



# *Stellar Dynamos in 90 minutes or less!*

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*Research Computing*

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*( with contributions and inspiration from Mark Miesch )*



# Why are we here?

- Stellar dynamos: Outstanding questions
- A closer look at Solar Magnetism
- Dynamo theory in the solar context
- The big question: convective flow speeds
- Today: emphasize induction
- Tomorrow: more on convection

# Question

*What even is a dynamo?*



## Dynamo

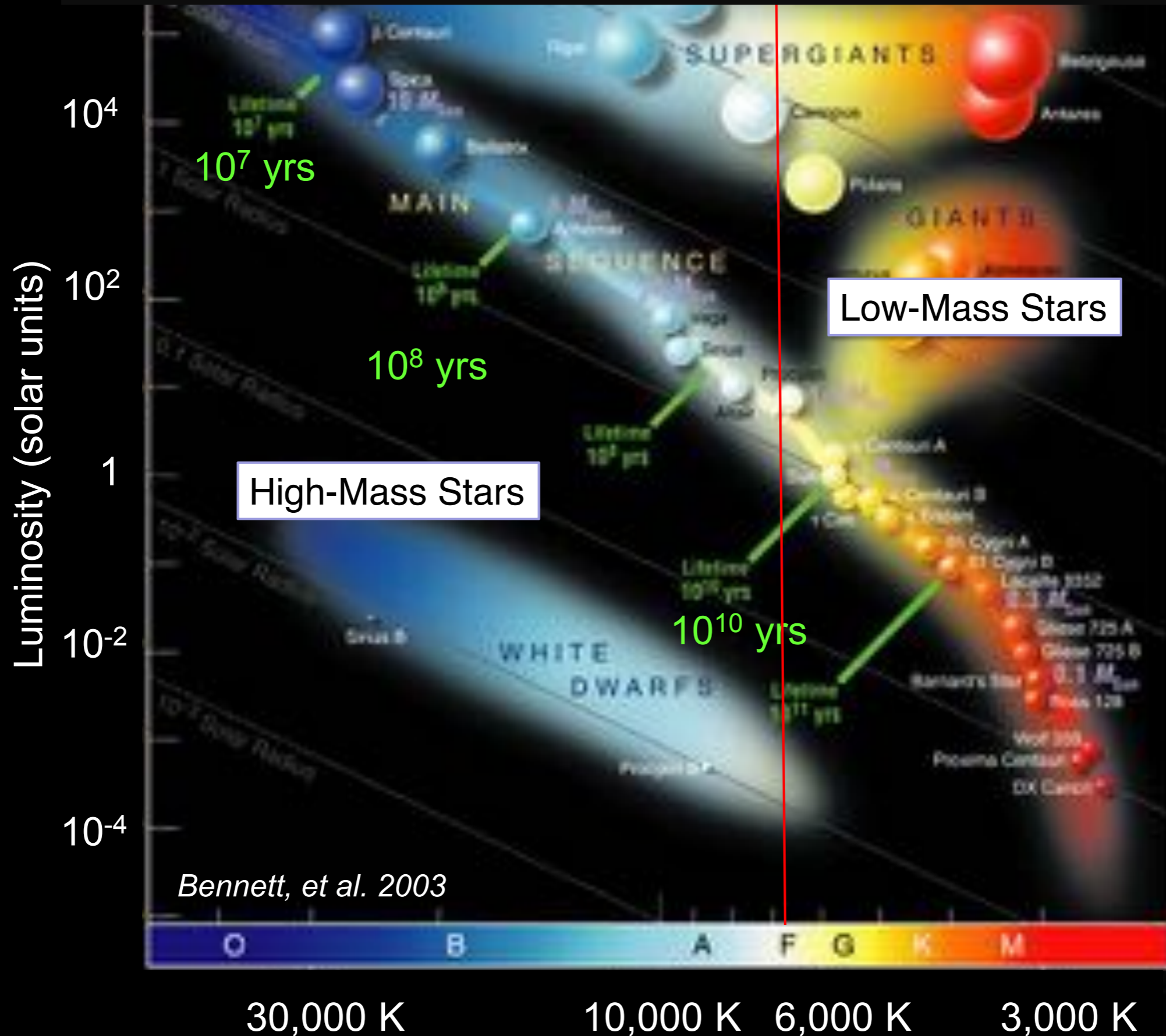
The process by which a magnetic field is sustained against decay through the motion of a conducting fluid.

## Stellar Dynamo

The process by which a star maintains its magnetic field via the convective motion of its interior plasma.



# One Broad Distinction



# Question

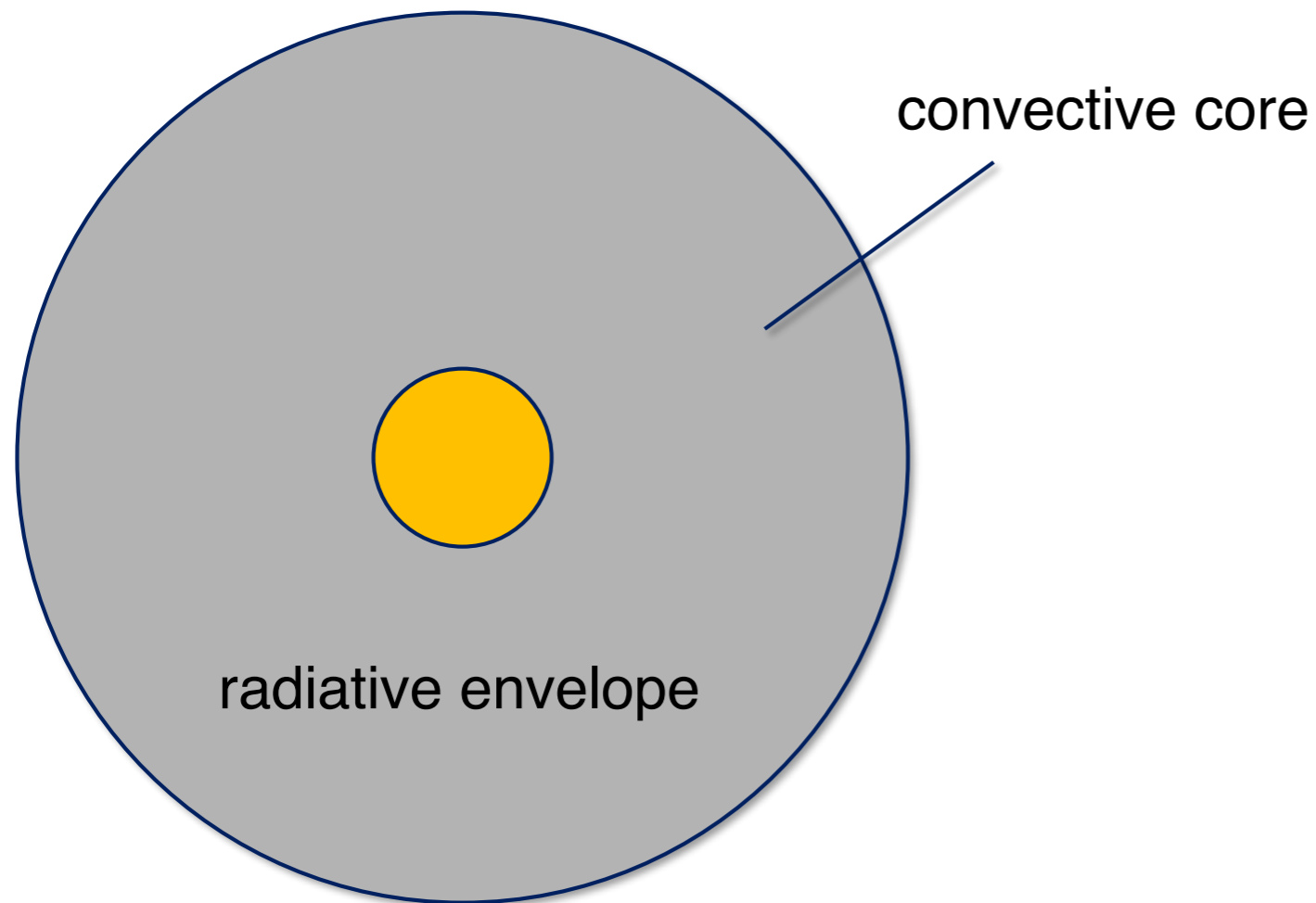
*As far as dynamo theory is concerned, what do you think is the main difference between massive and low-mass stars?*



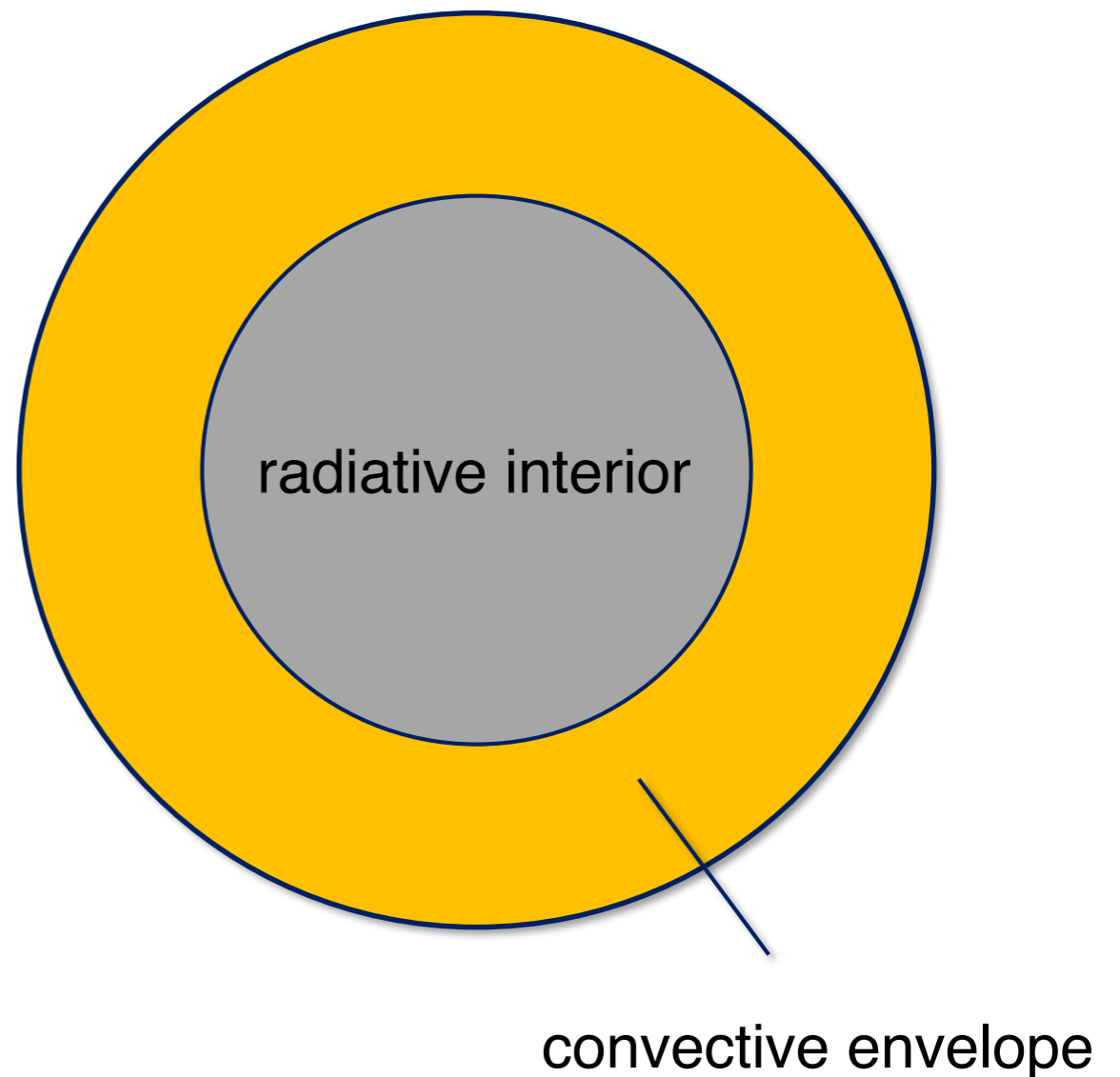
# Massive vs. Low-Mass Stars

The key difference is...  
...~~mass~~, ...~~luminosity~~, ...~~size~~ ... **geometry!**

*massive stars*



*low-mass stars*



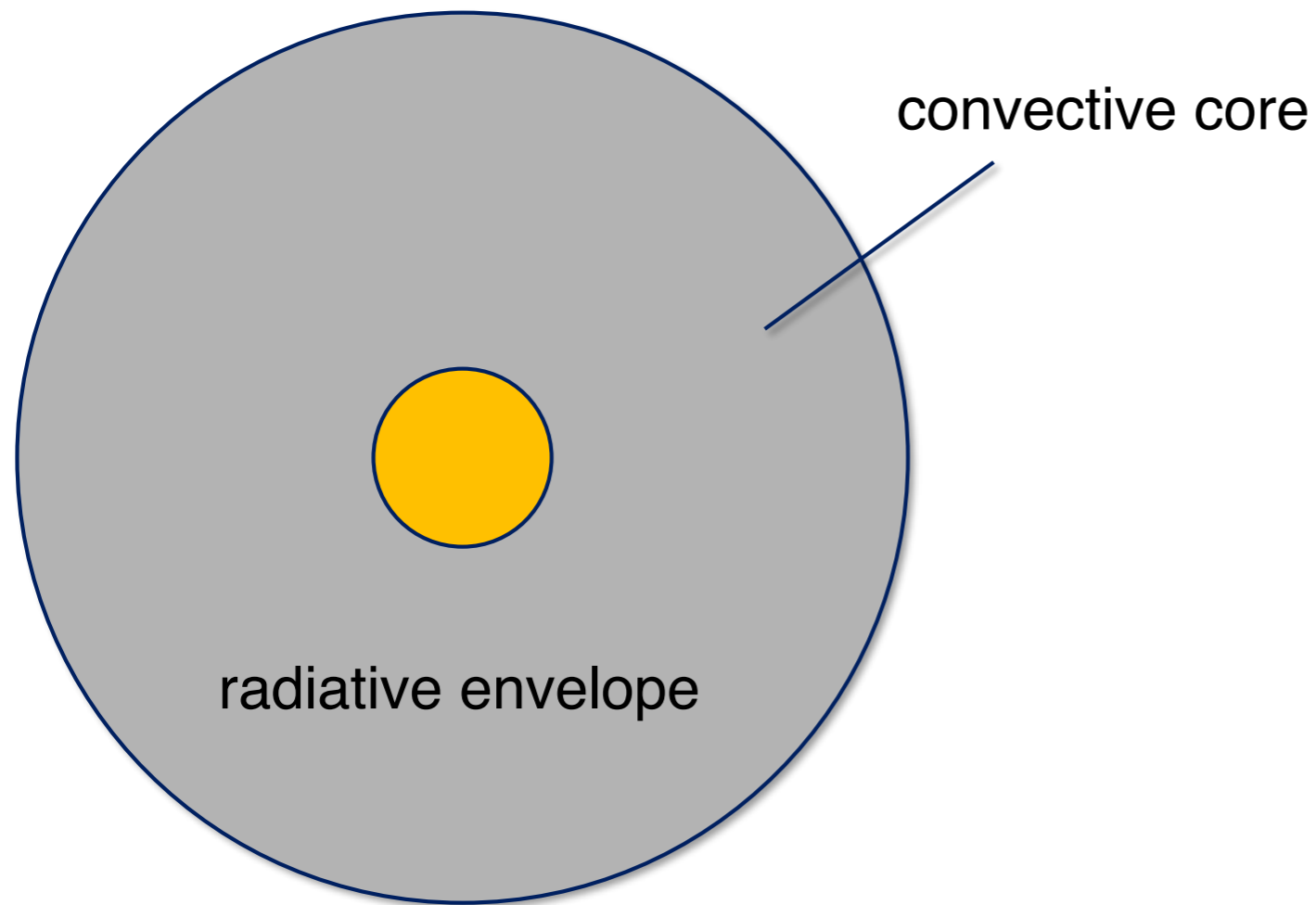
Different magnetic field configurations arise in different geometries.



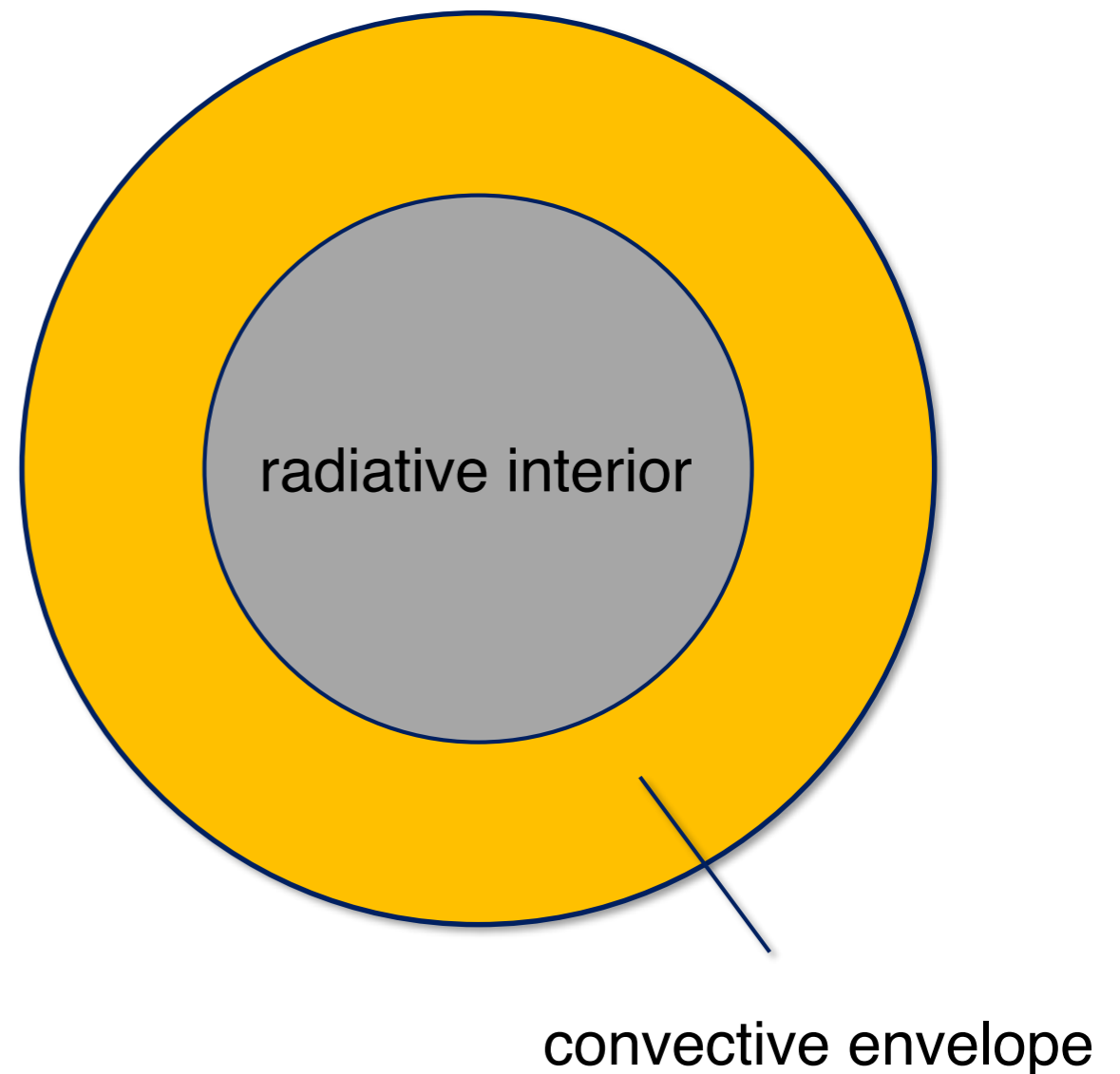
# Massive vs. Low-Mass Stars

Fundamental questions similar, but some differences.

*massive stars*



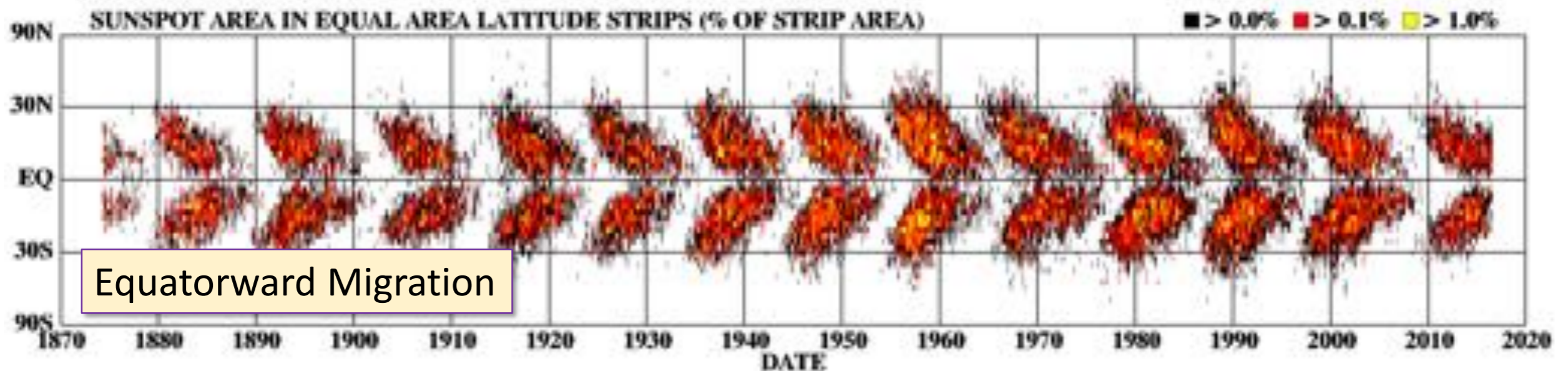
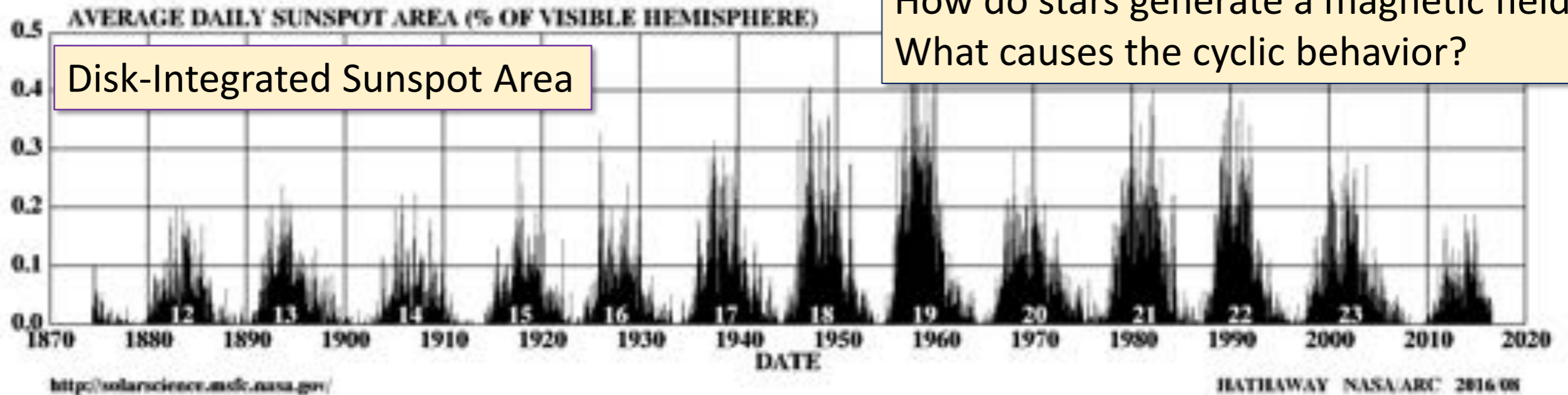
*low-mass stars*



Different magnetic field configurations arise in different geometries.

# Stellar Dynamo Question: The Sun's Magnetic Cycle

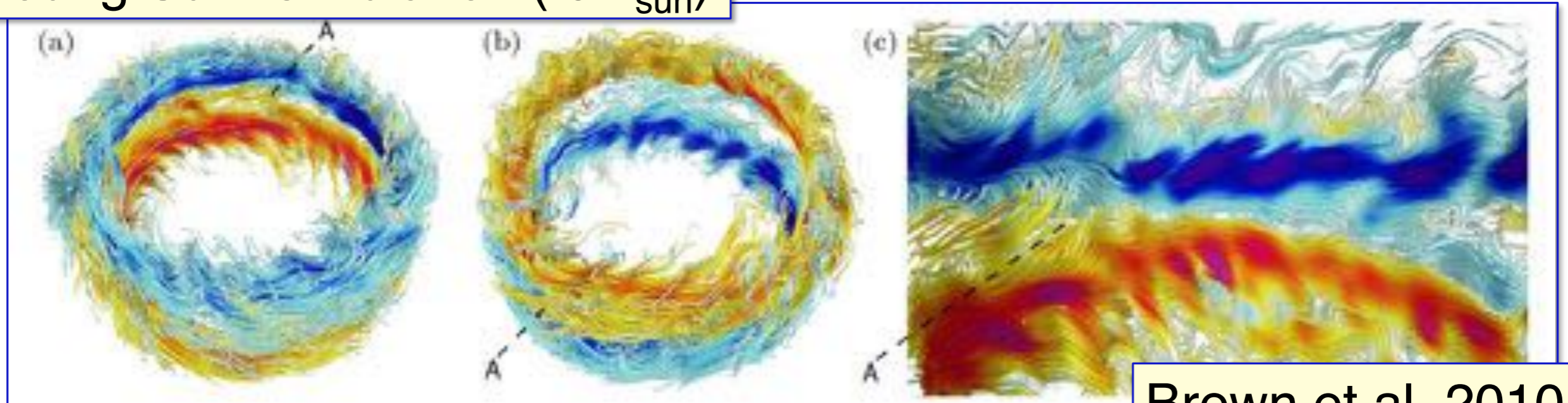
How do stars generate a magnetic field?  
What causes the cyclic behavior?



