscosity}$$

• ... as does the temperature equation:

$$\frac{\partial T}{\partial t} = -\boldsymbol{v} \cdot \boldsymbol{\nabla} T + \kappa \boldsymbol{\nabla}^2 T \qquad \text{thermal diffusivity}$$

• ... as does the induction equation:

$$\frac{\partial \boldsymbol{B}}{\partial t} = \boldsymbol{\nabla} \times (\boldsymbol{\nu} \times \boldsymbol{B}) \dots + \eta \boldsymbol{\nabla}^2 \boldsymbol{B}$$
 magnetic diffusivity



Time / Height

- As a warm parcel rises, it mixes with its surroundings via diffusion:
 - Momentum \rightarrow slows down
 - Temperature \rightarrow cools down / weakens buoyancy
- Relative timescale of buoyancy vs. diffusion determines efficiency



Time / Height

• Competition between buoyancy and diffusion characterized via Rayleigh number Ra:

$$Ra = \left(\frac{\text{viscous diffusion time across layer}}{\text{freefall time across layer}}\right) \left(\frac{\text{thermal diffusion time across layer}}{\text{freefall time across layer}}\right)$$

- High Ra: Fluid moves across domain before diffusion has time to act.
- Low Ra: Diffusion slows rise/fall and prevents efficient transport of heat
- Convection sets in around Ra = 1,000
- What is Ra for the Solar convection zone? Let's estimate it.

Convection in the Sun

Exercise 1: The Diffusive Timescale

• Consider the 1-D diffusion equation:

$$\frac{\partial v}{\partial t} = v \frac{\partial^2 v}{\partial x^2}$$

• Seek a solution of the form:

$$T = Ae^{t/\tau}\sin(kx)$$

• What is τ ? Is it positive or negative?

Exercise 1: The Diffusive Timescale

- I find that: $\tau_{visc} = -\frac{1}{vk^2} \approx -\frac{\lambda^2}{v}$
- For the solar convection zone:

$$\upsilon \approx 1 \text{ cm}^2 \text{s}^{-1}$$
 $\tau_{visc} \approx 4 \times 10^{20} \text{s} \text{ (about } 10^{13} \text{ yr)}$
 $\lambda \approx 2 \times 10^{10} \text{ cm} \text{ (CZ depth)}$

• Thermal Diffusion Time:

 $\kappa \approx 10^7 \,\mathrm{cm}^2 \mathrm{s}^{-1}$ $\tau_{thermal} \approx 10^6 \, yr$

Exercise 2: The Freefall Timescale



^{*}Rast et al., 2008, ApJ, 673, 1209 ^{*}Kuhn et al., 1998, Nat. Lett., 392, 155

In Summary

$$\operatorname{Ra} = \left(\frac{\tau_{viscous}}{\tau_{freefall}}\right) \left(\frac{\tau_{thermal}}{\tau_{freefall}}\right) = \left(\frac{4 \times 10^{20} \, s}{10^6 \, s}\right) \left(\frac{4 \times 10^{13} \, s}{10^6 \, s}\right) \approx 10^{22}$$

- This is well above 1,000, so diffusive effects are minimal globally
- On small enough spatial scales, they WILL matter on the freefall timescale
- Estimate:

$$\tau_{freefall} = \frac{\lambda^2}{\upsilon} \to \lambda \approx 10 \ m$$

On par with the length of a typical room in your home.

What Might we See: Canonical Picture





Ahlers, Grossman & Lohse, 2009, Rev. Mod. Phys., 81, 503

Schematic Power Spectrum



Increasing Wavenumber/ Decreasing length scale



https://youtu.be/OM0l2YPVMf8

 $Ra = 10^{13}$

2021 Heliophysics Summer School

What About in a System like the Sun?

- Density scale height acts like box scale:
 - Compressibility \rightarrow Small structure near surface
 - Large structure throughout
 - Density scale height O(100) Mm at CZ base



Base of the convection zone

Hotta et al., 2014, ApJ, 786, 24



Red Downflow / Blue Upflow

Image Credit: Bob Stein (MSU) Chris Henze (NASA) https://web.pa.msu.edu/people/steinr/research.html

What do we see on the Sun? Surface Convective Spectrum


Supergranulation

L \approx 30 Mm Harmonic Degree 100 U \approx 400 m s⁻¹

AIA 1700

Probing Deeper: Local Helioseismology



- Using helioseismology, we can also measure convective flows below the surface.
- Are large-scale flows possibly visible there?