- Magnetic activity increases with integrated sunspot area
- Mean magnetic polarity reverses every 11 years

# Big Question: Magnetism and Stellar Age?

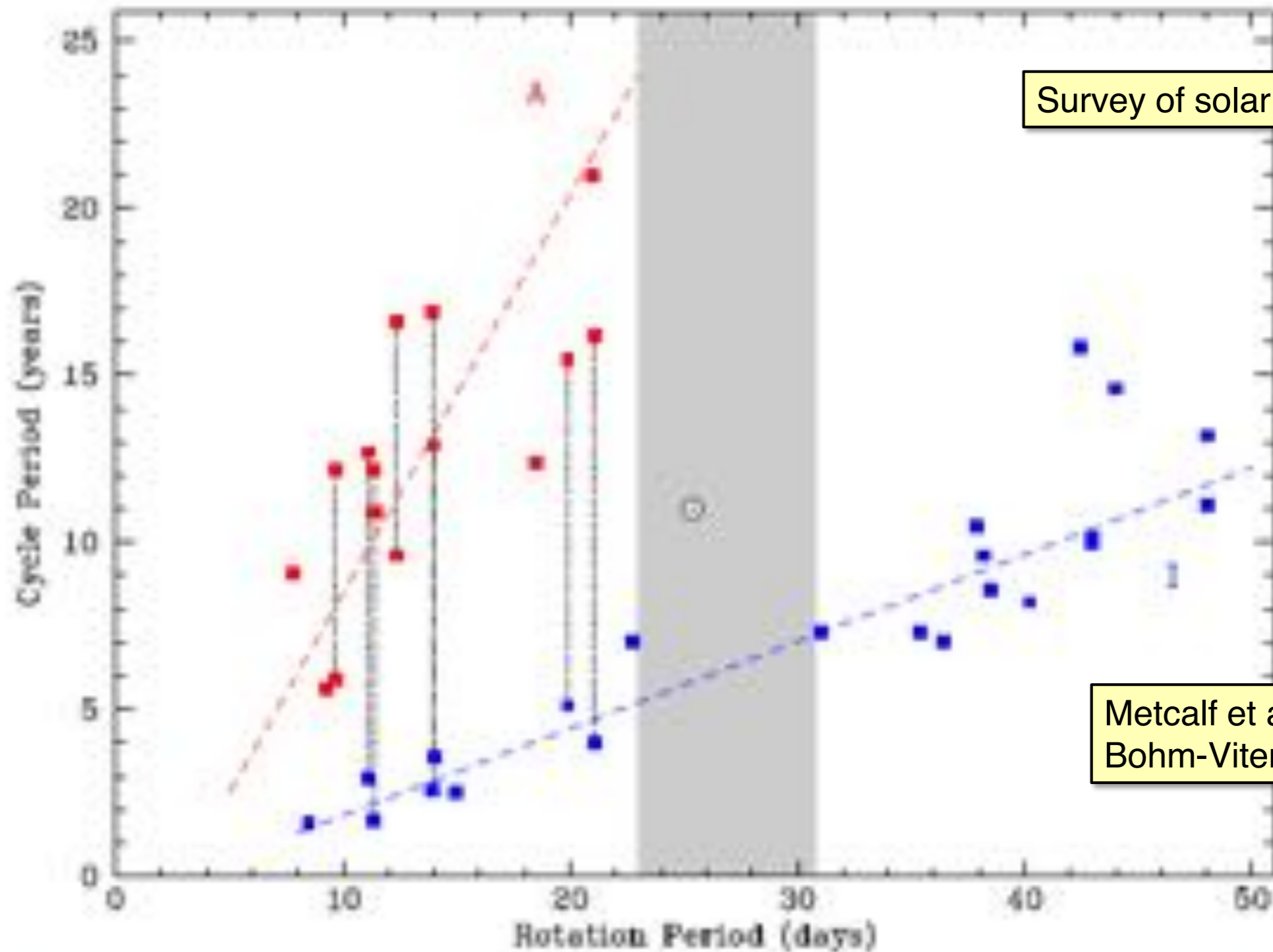
“Young Sun” simulation ( $3\Omega_{\text{sun}}$ )



Brown et al. 2010

- Stars rotate more slowly as they age.
- Rapid rotation favors large-scale magnetic fields.
- Is a tachocline necessary for organized field growth?

# Big Question: Is the Sun “normal”?

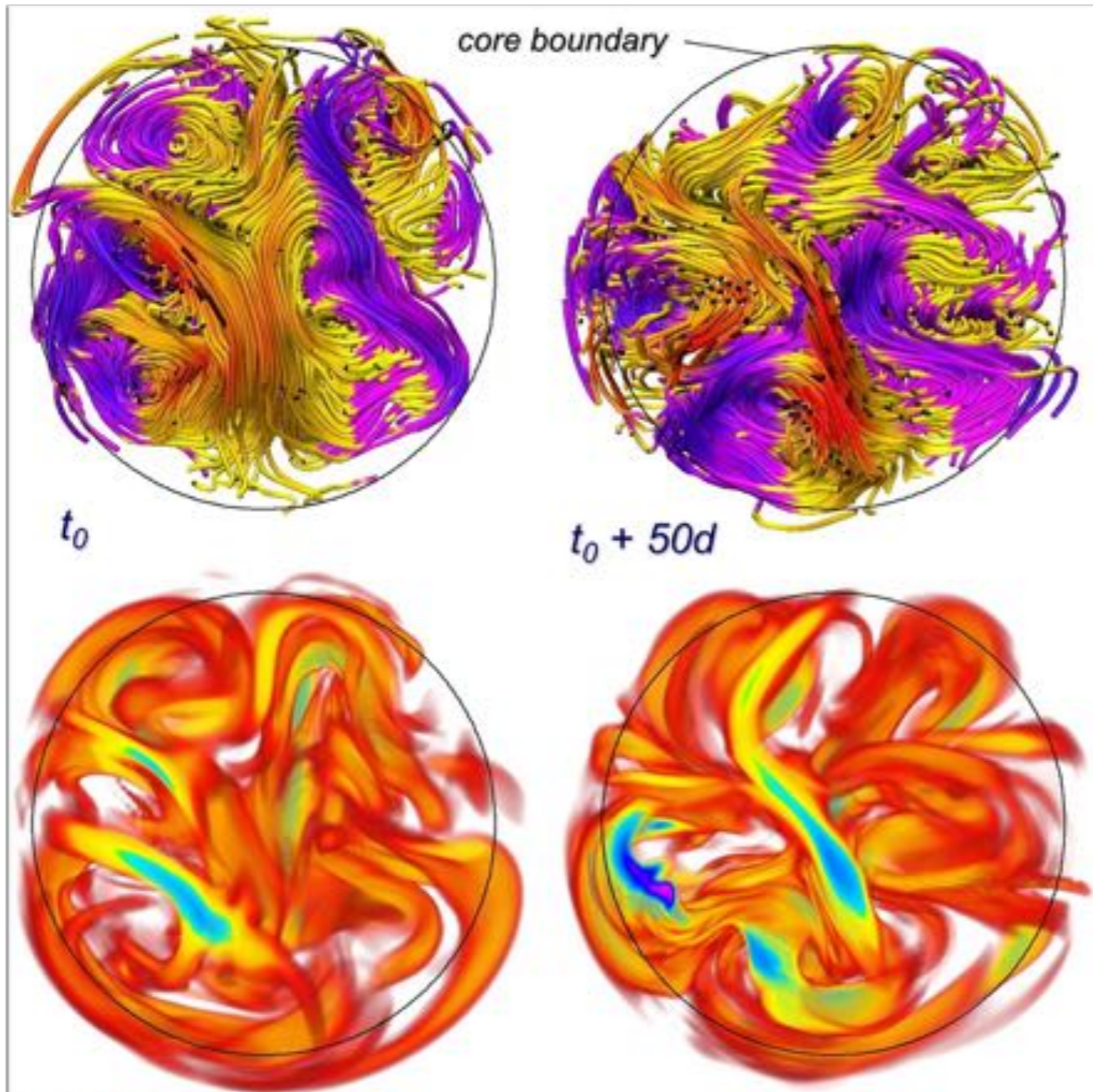


Survey of solar analogues

Metcalf et al. 2016  
Bohm-Vitense (2007)

# Big Question: Massive Star Dynamos?

streamlines



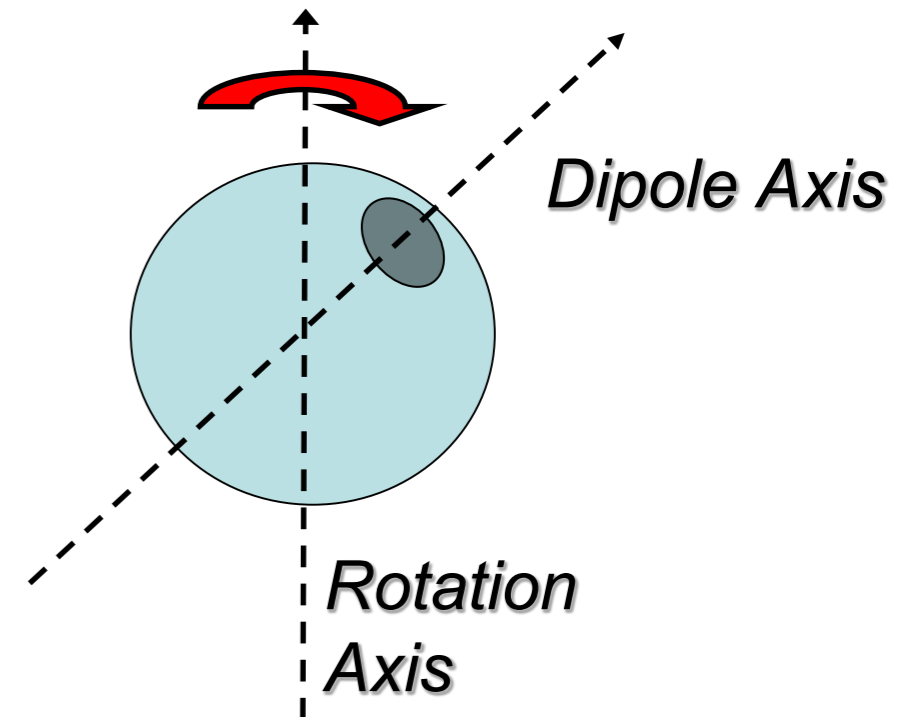
- How is the magnetic field structured?
- Are core-generated fields visible at the surface?
- Can core-generated fields become buoyant?

magnetic energy

Featherstone et al. 2010 (A stars)  
see also Augustson et al. 2016 (B stars)

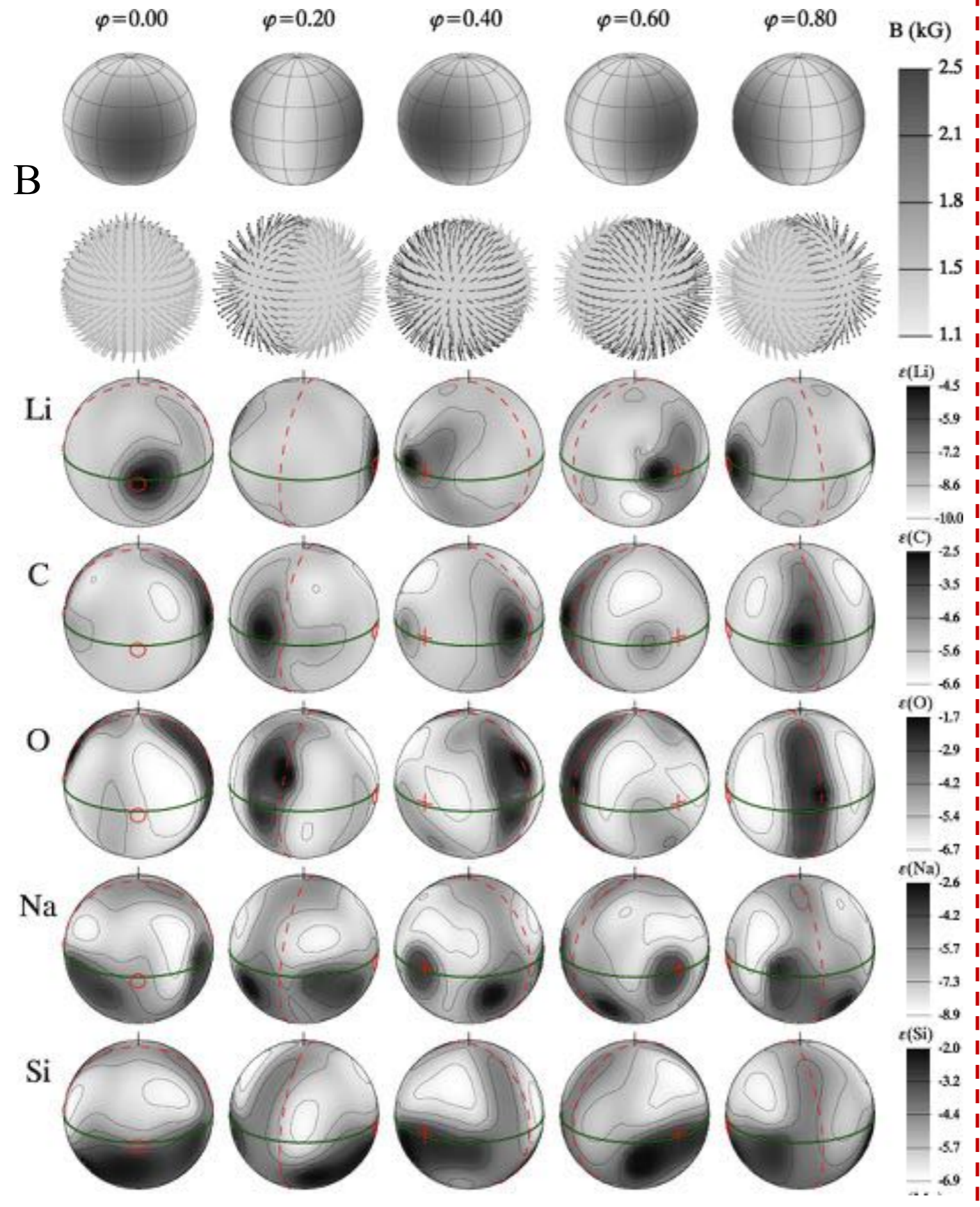
# Peculiar Question: Ap and Bp Stars

- Abnormally strong abundances of Si and various rare earth metals (Hg, etc.)
- Magnetic: typical field strengths of a few hundred Gauss.
- Field strengths and line widths vary periodically: Oblique Rotator Model
- Rotation periods from days to decades (magnetic braking?)



## Source of Magnetic Field?

- Core-dynamo? (but diffusion time through radiative zone very long)
- Primordial magnetic field?



*Magnetic Field*

*Abundance Maps*

*Magnetic Doppler Imaging*

*Ap Star HR3831*

*Kochukhov et al. 2004*

# Big Question: Exoplanets and Host-Star Magnetism

## TRAPPIST-1 System

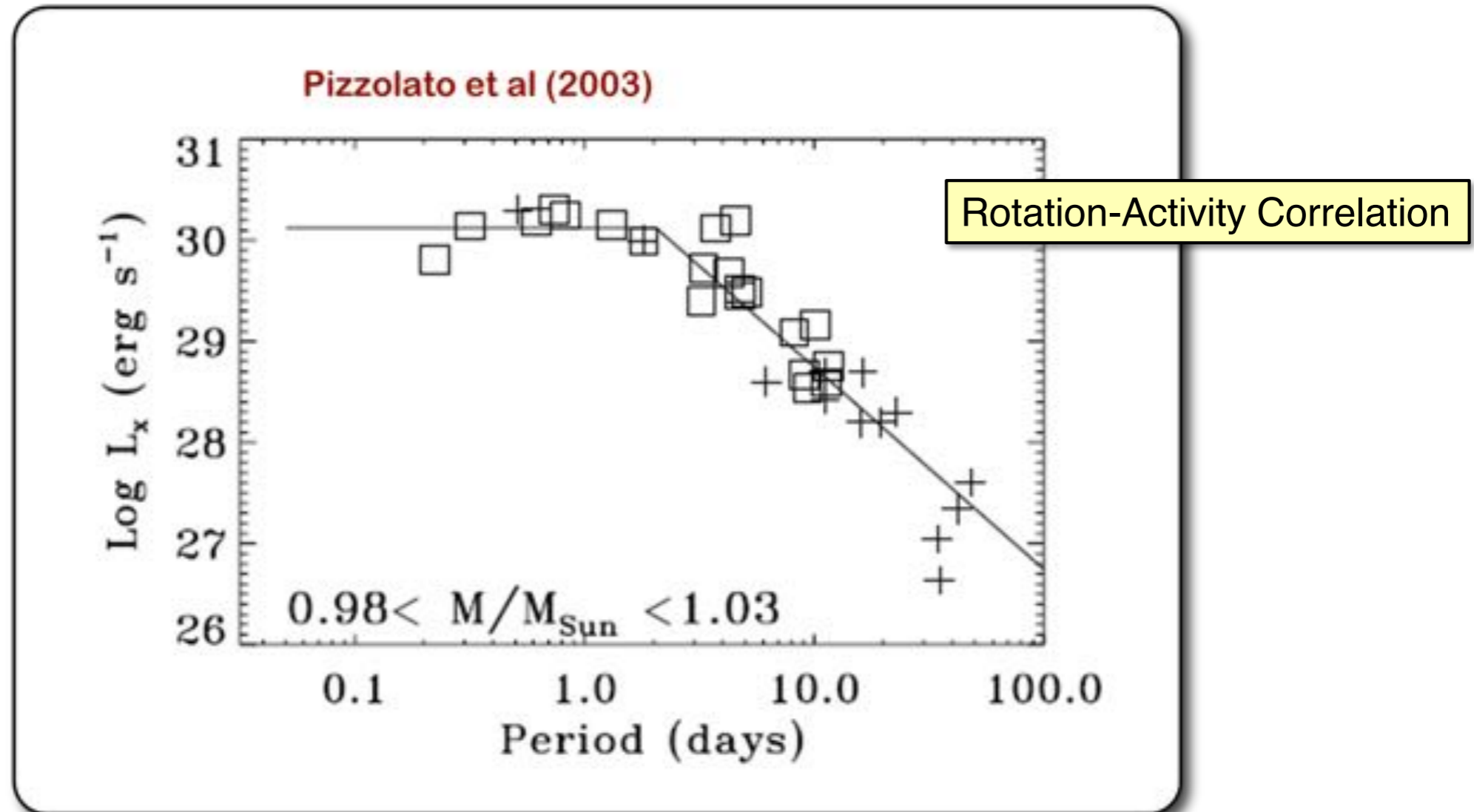


- Exoplanets most easily found around low-mass M dwarfs
- Vigorous dynamo action + fierce flaring
- How does magnetism impact habitable zone?

Illustration  
Credit: NASA/JPL-Caltech



# Big Question: Relationship between Magnetism and Stellar Rotation Rate?



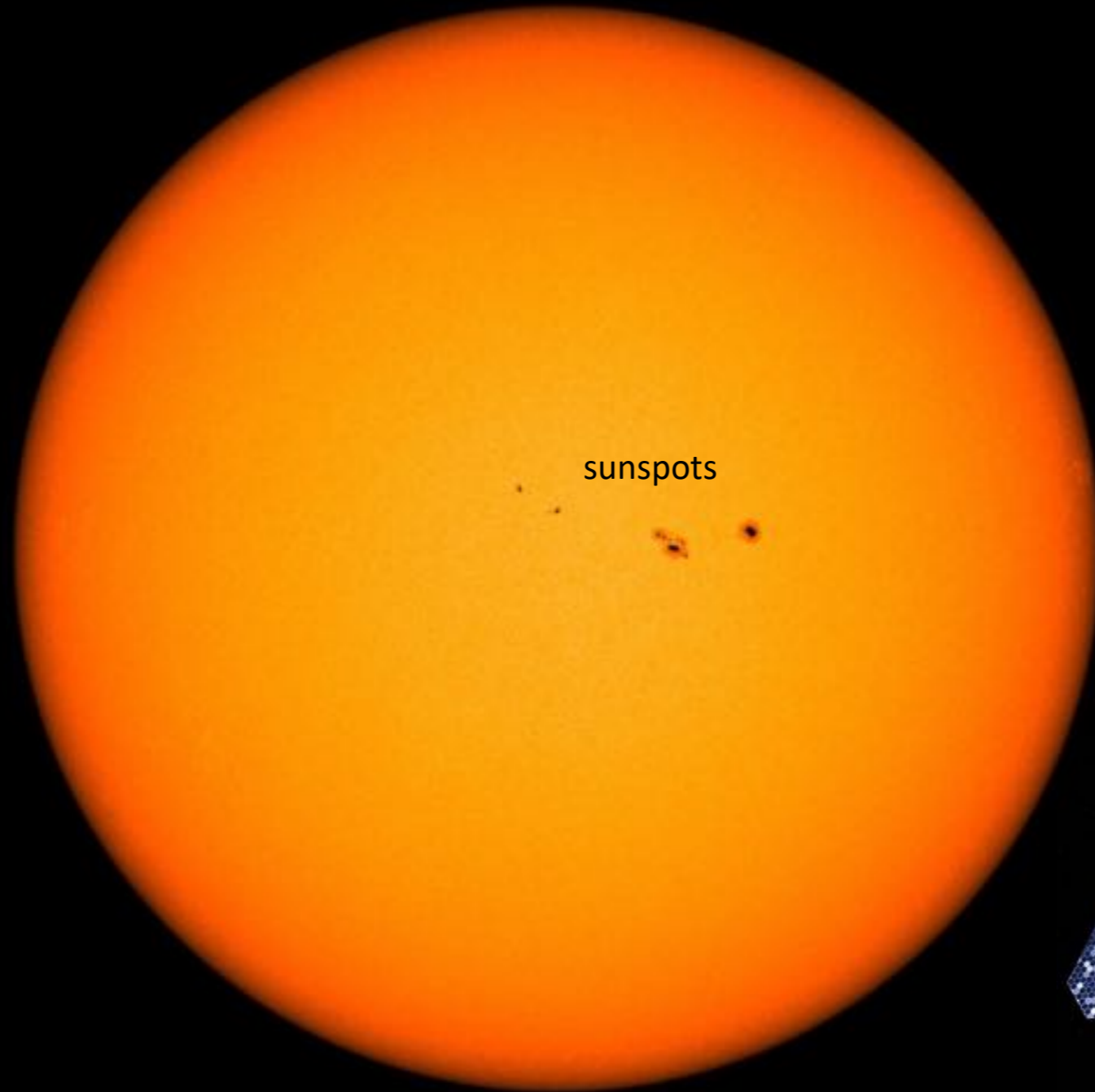
- Solar-like stars shown
- General trend holds for all low-mass stars
- What causes saturation?

# At the end of the day...

- The Sun is a star
- Stellar magnetism is the superset of solar magnetism
- We study stellar dynamos indirectly via the Sun as much as we do directly via observations
- Let's turn to the Sun, which we can **RESOLVE!**

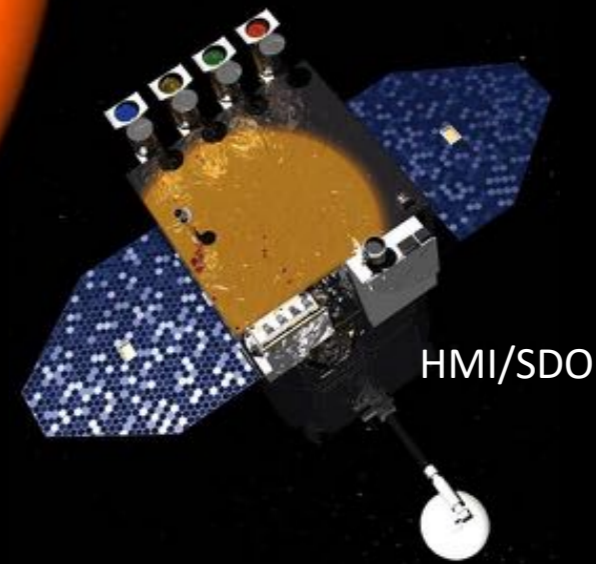
# The Sun

( 9/7/2016)

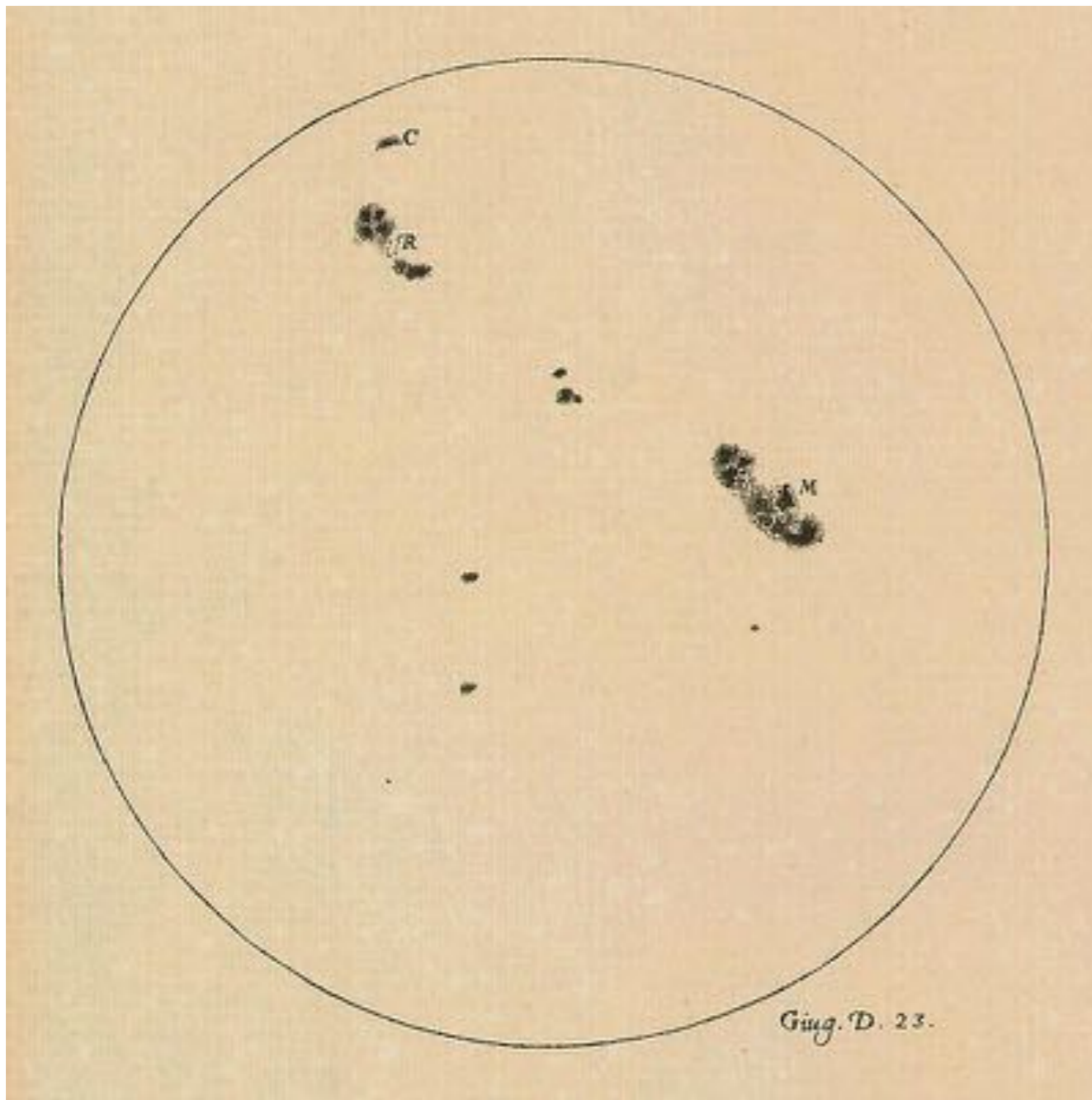


sunspots

visible light  
617 nm



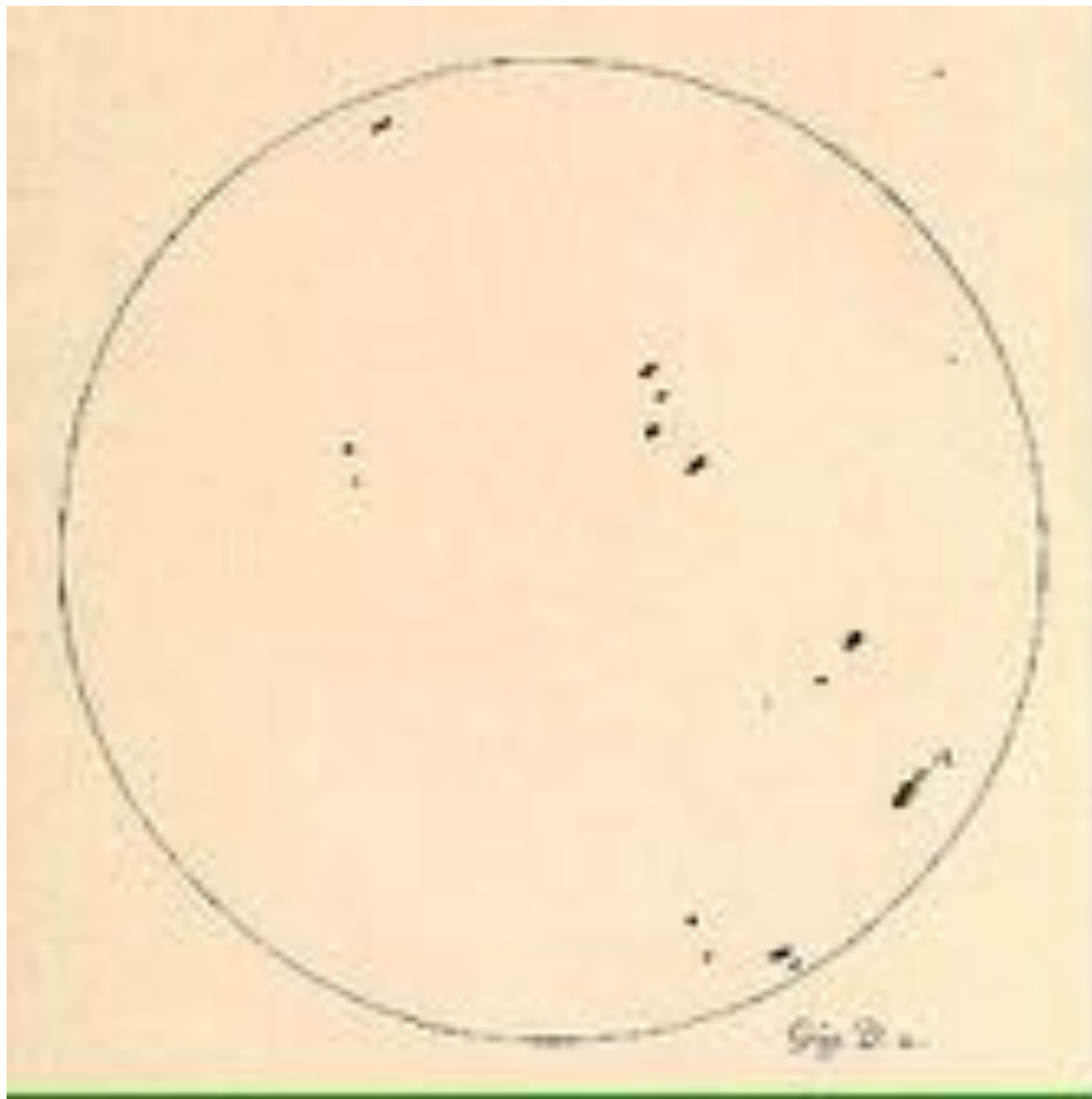
HMI/SDO



Detailed sunspot records  
from 1600s onward  
(Galileo Galilei, 1612)