Featherstone et al., 2010



How Deep Can We Go?

- Axisymmetric flows imaged throughout convection zone.
- Other flow measurements confined to upper 15% ...
- Not all observations agree...



The Convective Conundrum



- Large-scale power appears to be missing or very weak
- Disagreement between helioseismic analyses
- Where does supergranulation come from?
- How does Sun transport its heat with such weak flows?

The Convective Conundrum



The Effect of Rotation

Rotating Convection

- The Sun rotates once every 27 days.
- Rotation changes the picture drastically.
- Rotational influence on flow traditionally characterized in two ways
- The first is via the Ekman number Ek:

Ek
$$\equiv \frac{\text{rotation period}}{\text{viscous timescale}} \approx 10^{-15}$$
 in the Sun

- This tells us that relative to rotational effects, viscous diffusion is very weak.
- Unsurprising given our earlier analyses and the fact that the Sun rotates every 27 days.

<u>The Rossby Number</u> (this is important)

- The other way we quantify the effect of rotation on convection is through a Rossby number Ro.
- Different ways to define, but all have the same flavor:

 $Ro \equiv \frac{rotation \ period}{convective \ timescale}$

- High Ro \rightarrow weak rotational influence
- Low Ro \rightarrow strong rotational influence
- How/why?

<u>The Coriolis Force</u> (still important)

- Two important effects arise from the Coriolis force:
 - 1. Strong Coriolis force implies invariance of convective structure with rotation axis (Taylor Proudman effect; stated without proof)
 - 2. Fluid motions become curved...
- Coriolis force given by:

$$F_{C} = -2m\Omega \times v$$

• Mathematically similar to Lorentz force, so we define a gyro radius:

$$r_{gyro} = \frac{v}{2\Omega}$$

<u>The Gyro Radius and Rossby Number</u> (still important...almost there)

- Let's look more closely at this.
- Let L be convection zone depth. Multiply by one...

$$r_{gyro} = \frac{v}{2\Omega} = \frac{L}{L} \frac{v}{2\Omega} = L \left(\frac{1}{2\Omega}\right) \left(\frac{v}{L}\right)$$
$$r_{gyro} \approx L \left(\frac{rotation \ period}{1}\right) \left(\frac{1}{convective \ overturning \ time}\right)$$

 $r_{gyro} \approx L Ro$

The Coriolis Force, the Rossby Number & Everything

- Two important effects :
 - 1. Structures align with rotation axis

Ω

2. Fluid motions become curved:

$$r_{gyro} = \frac{v}{2\Omega} \approx L Ro$$

• So what do we expect?



Non-rotating / Rapid Flow (High Ro)

Rapid Rotation / Low Speed (Low Ro)

2021 Heliophysics Summer School



OK, but wasn't this really just a bunch of "twiddle algebra?"

Fully 3-D, nonlinear

numerical models

bear this out.

Not Just Theoretical Musing! Experimental Results...



Cheng et al., 2015, GJI, 201,1 NoMag Experiment, SpinLab UCLA

rapid rotation / columnar cells

2021 Heliophysics Summer School

no rotation / Isotropic tusbulence



Flow Patterns at Different Rotation Rates (red upflow, blue downflow)



https://youtu.be/3iRggdo3i0I

(www.youtube.com/feathern24)



Hindman et al. 2020 Model #47 Antisolar/Polar Plumes Rayleigh Number = 1.63×10^7 Ekman Number = 3.46×10^{-4} Rossby Number = 4.62×10^{-2}



Scaling of Spectral Peak





- Change in spatial scale apparent in spectra
- Ro dependent
- Look at peak spectral power vs. Ro

Ro^{-1/2} Scaling:

- Triple Force Balance
- Non-diffusive



Where is the Sun on this Spectrum of Behavior?