Naked-eye observations  
from China since 23 BCE



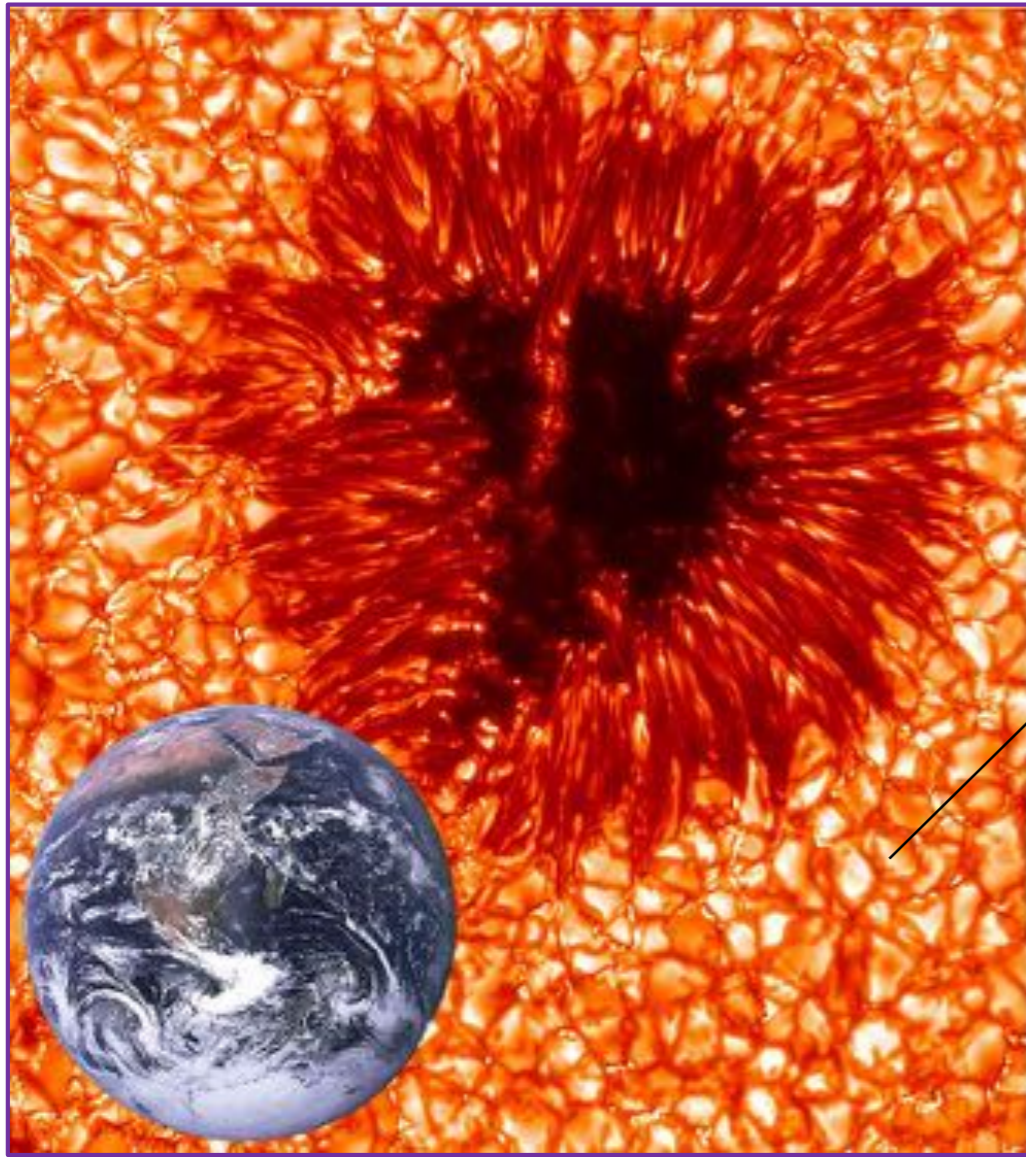


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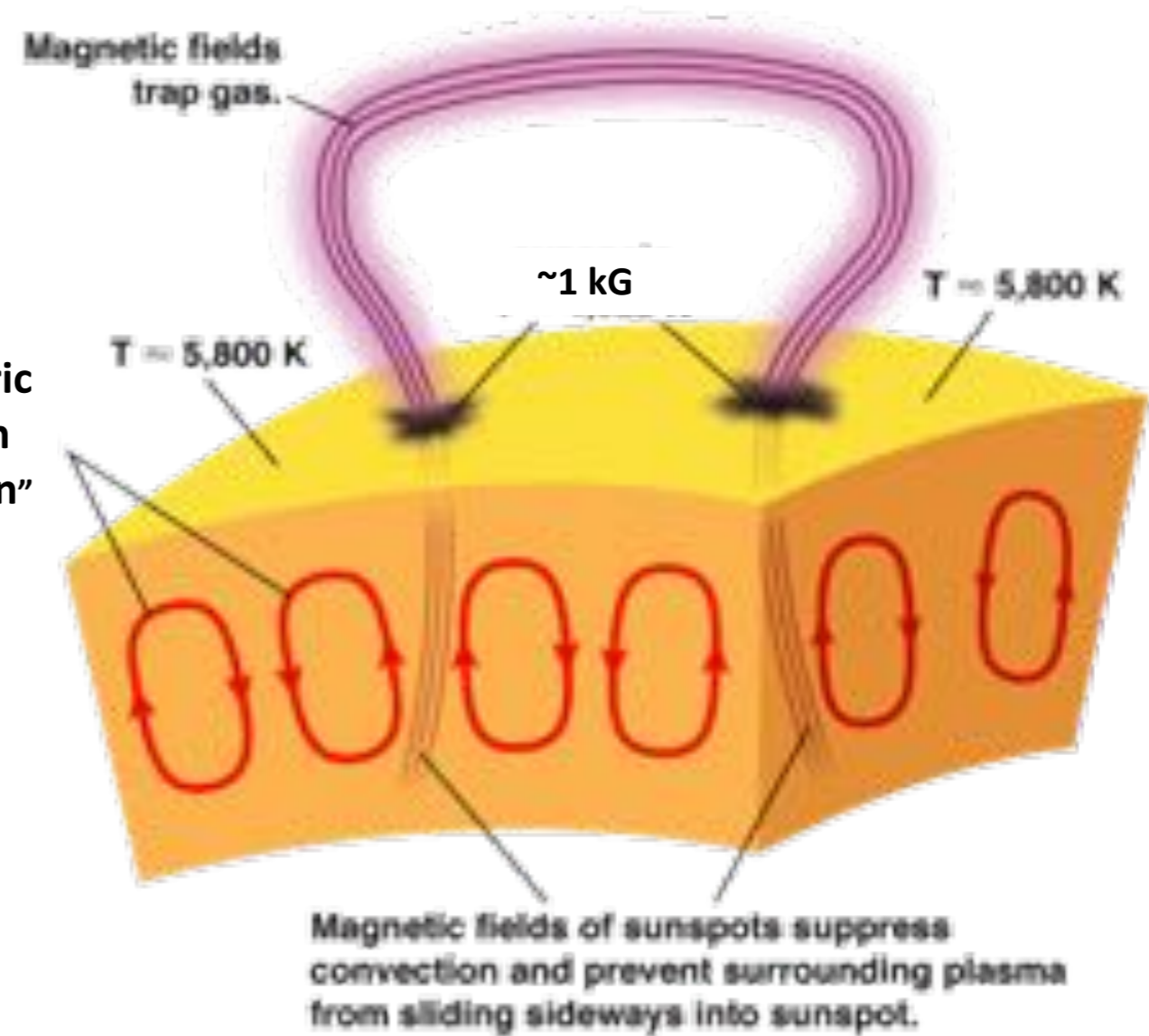


# Sunspots: A Closer Look

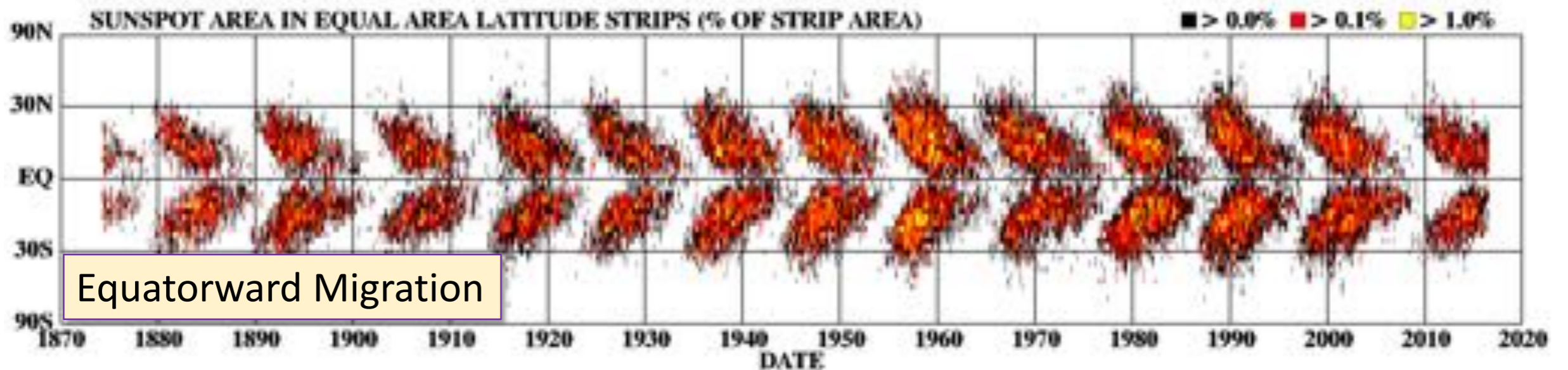
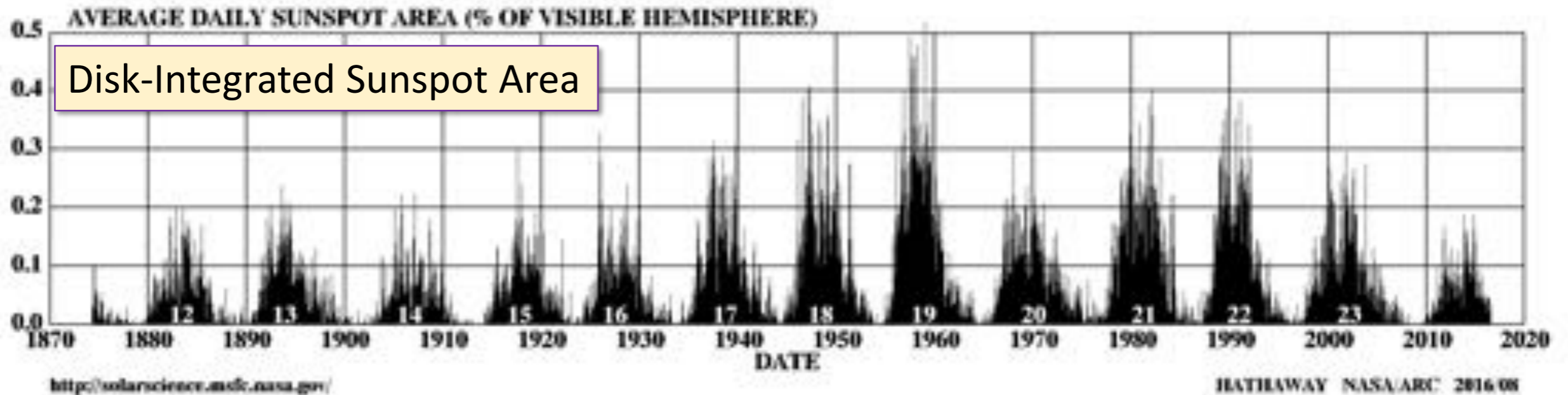


Swedish Solar Telescope (visible; 430 nm)

photospheric  
convection  
"granulation"

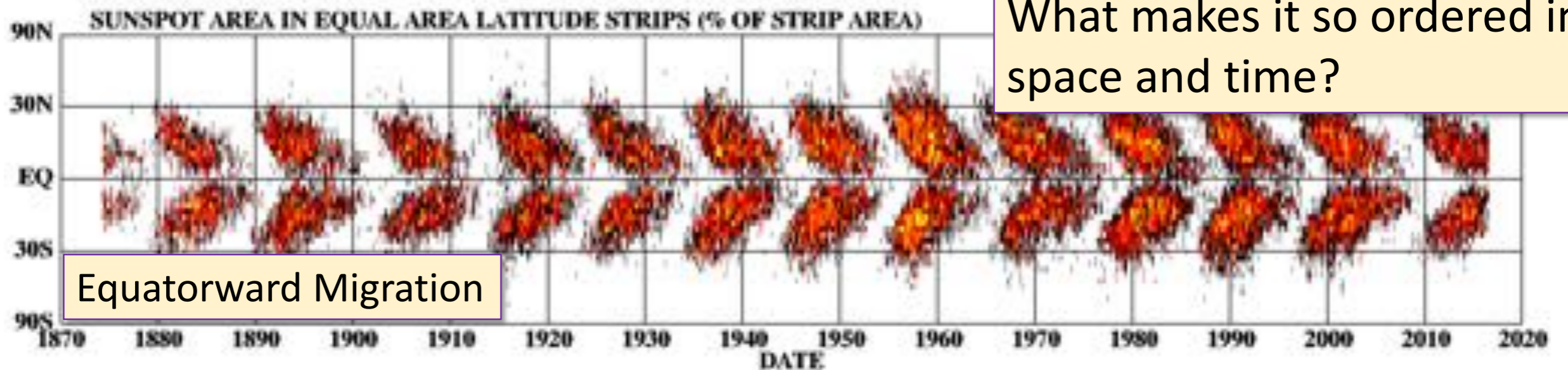
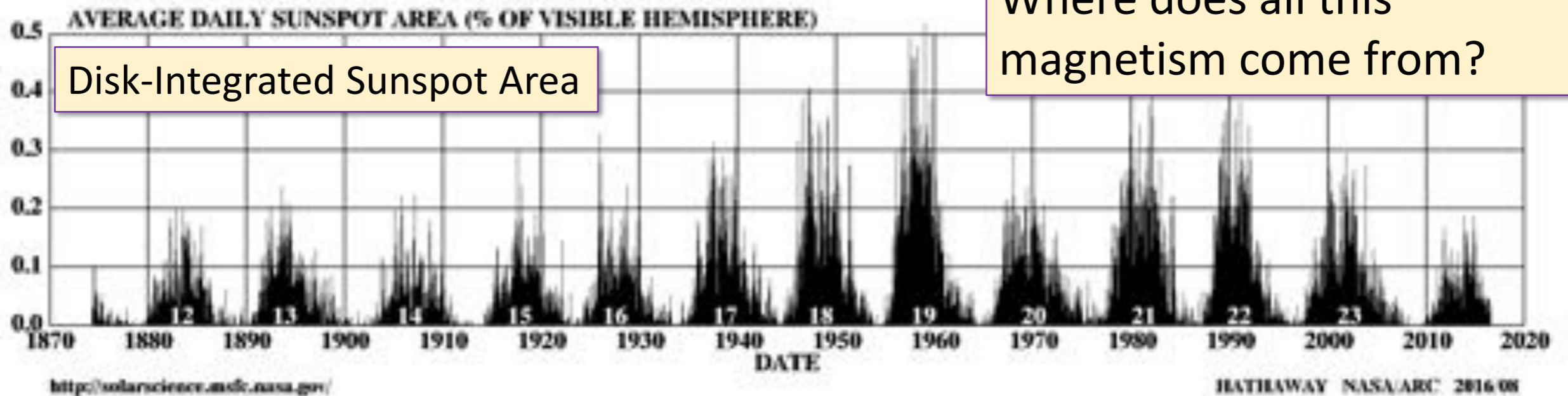


# The Sun's Magnetic Cycle



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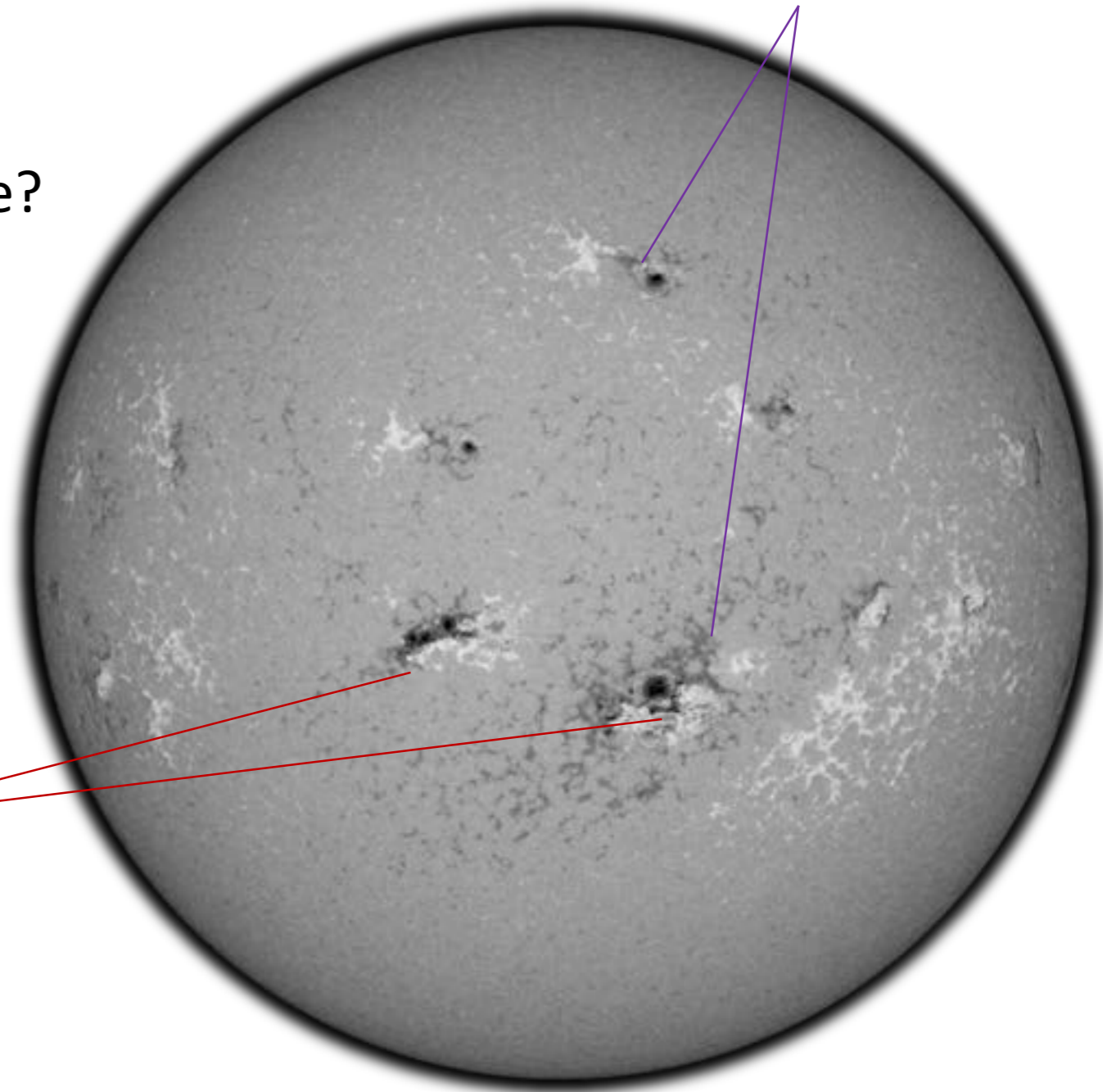
# Solar Dynamo: The Big Questions

Where does solar magnetism originate?  
Why is there a solar cycle?

Sunspot clusters ( active regions )

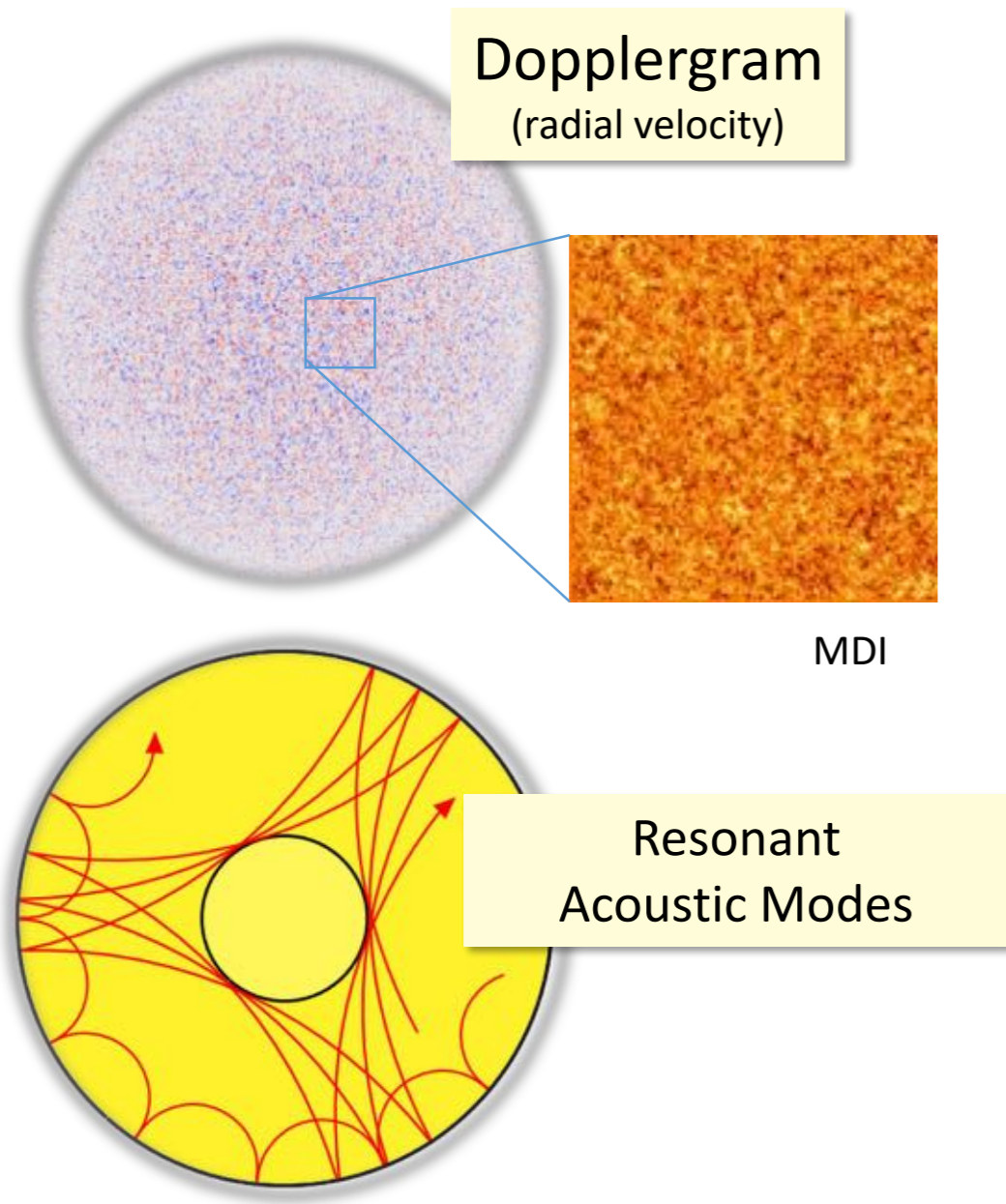
A deep origin for  
solar magnetism?

large-scale organization

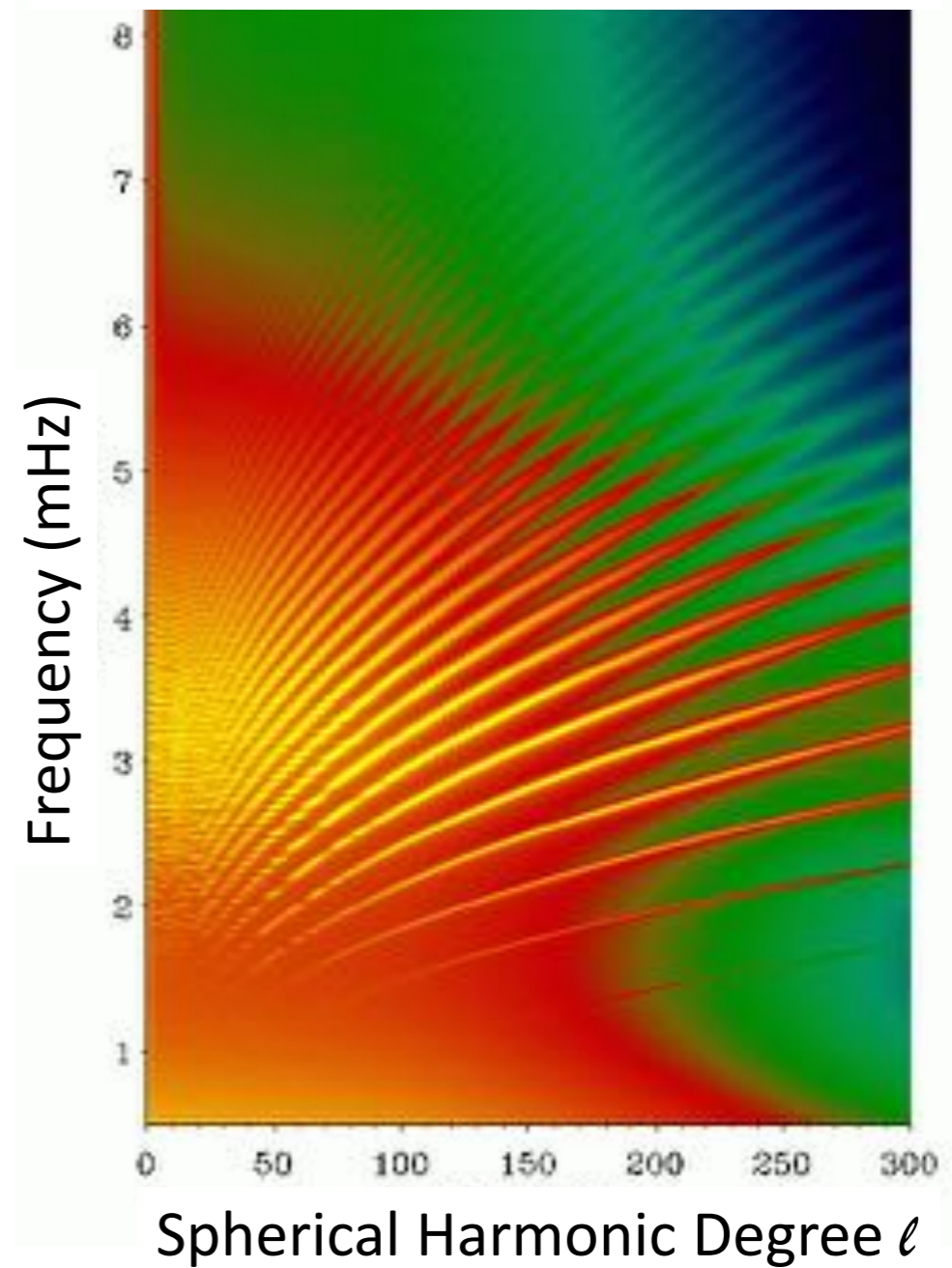


Line-of-sight magnetic Field (HMI)

# What Lies Beneath: Solar Helioseismology

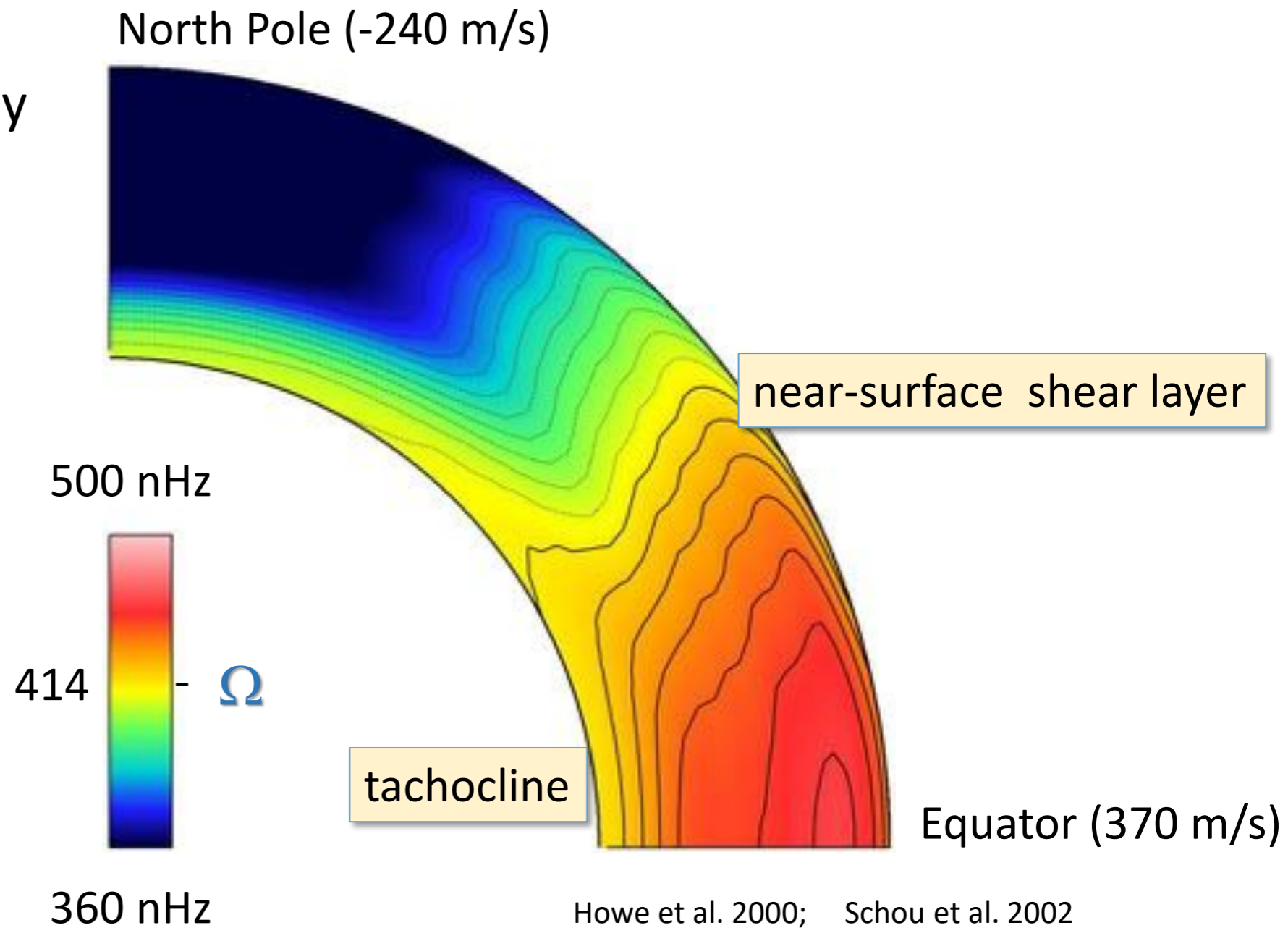


MDI Medium- $\ell$  Power Spectrum



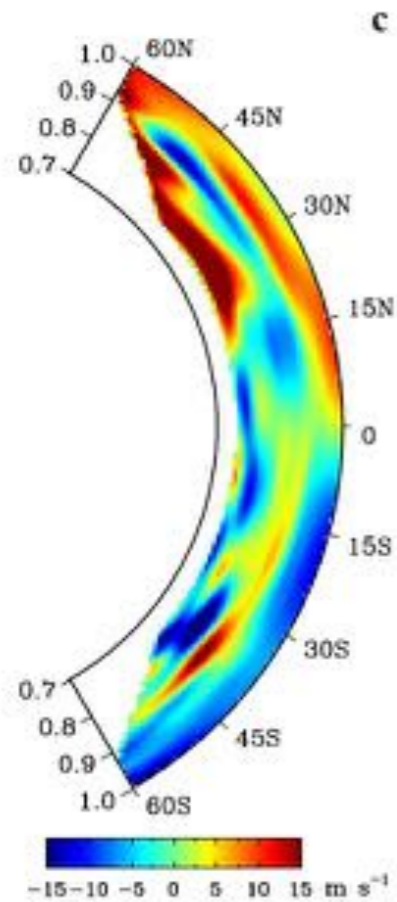
# Helioseismology Key Result: Differential Rotation

- Sun rotates differentially
- 24-day period equator
- 30-day period poles
- Latitudinal Shear
- Radial Shear



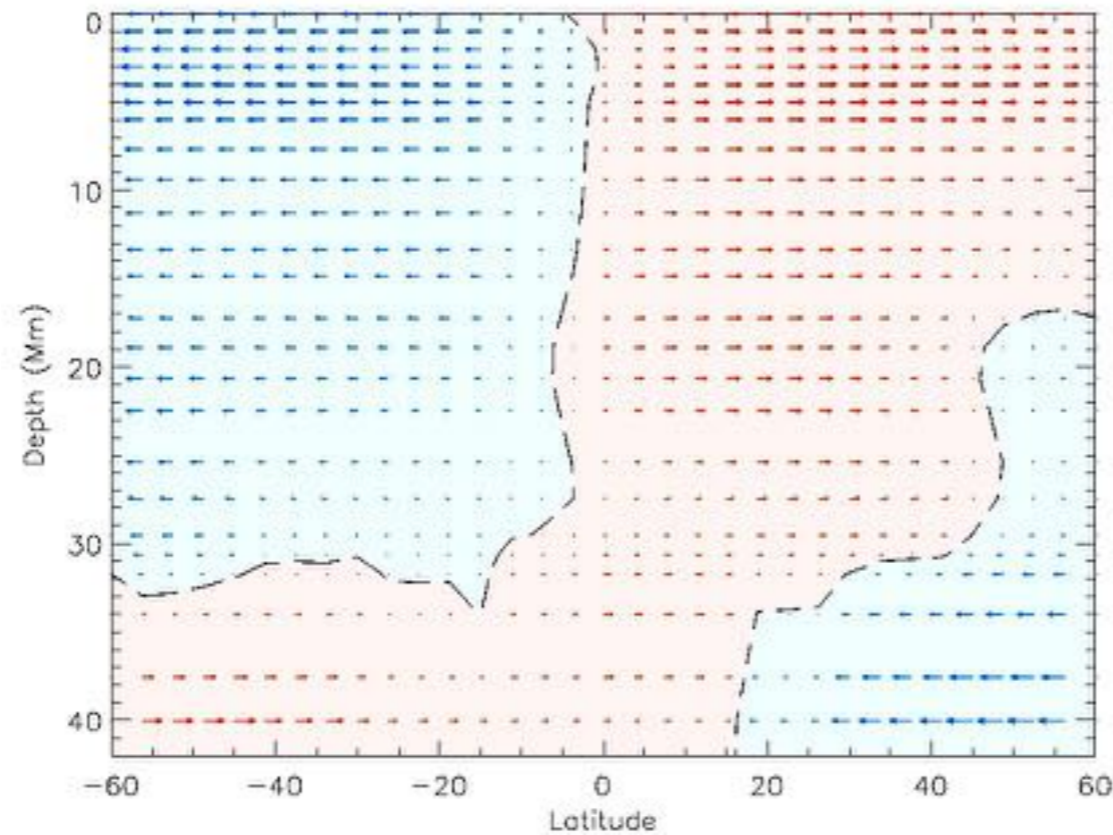
# Helioseismology Key Result: Meridional Circulation

## Time Distance

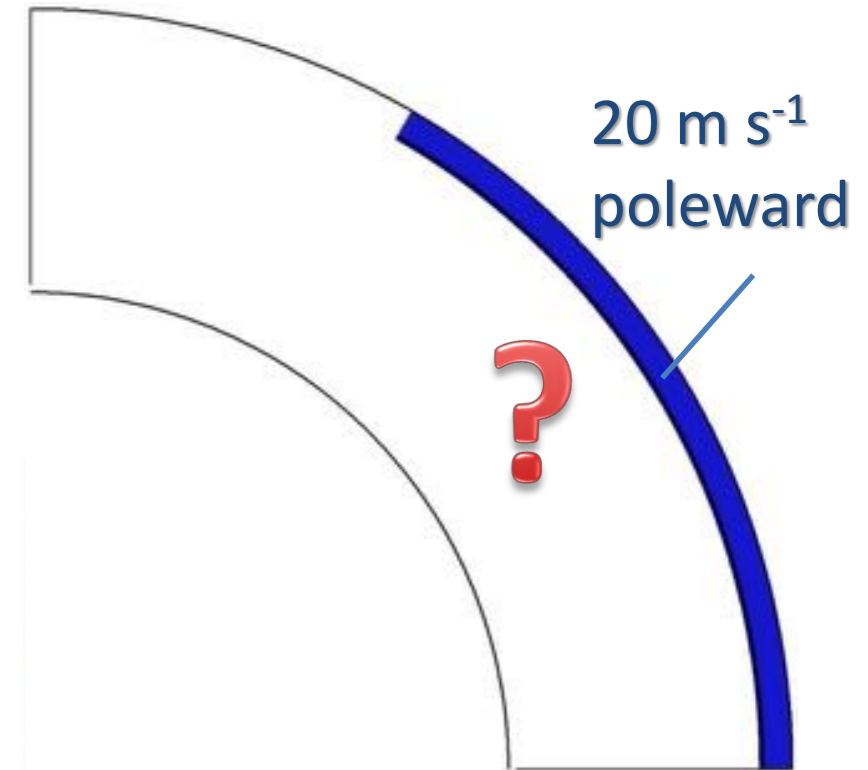


Zhao et al. 2012

## Ring Diagrams



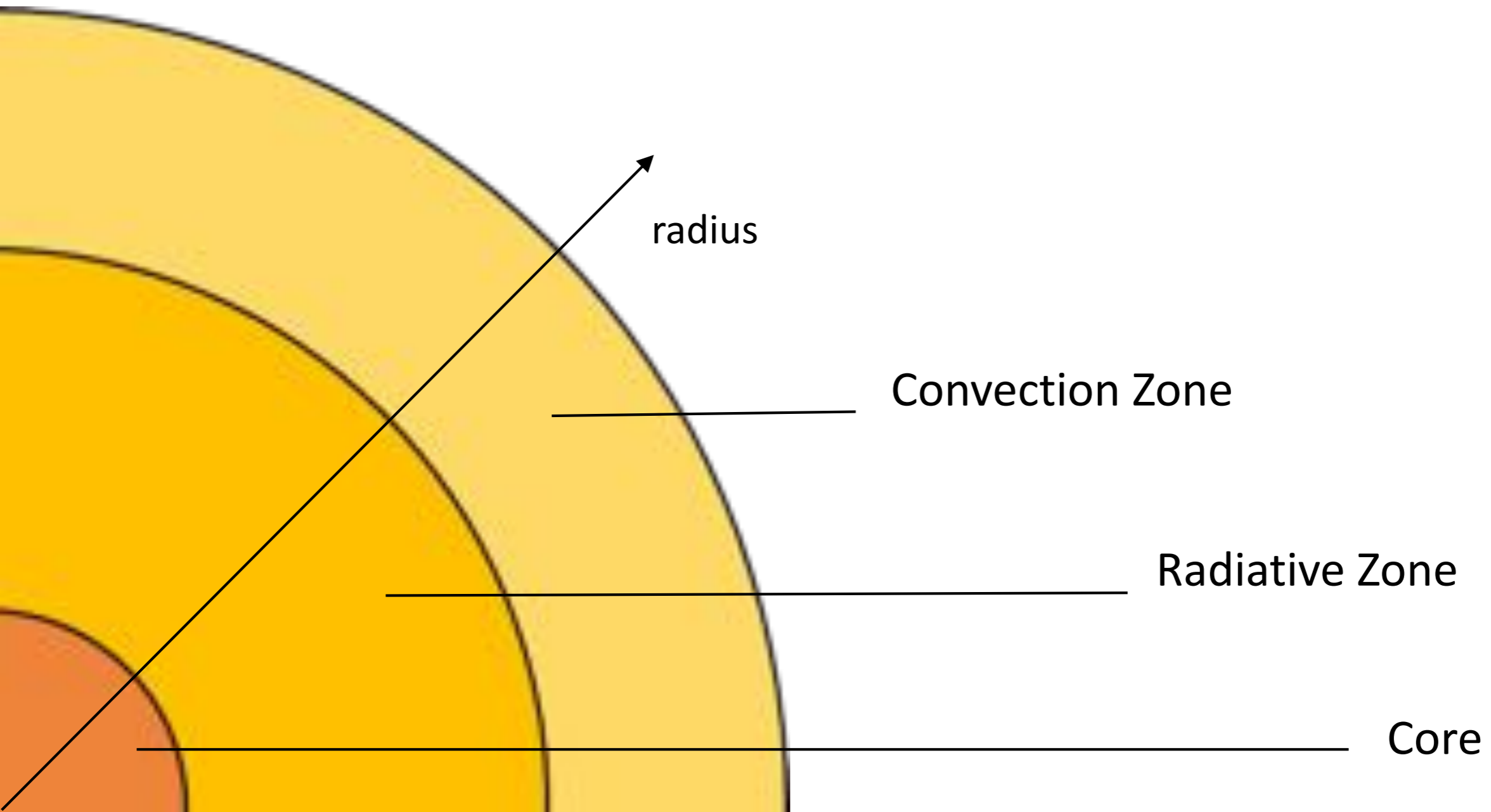
Greer et al. 2013



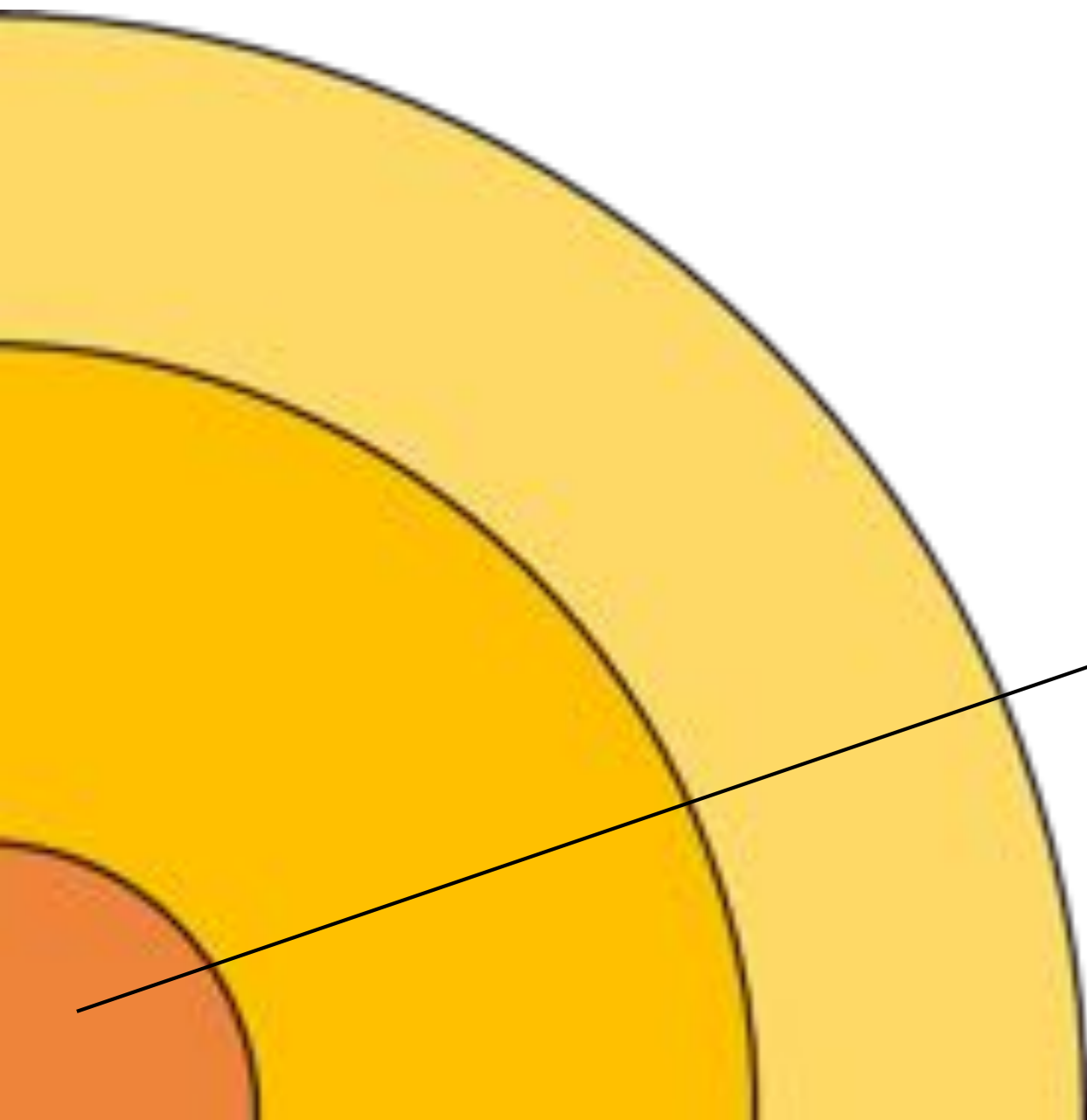
*Shallow or Deep reversal?*

*Latitudinal variation?*

# Helioseismology Key Result: Solar Structure



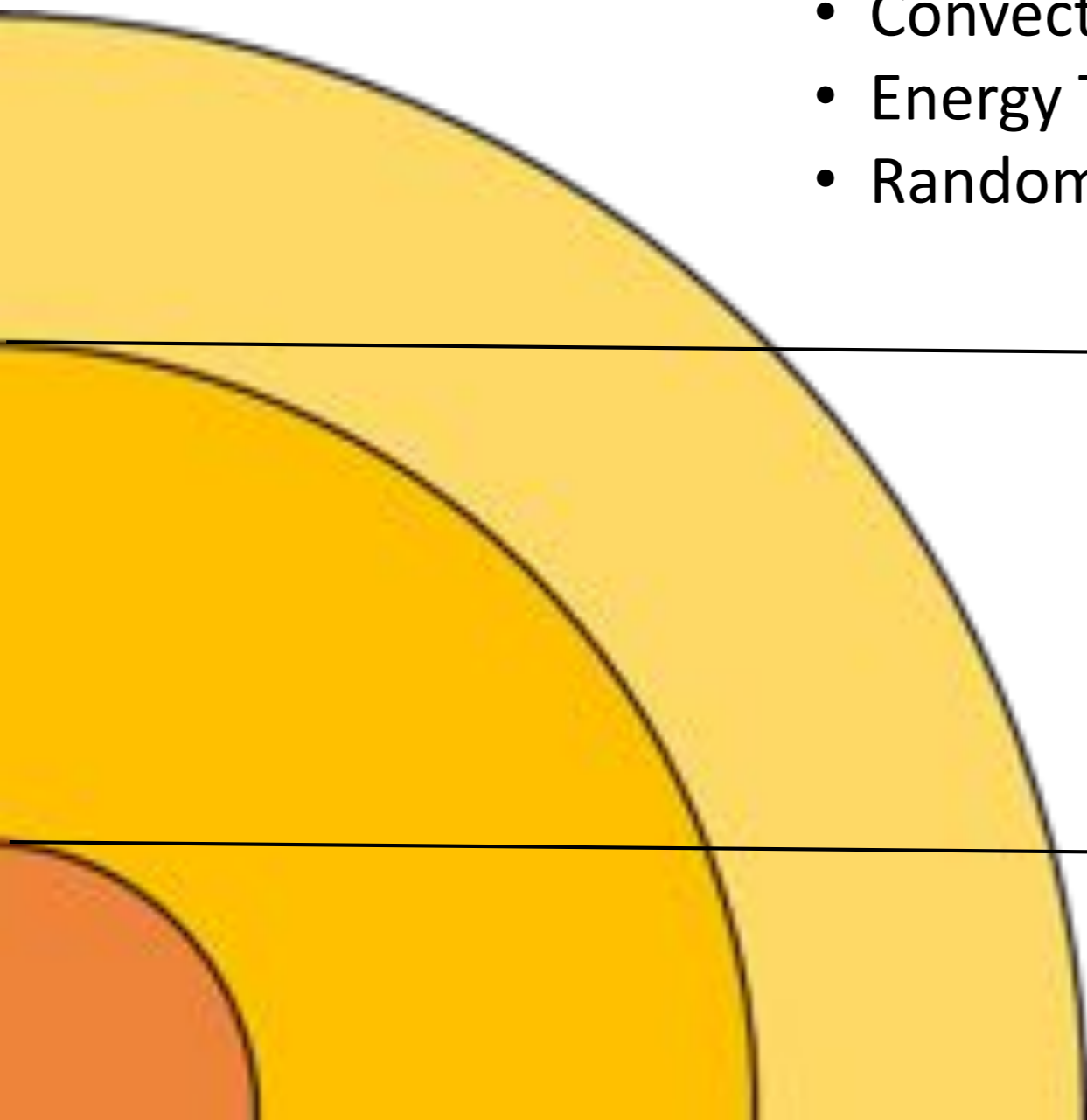
## Fusion Core



Central Temperature:	15.7 million K
Central Density:	$154 \text{ g cm}^{-3}$
Expanse:	$0 - 0.25 R_{\text{sun}}$

# Radiative Zone

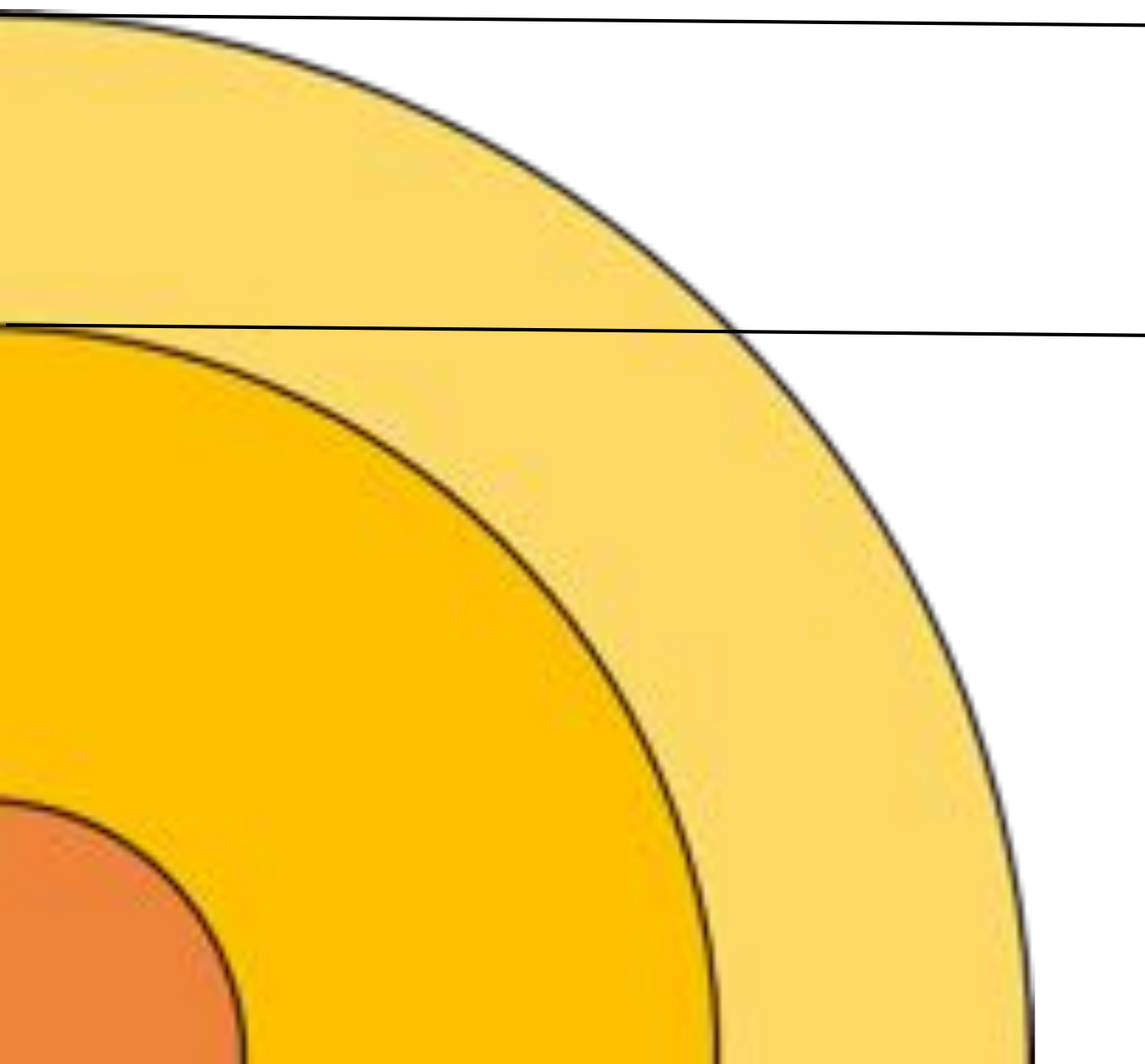
- Convectively **Stable**
- Energy Transport: photon scattering
- Random walk time: 100,000 years



Temperature:	2.3 million K
Density:	$0.2 \text{ g cm}^{-3}$
Radius:	$0.7 R_{\text{sun}}$

Temperature:	8 million K
Density:	$20 \text{ g cm}^{-3}$
Radius:	$0.25 R_{\text{sun}}$

## Convection Zone



Temperature: 5800K  
Density:  $2 \times 10^{-7} \text{ g cm}^{-3}$   
Radius:  $1 R_{\text{sun}}$

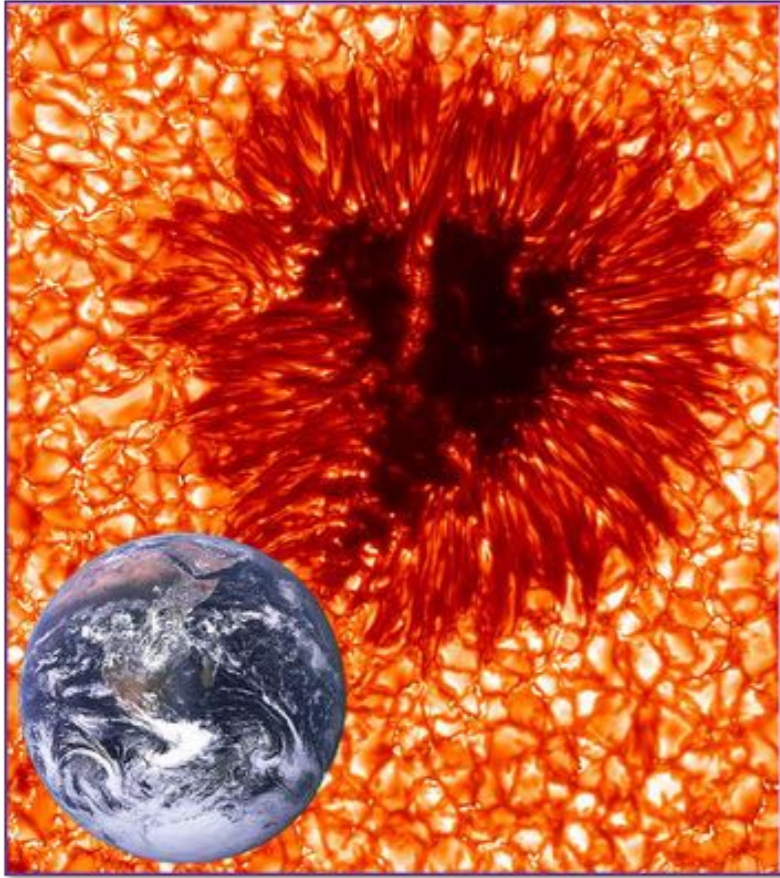
Temperature: 2.3 million K  
Density:  $0.2 \text{ g cm}^{-3}$   
Radius:  $0.7 R_{\text{sun}}$

- Convectively **unstable**
- Convective timescale: months, years?