Estimate the Rossby Number:

mean rotation period: 27 days

convective turnover time?

$$\tau_{conv} \approx 2\tau_{freefall} \approx 24 \ days$$

 $Ro \approx 1$

- Ballpark estimate only lots of assumptions
- Still, rotation matters Sun not at extrema
- Probably more to the right than the left
-Why?



Antisolar Differential Rotation

- Isotropic convection will try to mix (homogenize) angular momentum
- Star with solid-body rotation.
- Angular momentum is highest at the equator. Lowest at pole.
- Poles spin up. Equator spins down.
- Need a source of anisotropic transport to break this pattern.



Solar-like Differential Rotation

- In this state, angular momentum IS NOT homogenized.
- At low Ro, convection takes on columnar aspect.
- Columns drift and tilt in prograde sense.

Icarus, 190, 110

- Transfers angular momentum away from rotation axis.
- From this, we infer that Coriolis forces impact solar convection **←**Ω





Busse, F.H., 2002, Physics of Fluids 14, 1301

Differential Rotation and Rossby Number



AND: Glatzmaier & Gilman 1982; Brun & Toomre 2002; Gastine et al. 2014; Guerrero et al 2013; Kapyla et al. 2014 ...



Robust, Systematic Trend



Ro = 1 delineates a clear transition in behavior.

Can use this to check our earlier assumptions.

From solar-like to antisolar differential rotation in cool stars

Gastine et al., 2013, MRNAS Lett., 438, Issue 1, 11

Temperature Perturbation

- Recall that we assumed T' was roughly 1 K.
- Idea based on $1 = Ro_c$ as transition point
 - Measure a star's rotation rate
 - Measure a star's spectral type (to get CZ depth)
 - Classify a star's differential rotation and bound temperature fluctuations.
- EXAMPLE:
 - g at mid CZ is 379.3 m s⁻²
 - T at mid CZ is 9.6x10⁵ K (alpha = 1/T)
 - The Sun has a solar-like differential rotation.
 - Therefore:

$$\frac{1}{\Omega} \sqrt{\frac{g \propto T'}{L}} \le 1 \qquad \qquad T' \le \frac{\Omega^2 L T}{g} \approx 3.6 \text{ K}$$

Implications for the Dynamo

Where is the Sun on this Spectrum of Behavior?



... and why do we care?



Rotation Yields Helical Convection



Helical Convection Yields Differential Rotation



24-day period equator

• 30-day period poles

۲

Shearing:

- Latitudindal
- Radial (Tachocline)

An Interface Dynamo?



- 24-day period equator
- 30-day period poles



- Does tachocline shear form the basis of the dynamo?
- Parker, 1993, ApJ, 408, 707

Convection Also Drives Meridional Circulation



More generally, the location of the Sun along the Rossby spectrum seems key to reproducing several aspects of the dynamo in models...

Models: Magnetic Cycles



<u>Magnetic Features</u>



Models: Large-Scale Magnetic Structure



- Possible alternative to interface dynamo?
- Possibly working in tandem?
- Driven roughly equally by Omega and turbulent alpha effects

Models: Buoyant Magnetic Loops


Where do we go from here?

<u>Clues From Out of the Ecliptic?</u>

Differential Rotation

Meridional

Circulation



Is there a polar spinup?

What is the highlatitude structure of MC?

2021 Heliophysics Summer School

Clues From Out of the Ecliptic?



Non-rotating / Rapid Flow (High Ro)

Rapid Rotation / Low Speed (Low Ro)

2021 Heliophysics Summer School

Clues From Out of the Ecliptic?



- Clearly SOMETHING interesting at the poles
- Foreshortening effects and resolution constraints severe
- Need direct views over long periods!



If Time Allows: A Novel Experiment...



Cheng et al., 2015, GJI, 201,1

Controlled via tank height. ٠

٠



Experiments: What else do we lack?