*region of extreme contrasts...*

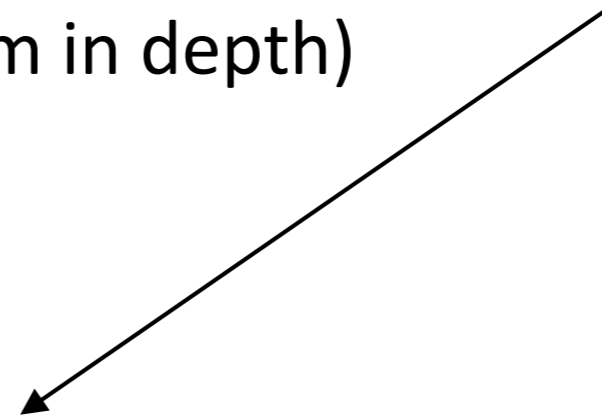
*... ionized plasma!*





### Note:

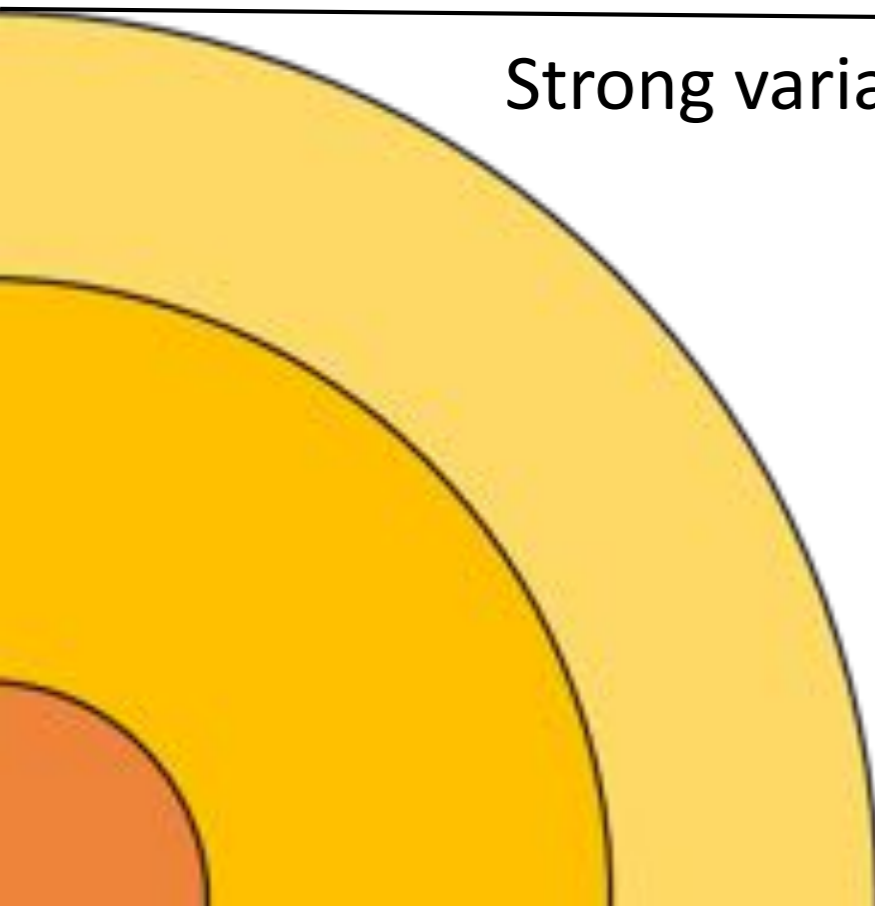
The convection that we can see occurs in a region thinner than the width of this line (about 1,000 km in depth)



Strong variation with depth

Temperature:	5,800K
Density:	$2 \times 10^{-7} \text{ g cm}^{-3}$
Radius:	$1 R_{\text{sun}}$

Temperature:	14,400K
Density:	$2 \times 10^{-6} \text{ g cm}^{-3}$
Radius:	$0.9985 R_{\text{sun}}$

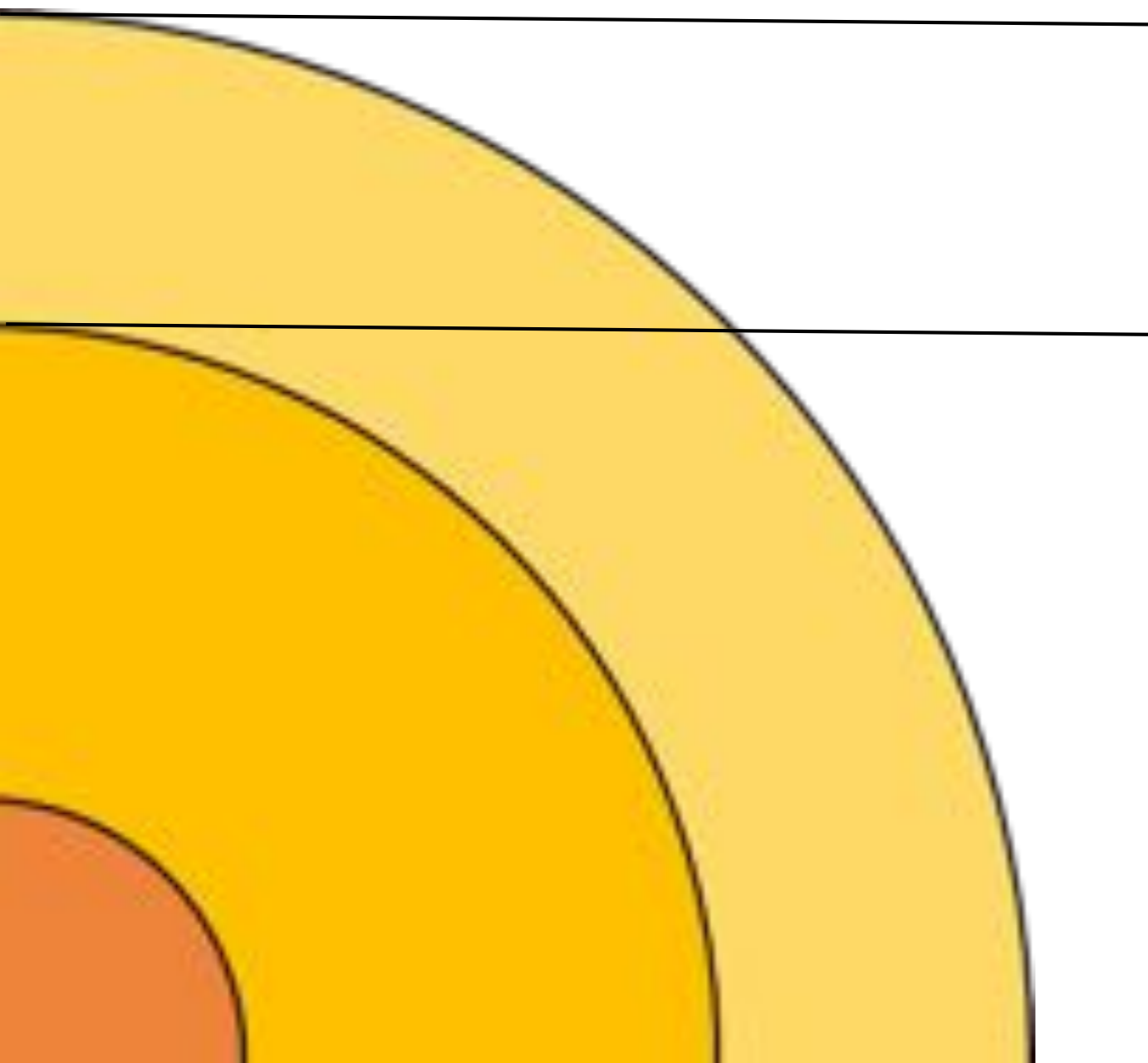


## Convection Zone Bulk

Temperature: 14,400K  
Density:  $2 \times 10^{-6} \text{ g cm}^{-3}$

Temperature: 2.3 million K  
Density:  $0.2 \text{ g cm}^{-3}$

- 11 density scaleheights
- 17 pressure scaleheights
- Reynolds Number  $\approx 10^{12} - 10^{14}$
- Rayleigh Number  $\approx 10^{22} - 10^{24}$
- Magnetic Prandtl Number  $\approx 0.01$
- Prandtl Number  $\approx 10^{-7}$
- Ekman Number  $\approx 10^{-15}$



# Question

***Where does the energy in the solar magnetic field come from?***



The **Solar Dynamo** generates magnetic fields from flows

**convection**

**differential rotation**

**meridional circulation**

magnetic energy ultimately comes from the Sun's own mass

**Fusion**

mass  $\Rightarrow$  radiation & thermal energy

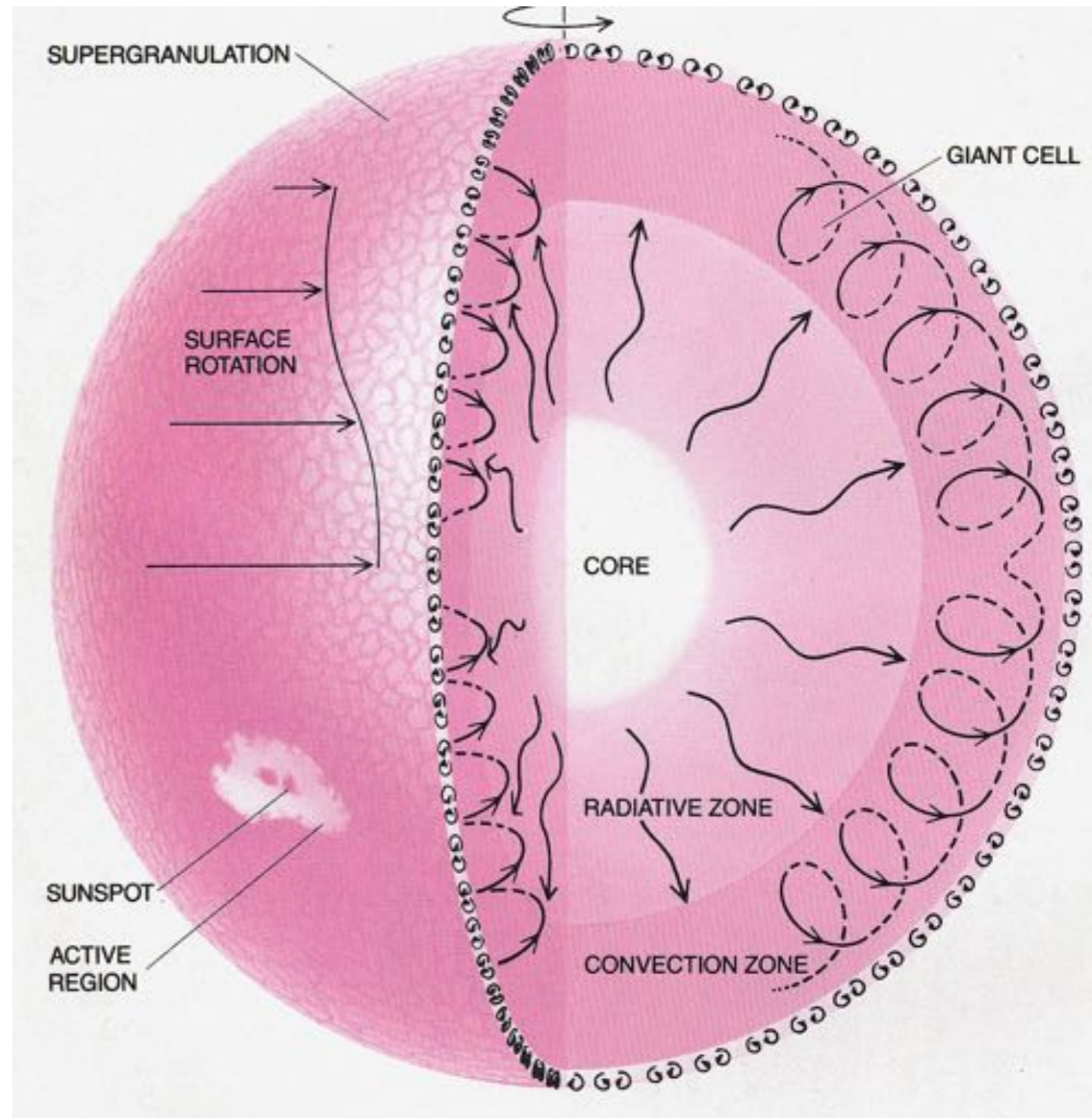
**Convection**

thermal energy  $\Rightarrow$  kinetic energy

**Dynamo**

kinetic energy  $\Rightarrow$  magnetic energy

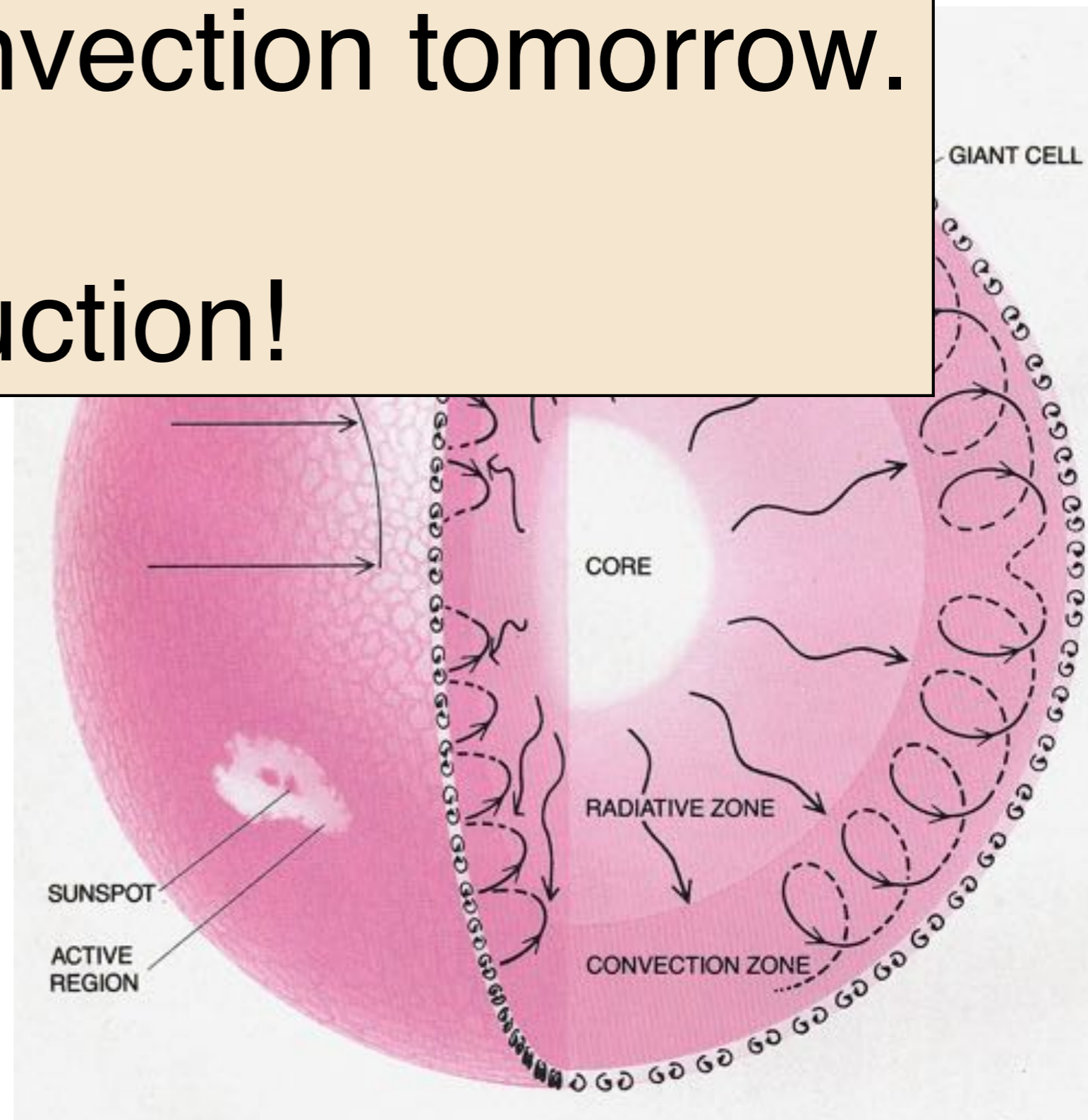
$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$



$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$

More on convection tomorrow.

Today: Induction!



## MHD Magnetic Induction equation

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B} - \eta \nabla \times \mathbf{B})$$

*Comes from Maxwell's equations (Faraday's Law and Ampere's Law)*

$$\frac{1}{c} \frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}$$

$$\nabla \times \mathbf{B} = \frac{4\pi}{c} \mathbf{J}$$

*And Ohm's Law*

*Magnetic diffusivity*

$$\tilde{\mathbf{J}} = \sigma \tilde{\mathbf{E}}$$

*electrical conductivity*

$$\eta = \frac{c^2}{4\pi\sigma}$$

## Creation and destruction of magnetic fields

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B} - \eta \nabla \times \mathbf{B})$$

*Source of Magnetic Energy*

*Sink of Magnetic Energy*

*How would you demonstrate this?*

*(Hint: have a sheet handy with lots of vector identities!)*

$$E_m = \frac{B^2}{8\pi}$$

# Creation and destruction of magnetic fields

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B} - \eta \nabla \times \mathbf{B})$$

*Dot with B...*

$$E_m = \frac{B^2}{8\pi}$$

*Source of Magnetic Energy*

*Sink of Magnetic Energy*

$$\frac{\partial E_m}{\partial t} = -\nabla \cdot \mathbf{F}_P - \frac{\mathbf{v}}{c} \cdot (\mathbf{J} \times \mathbf{B}) - \Phi_o$$

*Poynting Flux*

*Ohmic Heating*

$$\mathbf{F}_P = \mathbf{E} \times \mathbf{B} = \left[ \frac{\eta}{c} \mathbf{J} - \frac{1}{4\pi} (\mathbf{v} \times \mathbf{B}) \right] \times \mathbf{B}$$

$$\Phi_o = \frac{4\pi\eta}{c^2} J^2$$



# Creation and destruction of magnetic fields

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B} - \eta \nabla \times \mathbf{B})$$

*Source of Magnetic Energy*  
 $\sim U B / D$

*Sink of Magnetic Energy*  
 $\sim \eta B / D^2$

$$R_m = \frac{UD}{\eta}$$

*If  $R_m \gg 1$  the source term is much bigger than the sink term*

ratio of source and sink terms

**....Or is it???**

## Creation and destruction of magnetic fields

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B} - \eta \nabla \times \mathbf{B})$$

*Source of Magnetic  
Energy  
 $\sim U B / D$*

*Sink of Magnetic  
Energy  
 $\sim \eta B / \delta^2$*

*$\delta$  can get so small that the two terms are comparable*

*It's not obvious which term will "win" - it depends on the subtleties of the flow,  
including geometry & boundary conditions*

# Creation and destruction of magnetic fields

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B} - \eta \nabla \times \mathbf{B})$$

*Source of Magnetic  
Energy  
 $\sim U B / D$*

*Sink of Magnetic  
Energy  
 $\sim \eta B / \delta^2$*

## **What is a Dynamo? (A corollary)**

*A dynamo must sustain the magnetic energy (through the conversion of kinetic energy) against **Ohmic dissipation***

*How exactly does this work? It depends on the nature of the flow...*

# Large Scale Dynamos: The Mean Induction Equation

Go back to our basic induction equation

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$

Now just average over longitude and rearrange a bit  
(other averages are possible but we'll stick to this for simplicity)

The equation for the mean field comes out to be

$$\frac{\partial \bar{\mathbf{B}}}{\partial t} = \lambda \bar{\mathbf{B}}_p \cdot \nabla \Omega \hat{\phi} + \nabla \times (\bar{\mathbf{v}}_m \times \bar{\mathbf{B}}) + \eta \nabla^2 \bar{\mathbf{B}} + \nabla \times \boldsymbol{\varepsilon}$$

Ω-effect  
(large-scale  
shear)      Meridional  
circulation  
(transport)      Diffusion  
(molecular)      Fluctuating  
emf  
(small-scale  
shear)

$$\lambda = r \sin \theta$$

**Note:**  
The  $B$  field in the Sun is clearly not axisymmetric. Still, the solar cycle does have an axisymmetric component so that's a good place to start

No assumptions made up to this point beyond the basic MHD induction equation

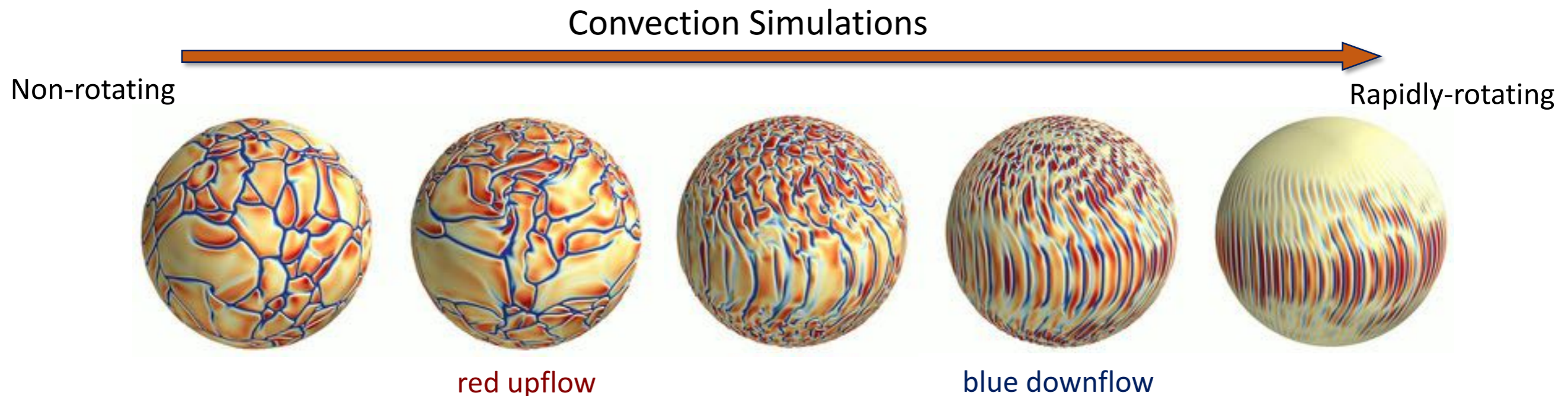
Straightforward to show that if  $E=0$ , the dynamo dies (Cowling's theorem)

# The MHD Induction Equation: Alternate View

$$\frac{\partial \mathbf{B}}{\partial t} = \underbrace{-\mathbf{B} \nabla \cdot \mathbf{v}}_{\text{compression}} + \underbrace{\mathbf{B} \cdot \nabla \mathbf{v}}_{\text{shear production}} - \underbrace{\mathbf{v} \cdot \nabla \mathbf{B}}_{\text{advection}} - \underbrace{\nabla \times (\eta \nabla \times \mathbf{B})}_{\text{diffusion}}$$

Large-Scale Shear (differential rotation)  
 Small-Scale Shear (helical rolls)

Rotation



*Rotating convection naturally generates both small-scale and large-scale shear!*

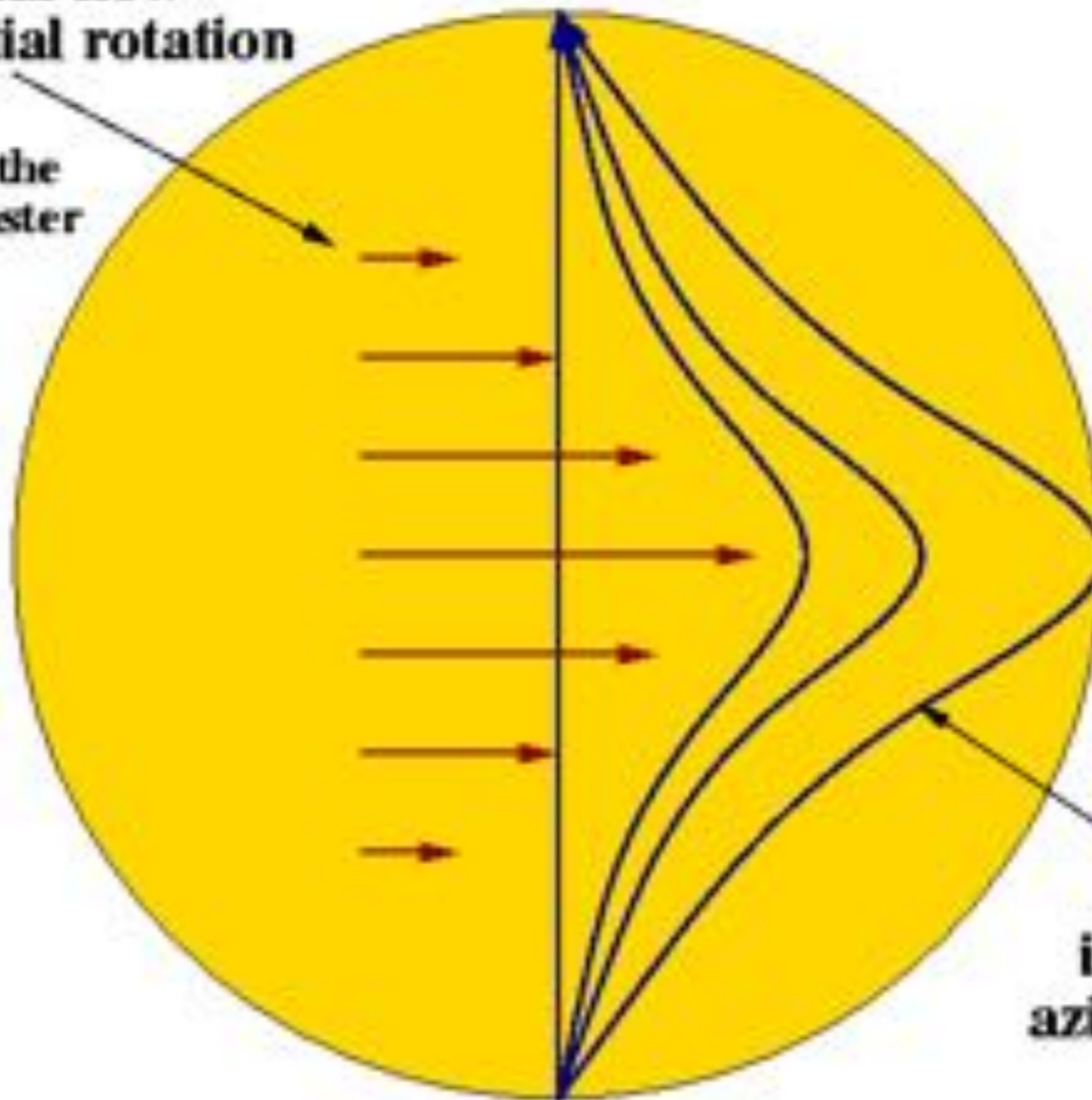
# The $\Omega$ -effect (large-scale shear)

Converts poloidal to toroidal field and  
amplifies it

...by tapping the kinetic energy of the  
differential rotation

**Azimuthal flow  
of differential rotation**

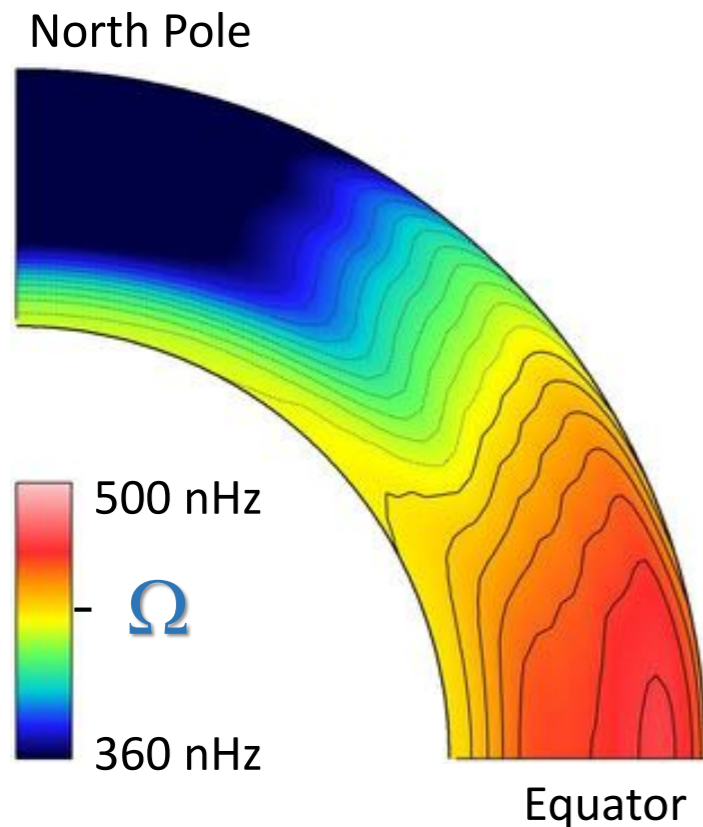
The longer the  
arrow the faster  
the flow



$$\nabla v_{\phi}$$

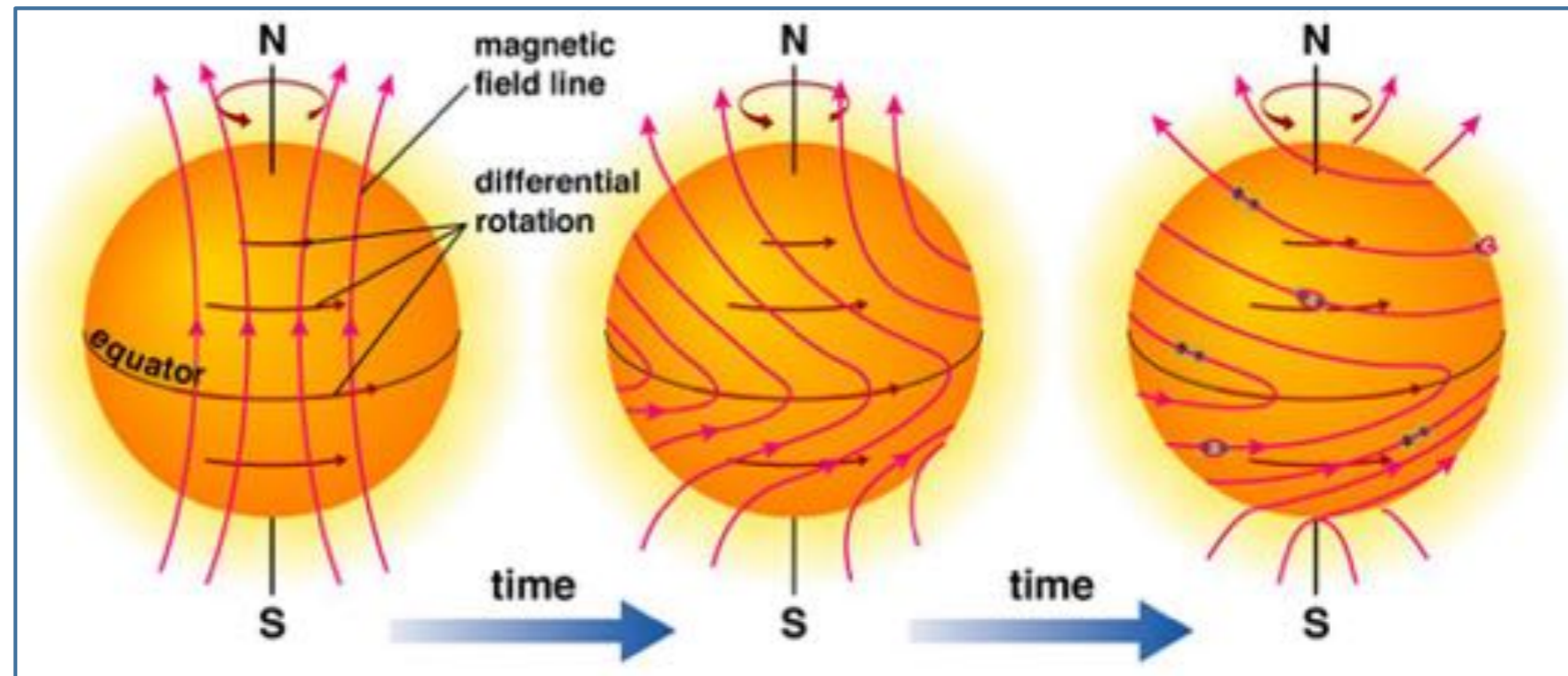
**Meridional  
magnetic field  
is transformed into  
azimuthal magnetic field**

# The $\Omega$ -effect (large-scale shear via helical convection)



Howe et al. 2000; Schou et al. 2002

## "Omega-effect"



Bennett, et al. 2003

- 24-day period equator
- 30-day period poles

Mean shear:

- Latitudinal (Omega effect)
- Radial (Tachocline; Interface Dynamo)

*Converts poloidal to toroidal field and amplifies it*

*...by tapping the kinetic energy of the differential rotation*

# The turbulent $\alpha$ -effect

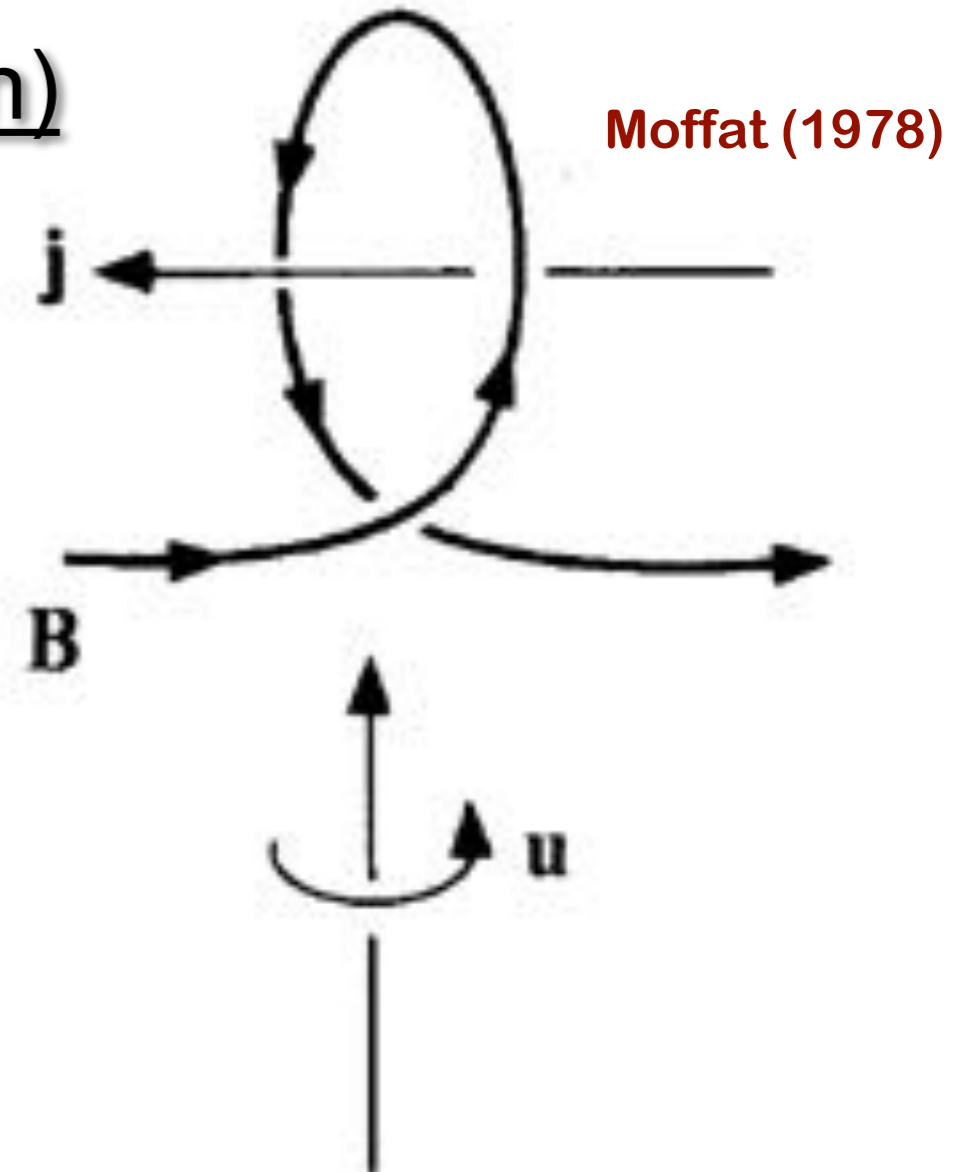
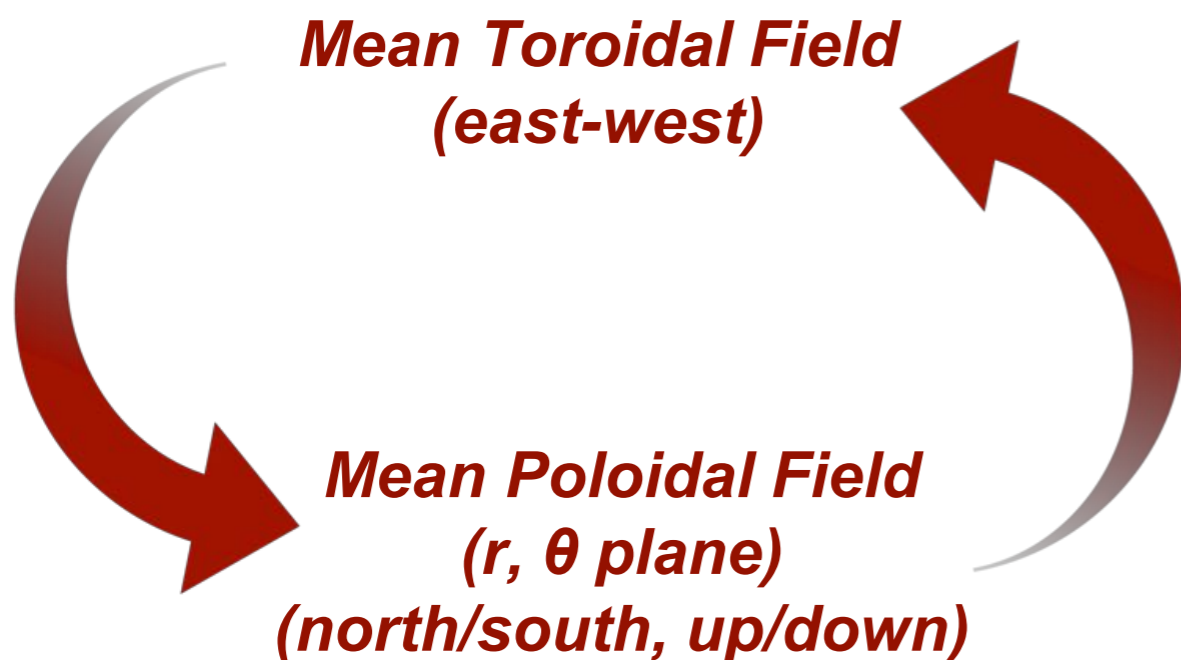
(small-scale shear via helical convection)

*Helical motions (lift, twist) can induce an emf that is parallel to the mean field*

$$\mathcal{E} = \overline{\mathbf{v}' \times \mathbf{B}'} = \alpha \overline{\mathbf{B}}$$

*This creates mean poloidal ( $r, \theta$ ) field from toroidal ( $\phi$ ) field*

*which closes the Dynamo Loop*



*Linked to kinetic, magnetic helicity*

*Linked to large-scale dynamo action*

*Illustrates the 3D nature of dynamos*

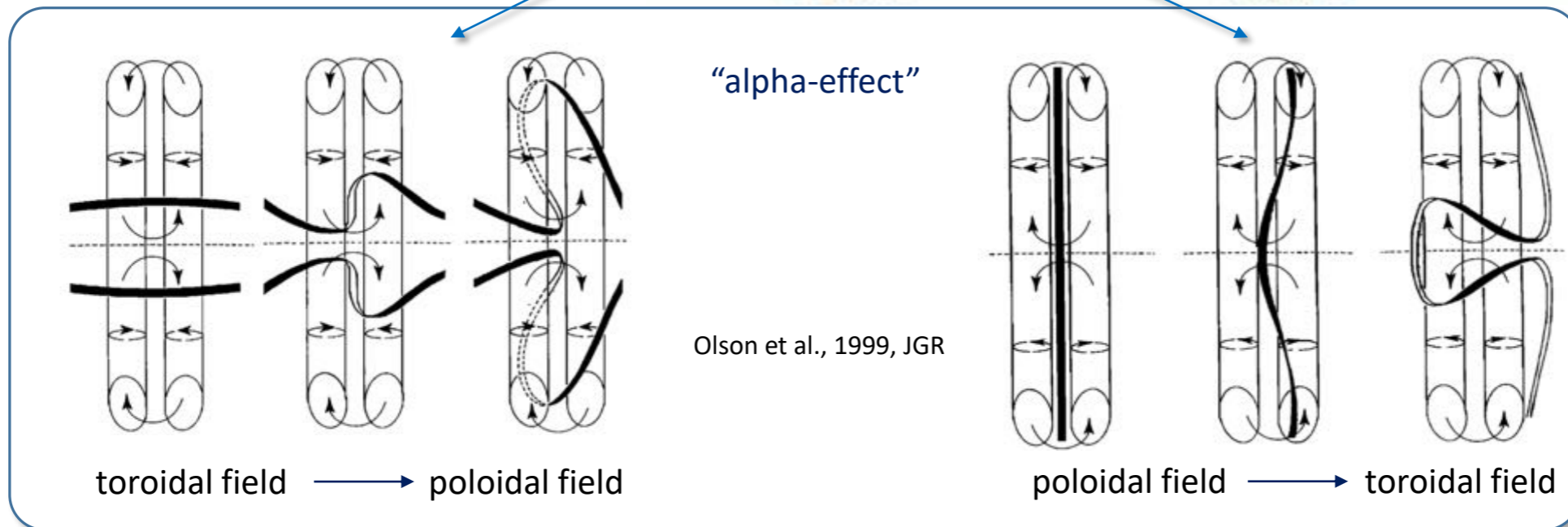
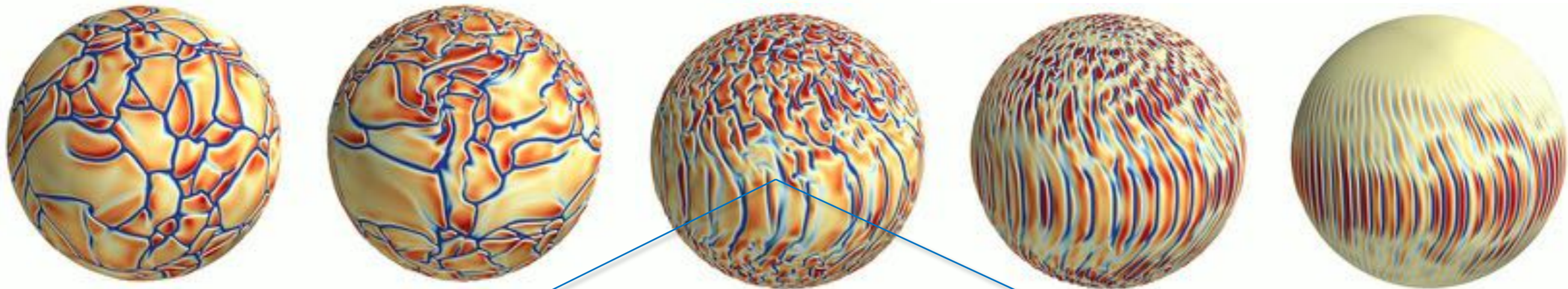


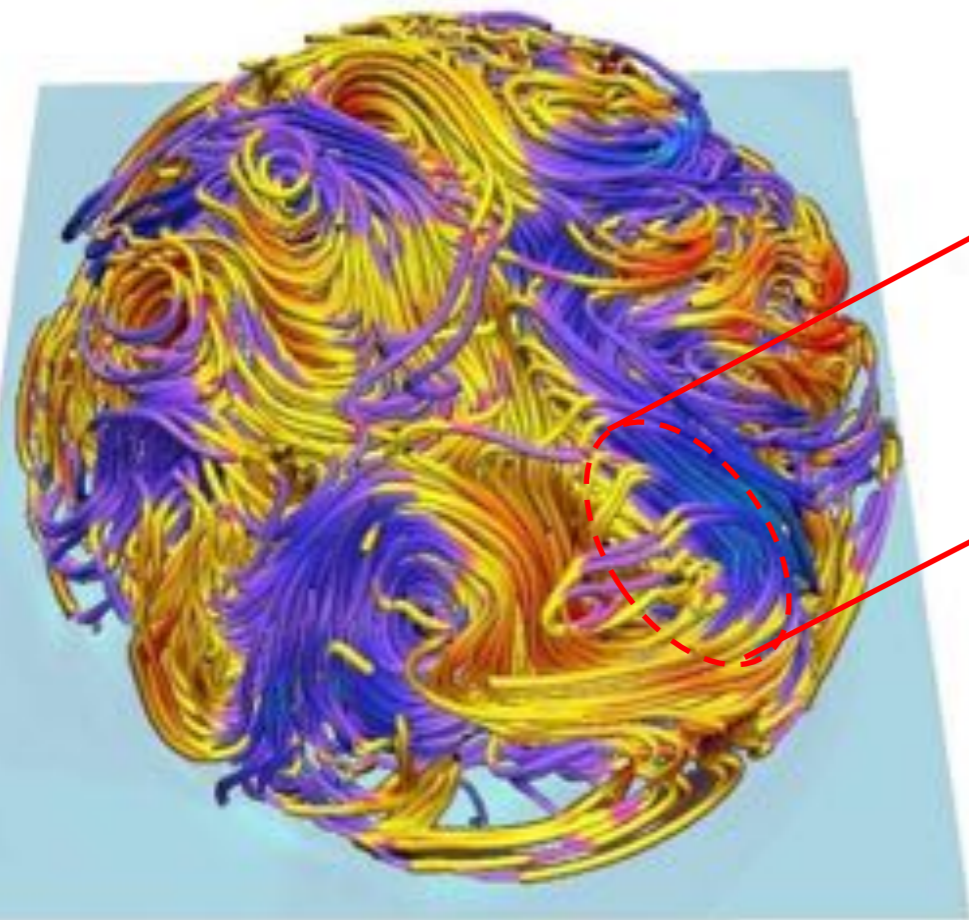
# Rotation Yields Helical Convection



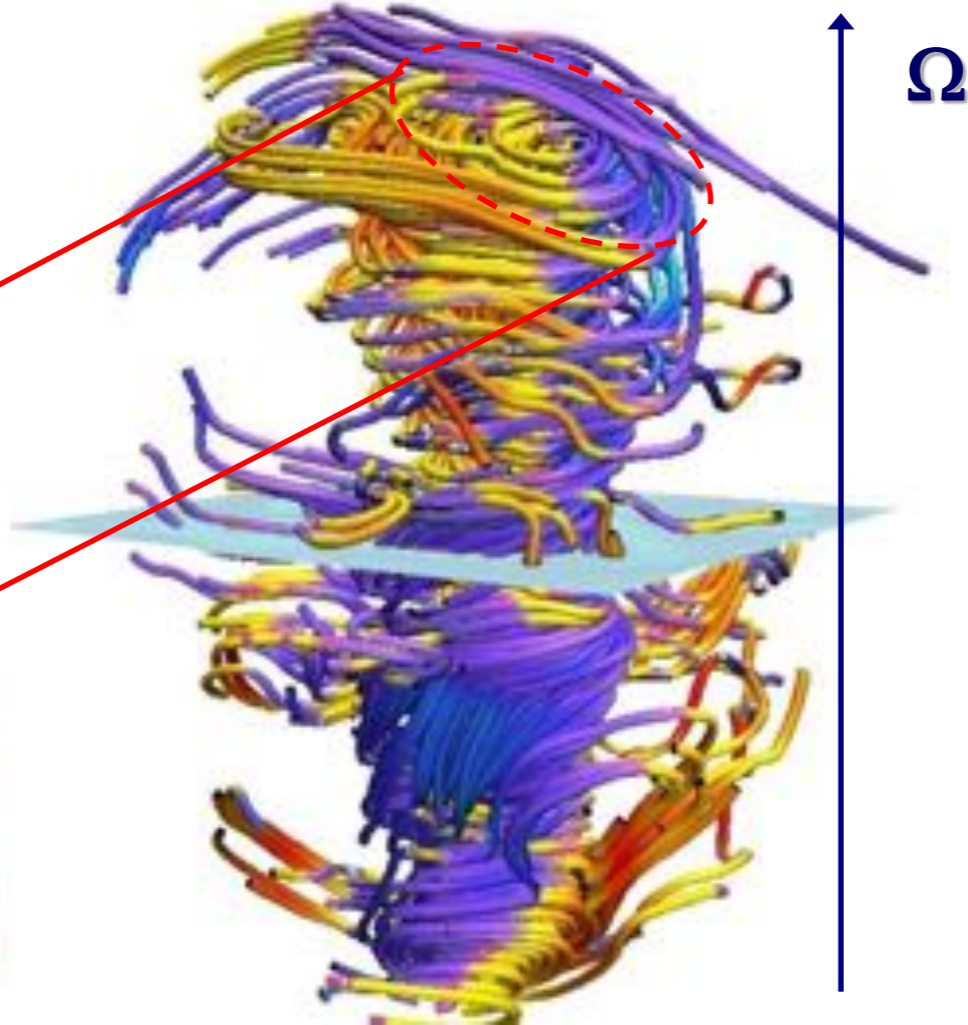
Non-rotating  
or  
Fast Convection

Rapidly-rotating  
or  
Slow Convection





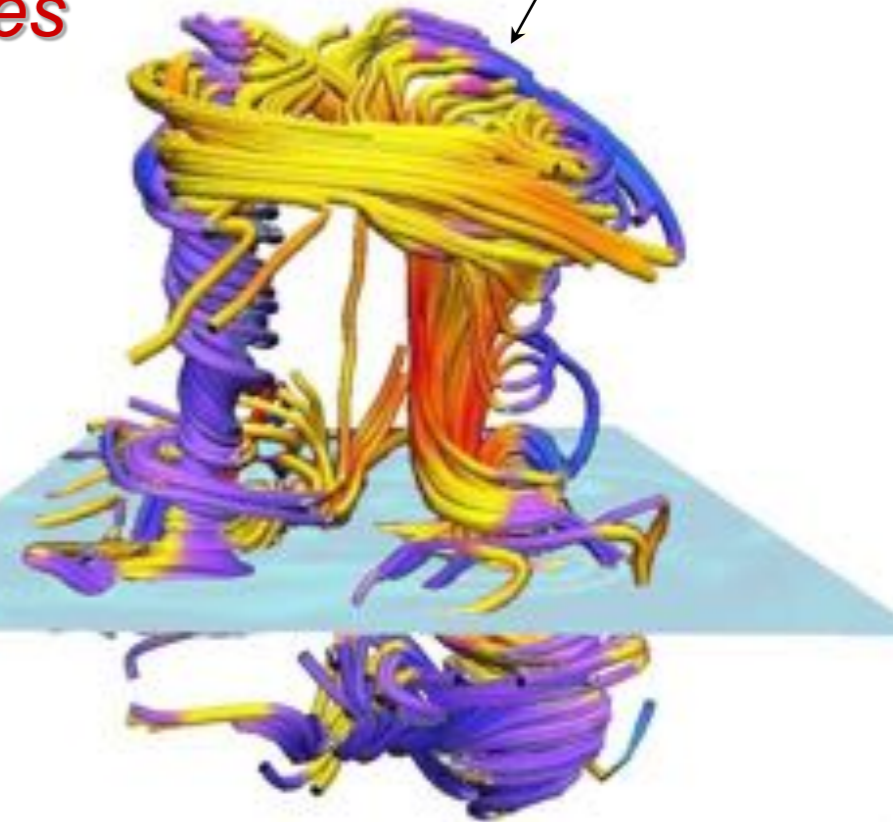
Northern Hemisphere



Helical  
Convection  
(Deep Shells)