- Extreme parameter regimes are not the only difficulties...
- Historically, other details difficult to explore experimentally:
 - Density stratification
 - Internal radiative heating
 - Spherical geometry/central force



Something New Under the Sun

UCLA Plasma Acoustics Experiment



Table-Top Plasma Acoustics Experiment



"Normal" State: Internally-Heated Plasma



 Rotation rate: 	50 Hz
Central temperature:	4,000 K
Outer temperature:	1,000 K
• Density:	O(10 ⁻⁴) g cm
 Ionization Fraction: 	10 ⁻⁵

-3

Experiment:

Pulse microwaves at resonant frequency of low-order, spherically symmetric mode.

Normal State



Microwaves pulsed off-resonance

Confined State



Microwaves pulsed on-resonance 29 kHz , Q = 700 - 900, Ma = 0.03 , 180 dB

Transition: Normal to Trapped

Rotation rate: 50 Hz

Phantom v2512 high-speed camera (33,000 Frames per Second)

Dynamics: Pycnoclinic Acoustic Effect

- Interaction of high amplitude sound w/ density gradients
- "Acoustic radiation pressure"

Standard Buoyancy

$$\frac{\partial \rho \boldsymbol{v}}{\partial t} = \dots + \alpha T' g \hat{\boldsymbol{r}} + \dots$$

Pycnoclinic "Buoyancy"

resonant mode velocity amplitude

$$\frac{\partial \rho \boldsymbol{v}}{\partial t} = \dots + \frac{\alpha T'}{2} \boldsymbol{\nabla} \langle v_s^2 \rangle + \alpha \langle v_s^2 \rangle \boldsymbol{\nabla} T' \dots$$





Rotation rate: 50 Hz

(11,000 Frames per Second)

Stable, radiatively heated interior.

Convectively unstable exterior...

The beginnings of a spherical convection experiment!

parameter		measure of
$\Delta \nabla \equiv \nabla - \nabla_{ad}$	superadiabaticity	Schwarzschild instability
$\mathrm{Ra} \equiv g \Delta \nabla d^4 / (\nu \chi H_\mathrm{p})$	Rayleigh nr.	thermal instability
$\text{Re} \equiv UL/v$	Reynolds nr.	hydrodynamic turbulence
$\mathrm{Rm} \equiv UL/\eta$	magn. Reynolds nr.	ratio of adv. to diff. of B
$\Pr \equiv \nu / \chi$	Prandtl nr.	ratio of smallest therm. to kin. scales
$Pm \equiv \nu/\eta$	magn. Prandtl nr.	ratio of smallest magn. to kin. scales
$Co \equiv 2\Omega L/U^{(a)}$	Coriolis nr.	rotational influence on flow
$\mathrm{Ta} \equiv (2\Omega d^2)^2 / \nu^2$	Taylor nr.	(de)stabilising effect of rotation
$S \equiv U \tau_{\rm c} / L$	Strouhal nr.	ratio of corr. time to turnover time
$Ma \equiv U/c_s$	Mach nr.	ratio of flow speed to sound speed
$\beta \equiv 2\mu_0 p/B^2$	plasma β	ratio of gas to magn. pressure

 Table 1. Dimensionless parameters characterizing convection and dynamo action

^(a) Identical to the inverse Rossby number. However, in some publications on stellar activity the Rossby number is defined as $P_{\rm rot}/\tau_{\rm c} = 4\pi/{\rm Co}$

Ossendrijver, M., 2003, "The Solar Dynamo," Astron Astrophys Rev, 11, 287

parameter (a) base of convection zone photosphere $\lesssim 10^{-6}$ $\Delta \nabla$ $\lesssim 0.5$ 10^{16} 10^{20} Ra 10^{12} 10^{13} Re 10^{10} 10^{6} Rm 10^{-7} 10^{-7} Pr 10^{-6} 10^{-3} Pm $2 \cdot 10^{-3} \cdots 0.4^{(b)}$ 15 Co 10^{27} 10^{19} Ta 10^{-4} Ma $10^5 \cdots 10^7 (c)$ $1^{(d)}$ β

Table 2. Representative values of dimensionless parameters in the Sun

^(a) Unless stated otherwise, estimated by setting $L \approx H_p$

^(b) Lower value: granulation; upper value: supergranulation

^(c) Magnetized plasma with $1 \leq B \leq 10$ T

^(d) Sunspots and magnetic elements