*Streamlines*



*Tilted orbits*

Fast Convection / slow rotation

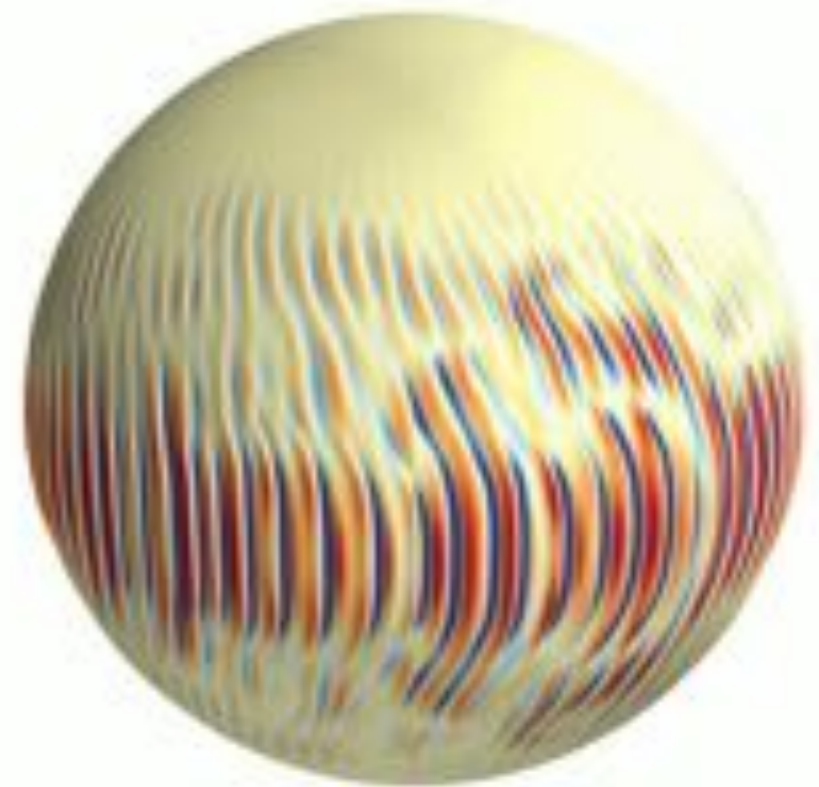
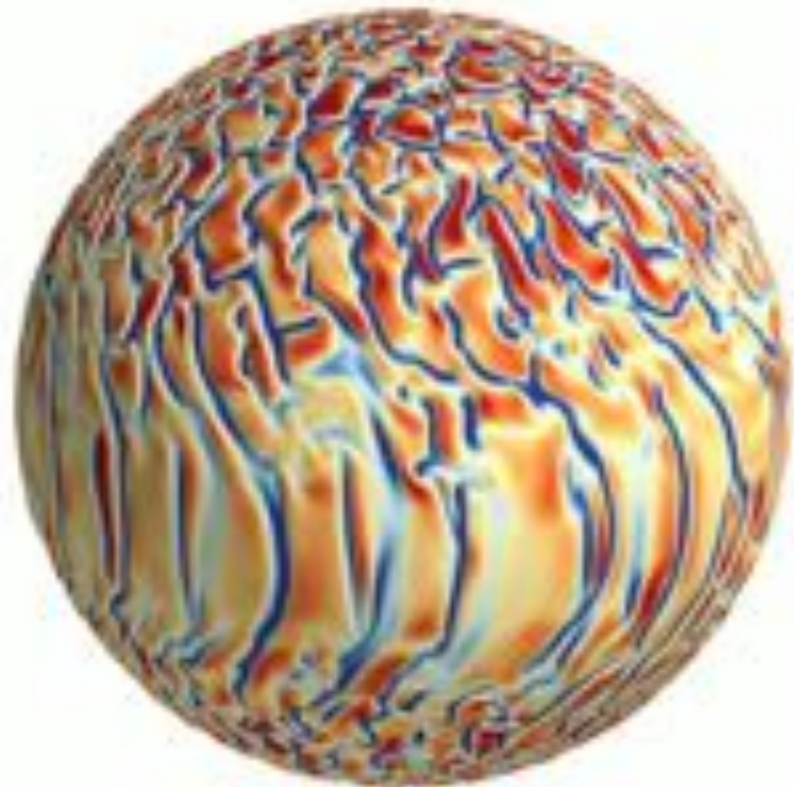


Helical Convection:  
Solar-like Simulations

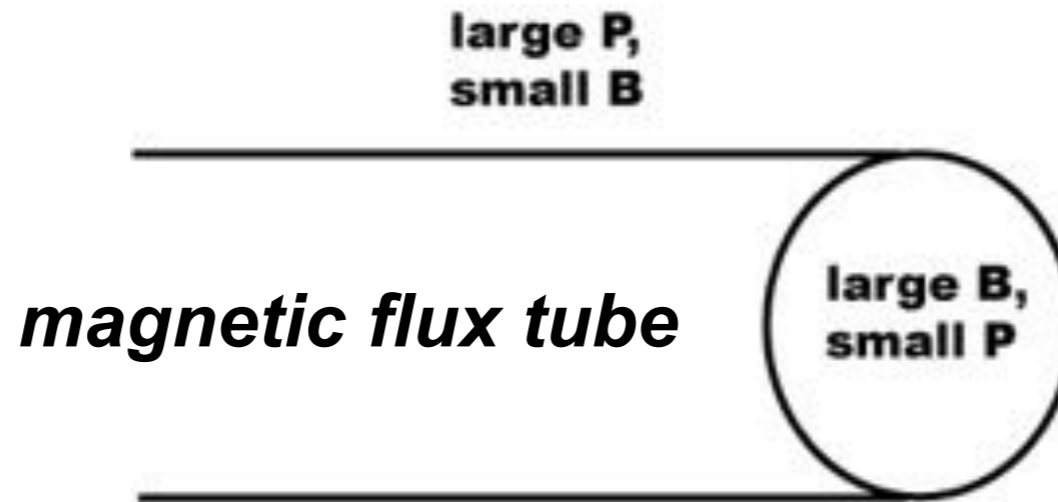
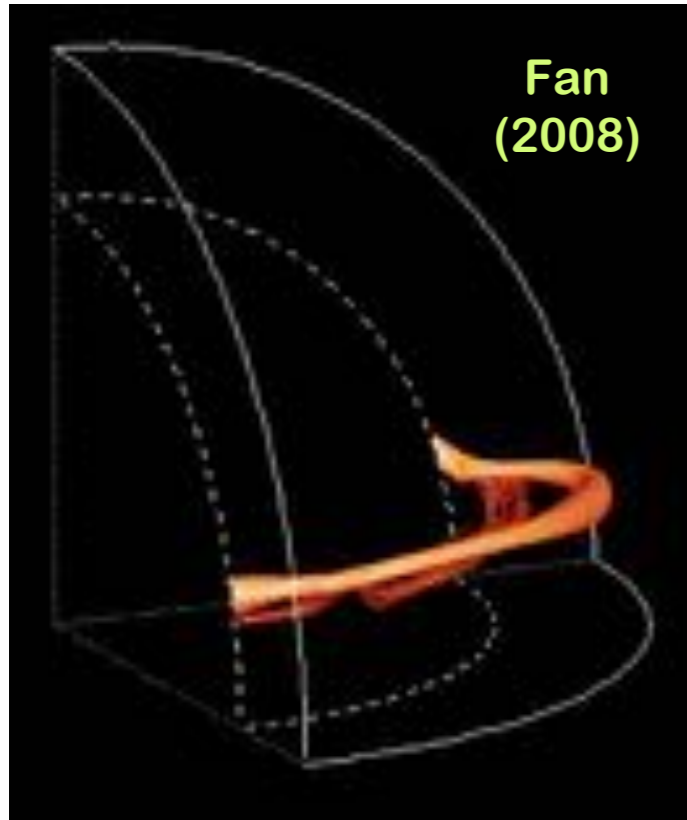
Radial Velocity  
Upper Convection Zone

red upflows

blue downflows



# Another Way: Starts with Magnetic Buoyancy



$$P = \mathcal{R}\rho T$$

$$P_m = \frac{B^2}{8\pi}$$

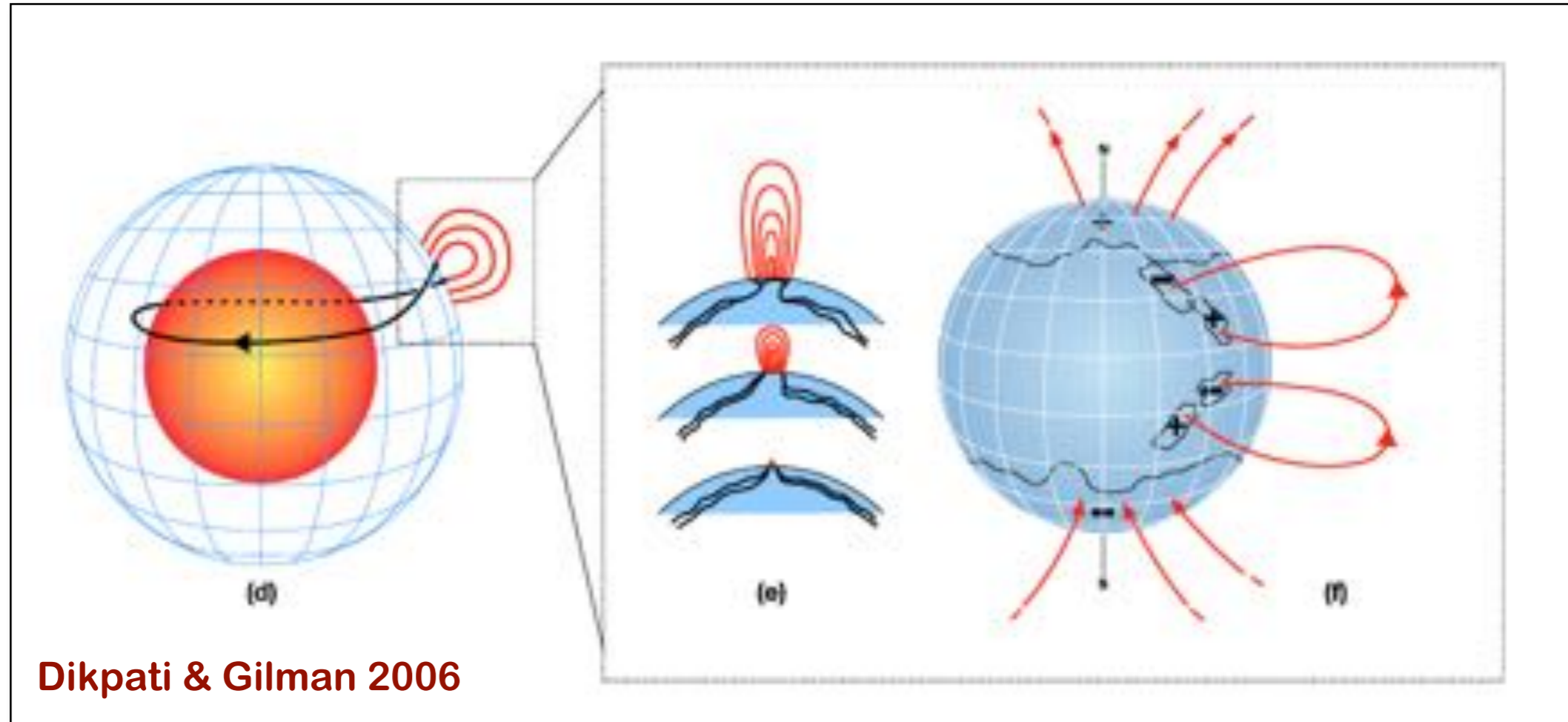
$$P^{(tube)} + P_m^{(tube)} \approx P^{(ext)}$$

$$P^{(tube)} \approx P^{(ext)} - P_m^{(tube)} < P^{(ext)}$$

**If**  $T^{(tube)} \approx T^{(ext)}$

$$\rho^{(tube)} < \rho^{(ext)}$$

# The Babcock-Leighton Mechanism



***Trailing member of the spot pair is displaced poleward relative to leading edge by the Coriolis force (**Joy's law: the higher the latitude, the more the tilt**)***

***Polarity of trailing spot is opposite to pre-existing polar field***

***Dispersal of many spots by convection and meridional flow acts to reverse the pre-existing poloidal field***

# Babcock-Leighton Dynamo Models

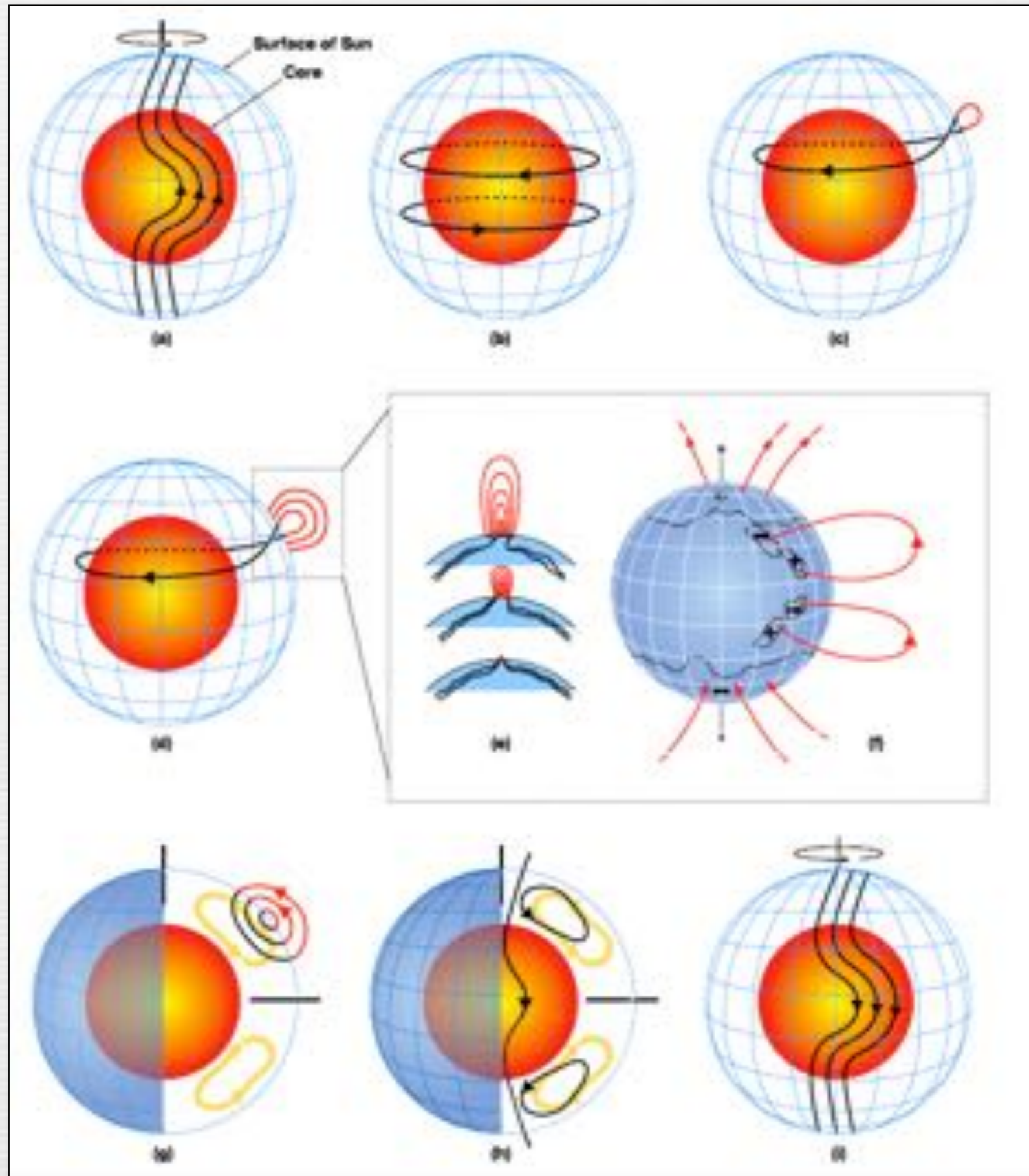
*Poloidal field is generated by the Babcock-Leighton Mechanism*

*Cycle period is regulated by the equatorward advection of toroidal field by the meridional circulation at the base of the CZ*

*2-3 m/s gives you about 11 years*

*For this reason, they are also called*

**Flux-Transport  
Dynamo Models**



## Final Thoughts on the Dynamo Process

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$

- $\mathbf{v}$  influences  $\mathbf{B}$  ...
- ... AND vice versa

$$\rho \frac{\partial \mathbf{v}}{\partial t} = -(\rho \mathbf{v} \cdot \nabla) \mathbf{v} - 2\rho (\boldsymbol{\Omega} \times \mathbf{v}) - \nabla P + \rho \mathbf{g} + c^{-1} \mathbf{J} \times \mathbf{B} - \nabla \cdot \mathcal{D}$$

## Final Thoughts on the Dynamo Process

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B}) + \eta \nabla^2 \mathbf{B}$$
$$\rho \frac{\partial \mathbf{v}}{\partial t} = -(\rho \mathbf{v} \cdot \nabla) \mathbf{v} - 2\rho (\boldsymbol{\Omega} \times \mathbf{v}) - \nabla P + \rho \mathbf{g} + c^{-1} \mathbf{J} \times \mathbf{B} - \nabla \cdot \mathcal{D}$$

- $\mathbf{v}$  influences  $\mathbf{B}$  ...
- ... AND vice versa

***This suggests two classes of dynamos:***

### ***Essentially Kinematic:***

***Small seed field that is initially kinematic (too weak to induce a significant Lorentz force) grows exponentially until it becomes big enough to modify the velocity field***

***This brings up the crucial issue of: **Dynamo Saturation*****

### ***Essentially Nonlinear:***

***The velocity field that gives rise to the dynamo mechanism depends on the existence of the field***

***The focus then shifts toward: **Dynamo Excitation + Dynamics*****



Ultimately, convective flows  
drive a stellar dynamo.

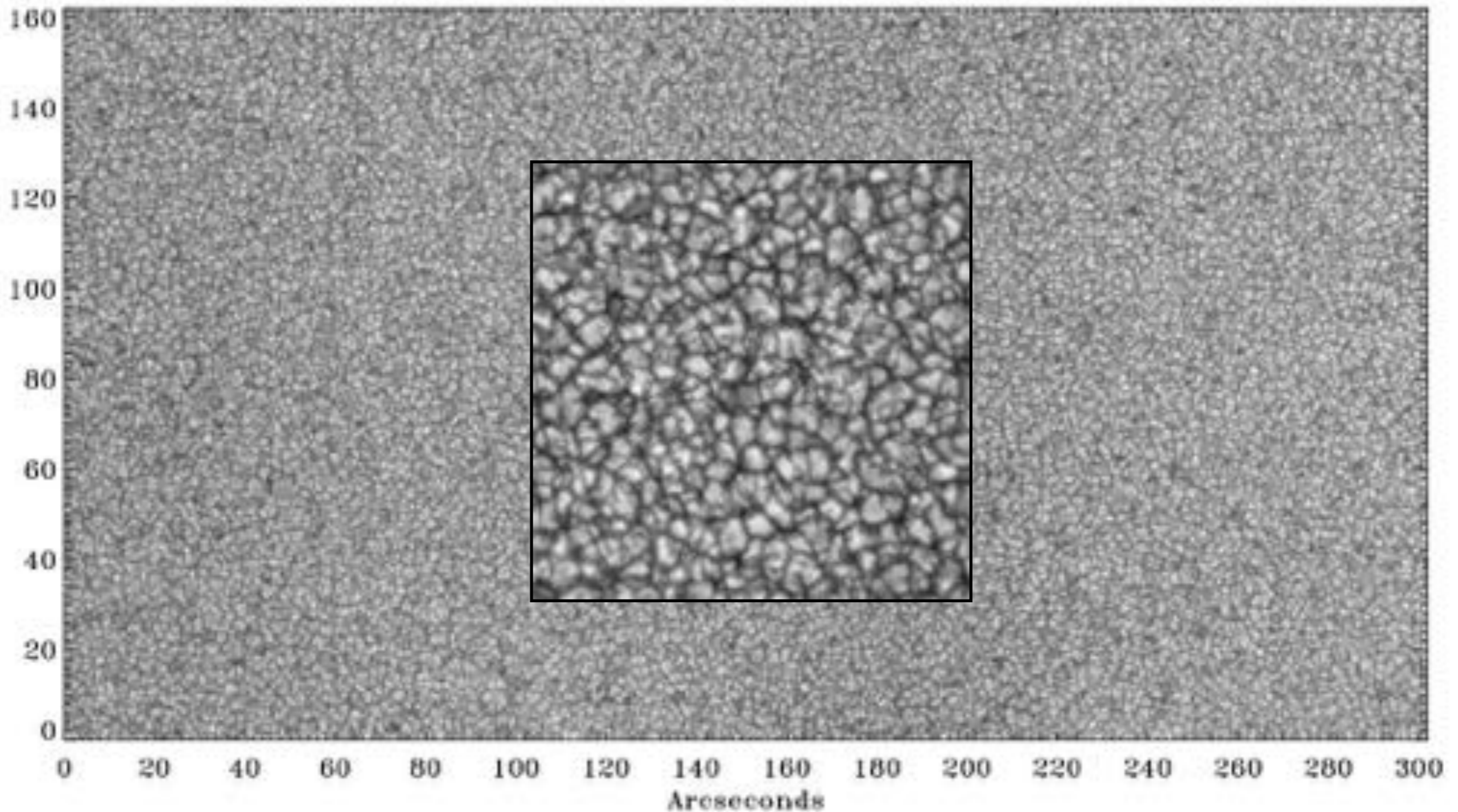
How fast are those flows?

What is their structure?

These are NOT easy  
questions to answer

# Granulation in the Quiet Sun

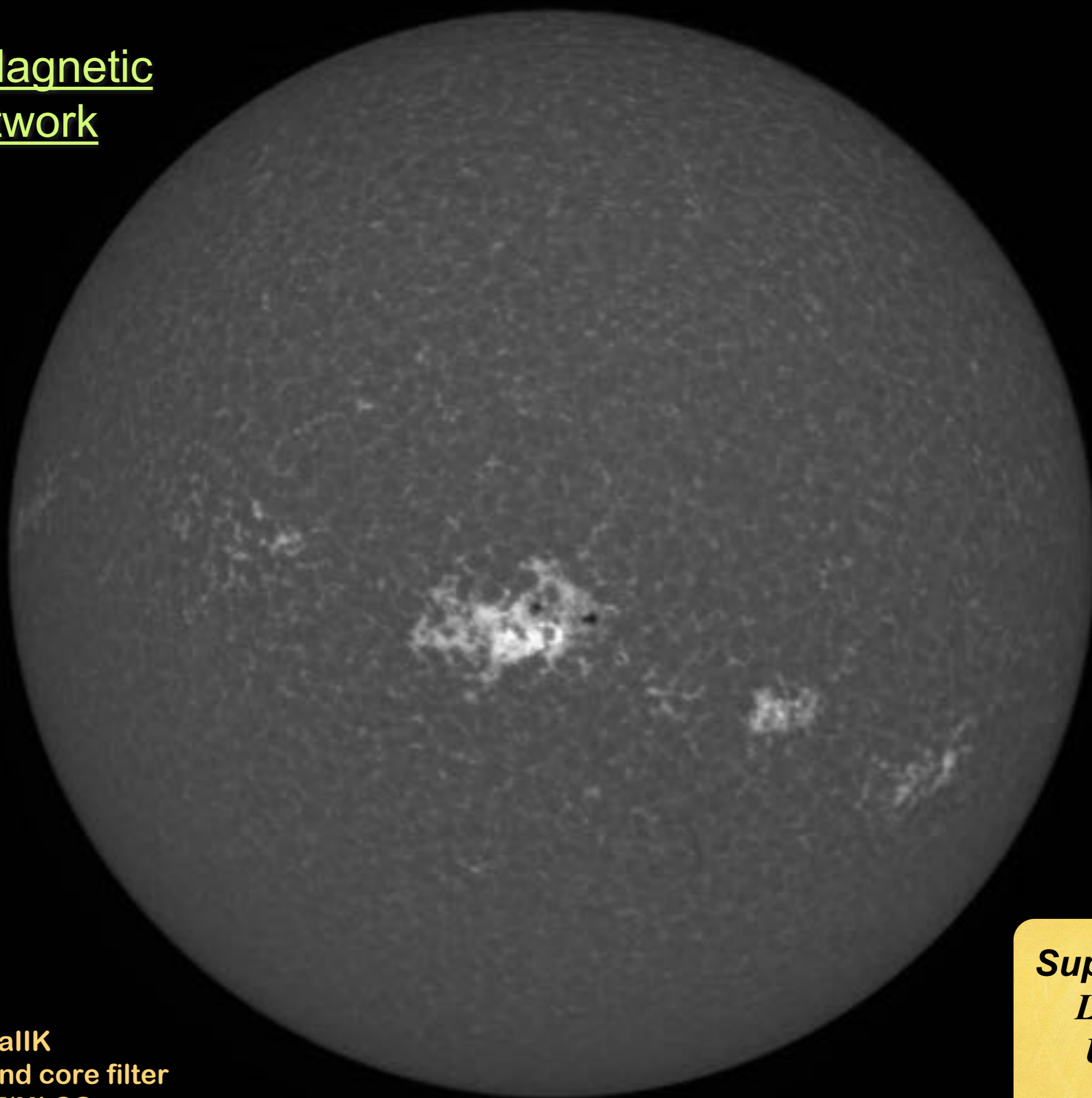
Lites et al (2008)



$L \sim 1-2 \text{ Mm}$   
 $U \sim 1 \text{ km s}^{-1}$   
 $\tau_c \sim 10-15 \text{ min}$

***Dominant size scale of solar convection***

# The Magnetic Network



CaIIK  
narrow-band core filter  
PSPT/MLSO

***Supergranulation***

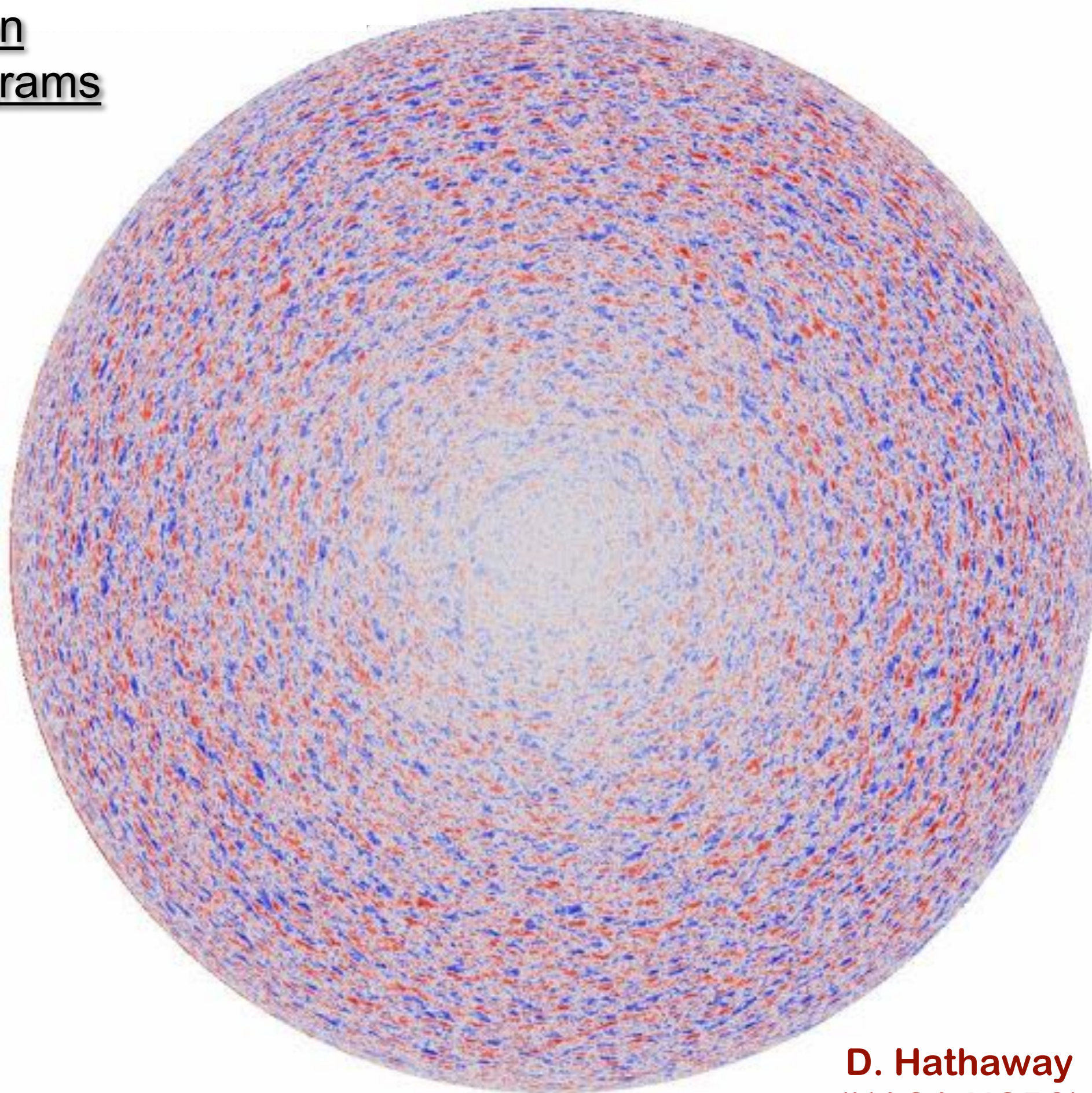
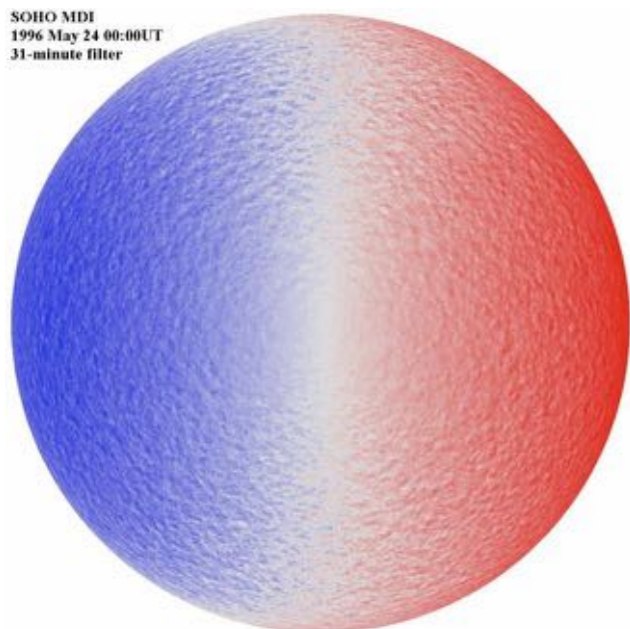
$L \sim 30\text{-}35 \text{ Mm}$

$U \sim 500 \text{ m s}^{-1}$

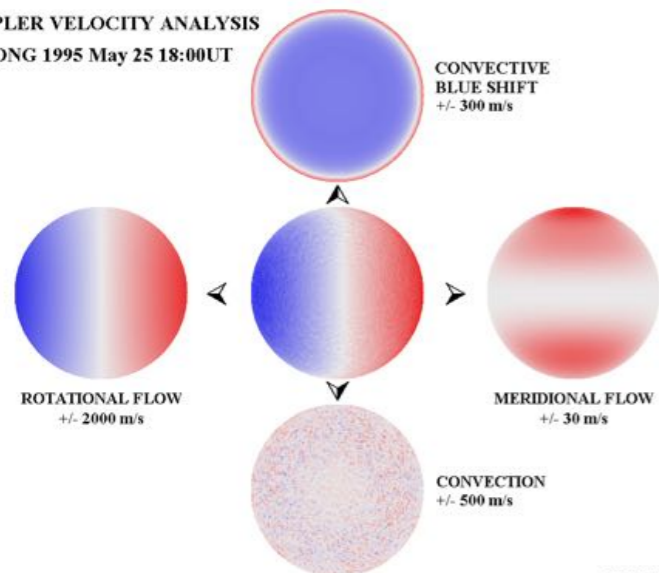
$\tau_c \sim 20 \text{ hr}$

# Supergranulation in Filtered Dopplergrams

*Most prominent in  
horizontal velocities  
near the limb*



DOPPLER VELOCITY ANALYSIS  
GONG 1995 May 25 18:00UT



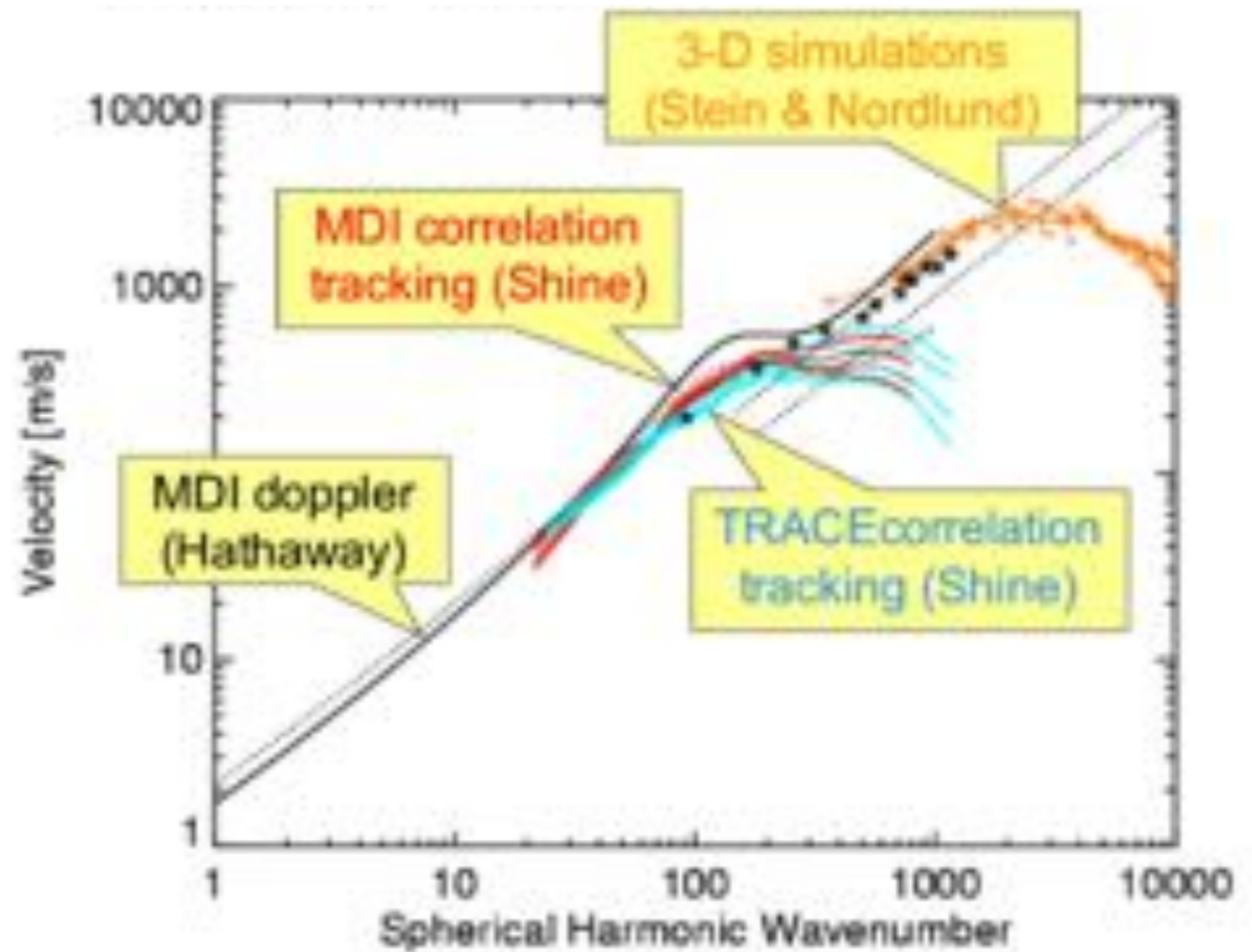
# A hierarchy of convective scales

***Density increases dramatically with depth below the solar surface***

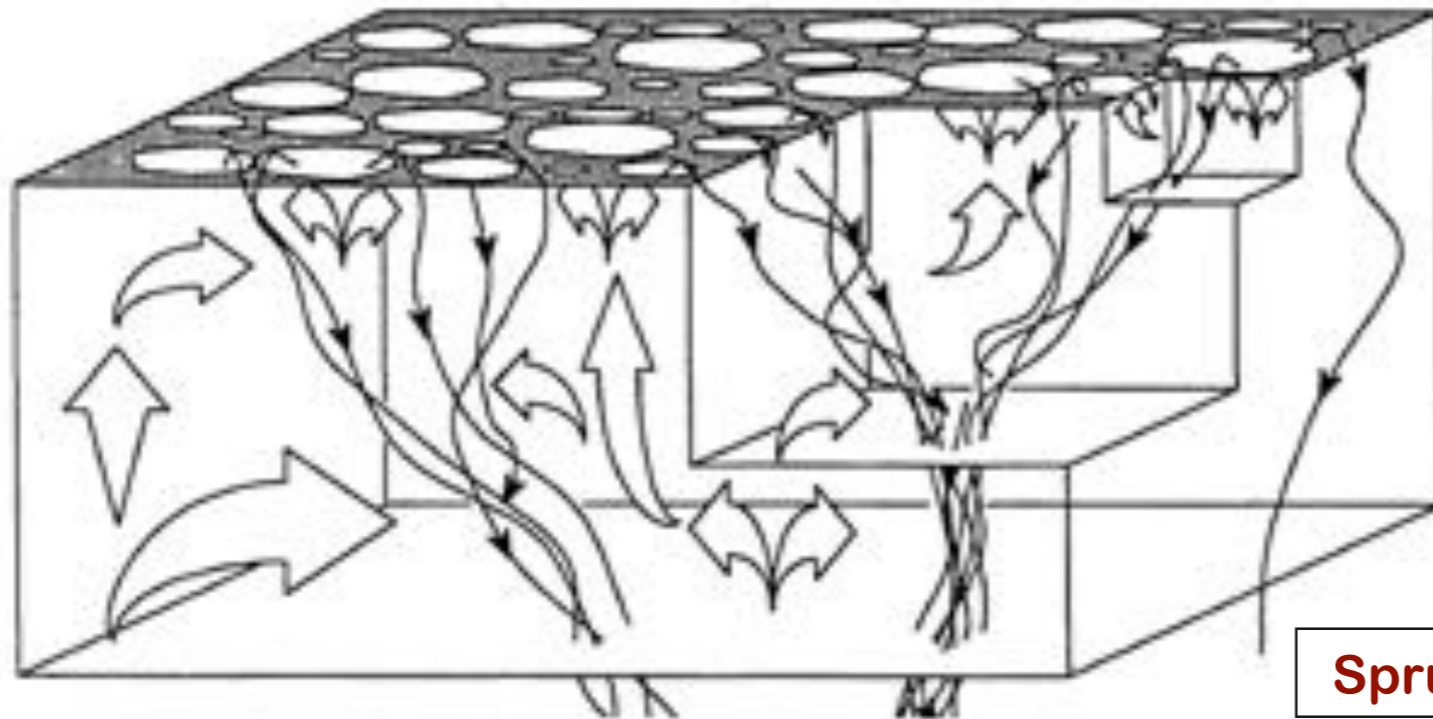
***Fast, narrow down flows (plumes)  
Slow, broad upflows***

***Most of the mass flowing upward  
does not make it to the surface***

***Downward plumes merge into  
superplumes that penetrate deeper***



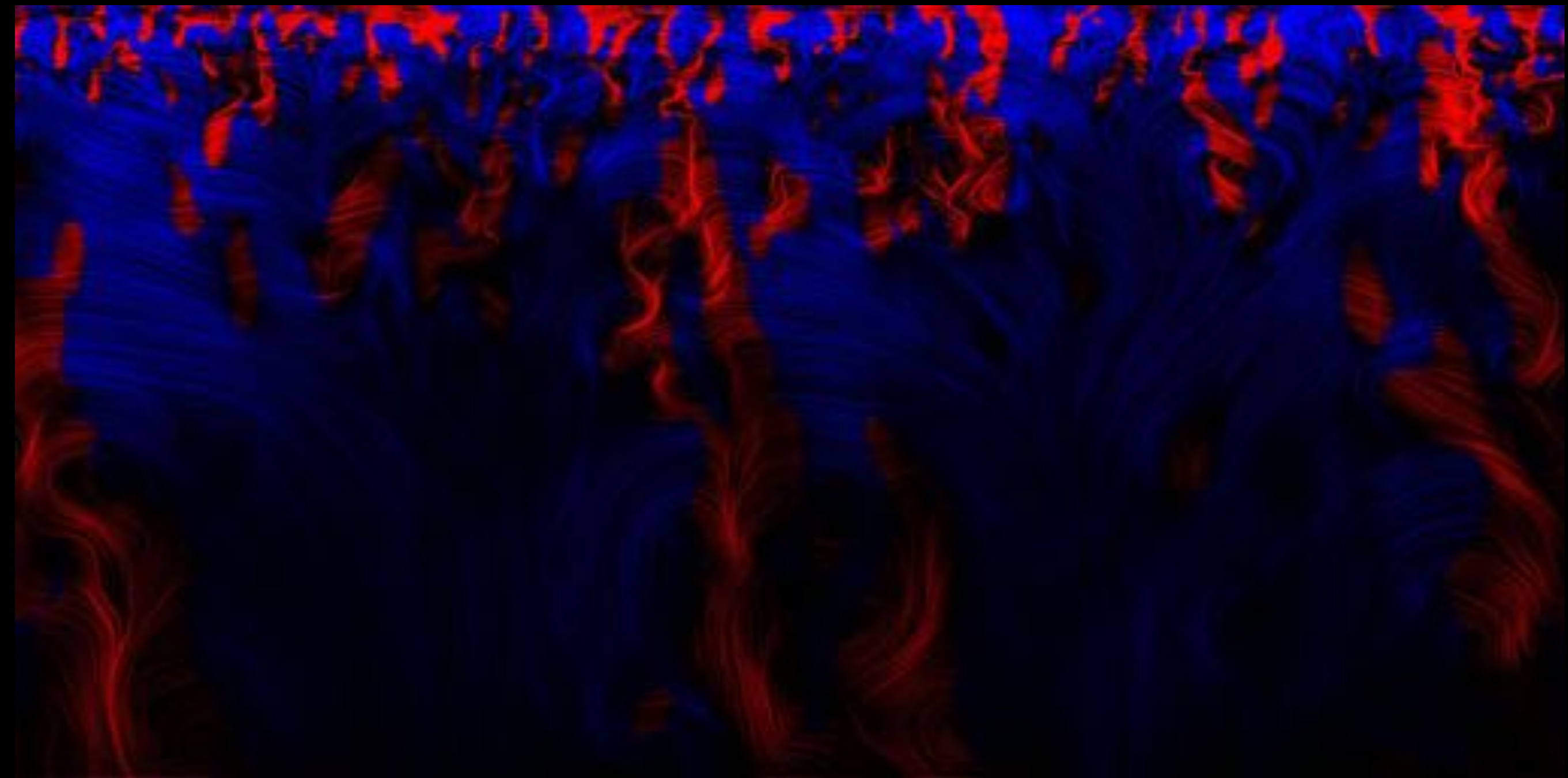
Nordlund, Stein & Asplund (2009)



***Supergranulation and  
mesogranulation are part of a  
continuous (**self-similar?**)  
spectrum of convective motions***

Spruit, Nordlund & Title (1990)

simulation by Stein et al (2006), visualization by Henze (2008)



*Size, time scales of convection cells increases with depth*

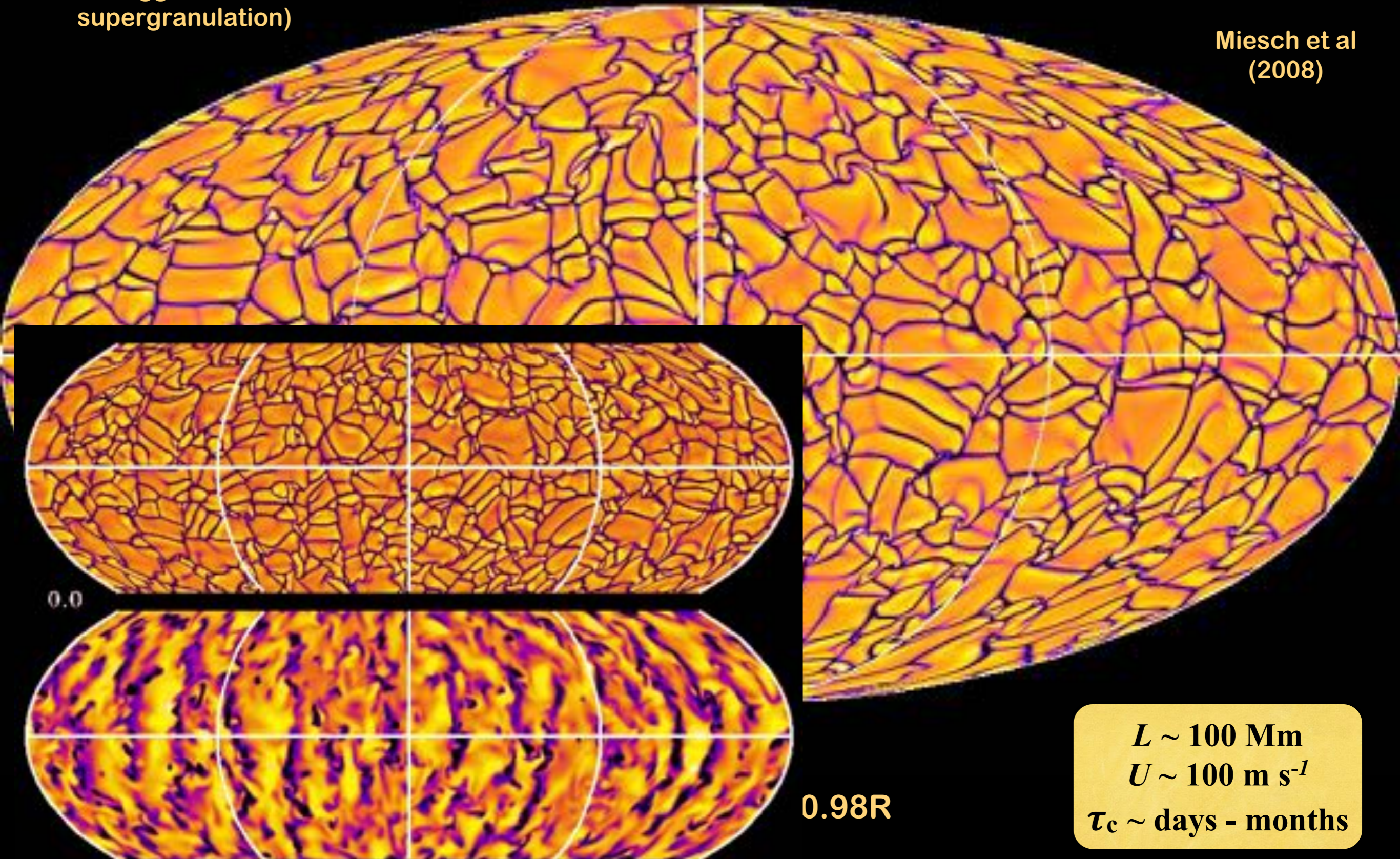
*But still stops at  $0.97R$ !  
what lies deeper still?*

# Giant Cells

(Loosely, anything bigger than supergranulation)

*Eventually the hierarchy must culminate in motions large enough to sense the spherical geometry and rotation*

Miesch et al  
(2008)



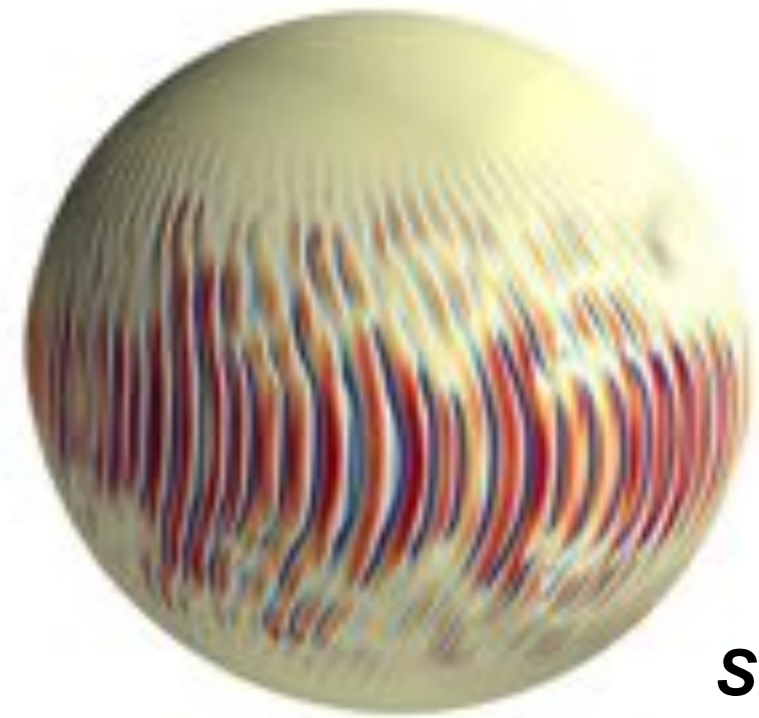
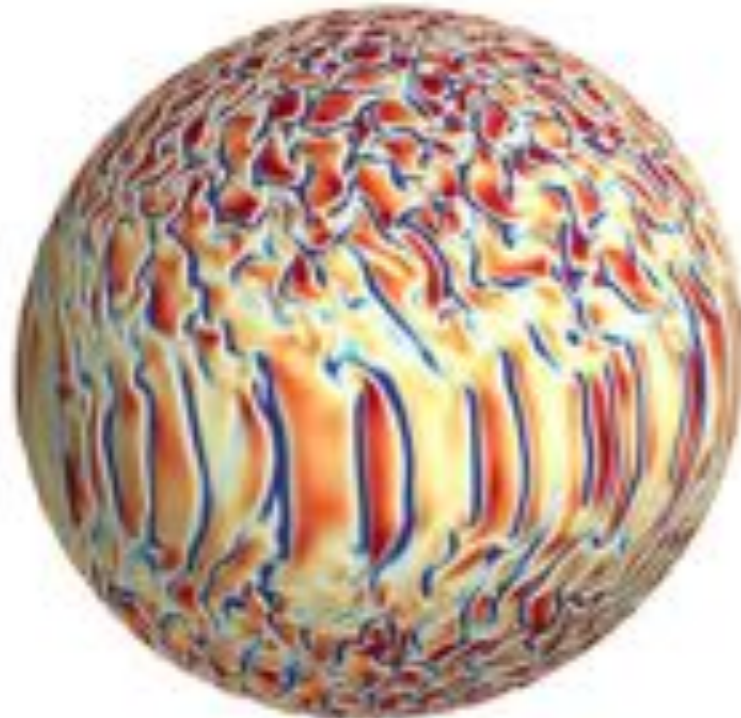
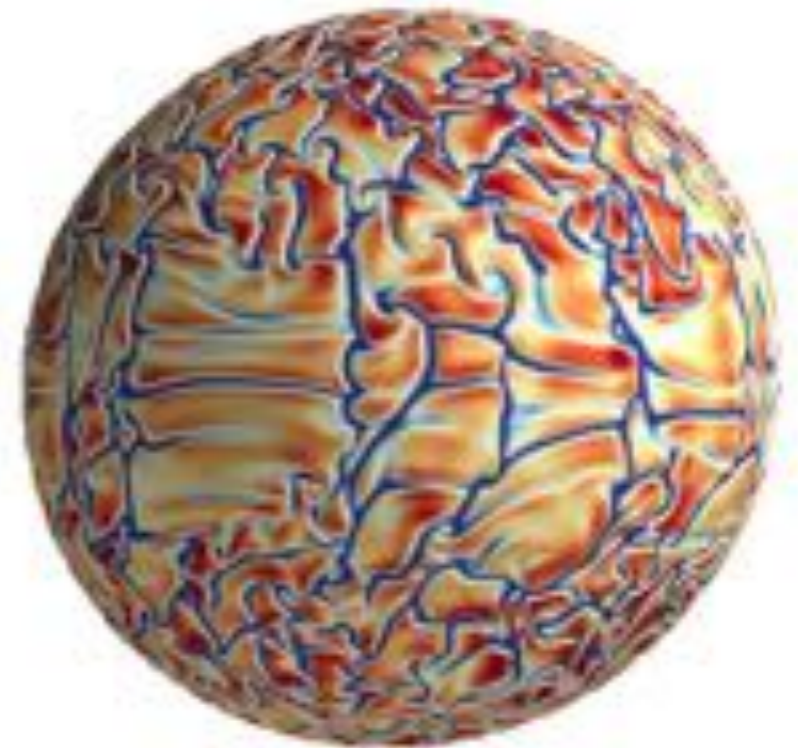
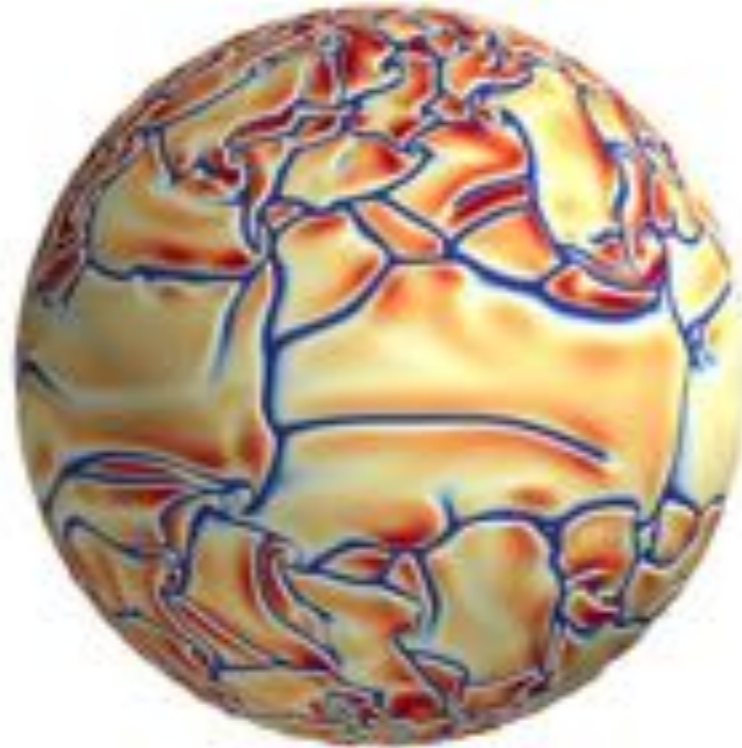
$L \sim 100 \text{ Mm}$   
 $U \sim 100 \text{ m s}^{-1}$   
 $\tau_c \sim \text{days - months}$

0.98R

0.0

**Rapid  
Convection**

**N. Featherstone**



**Slow  
Convection**

***Giant cells are notoriously difficult to detect  
(possibly masked by more vigorous surface  
convection)***

***How do we know they  
are there?***



We don't.

This is a major puzzle for solar  
(and also stellar) dynamo  
theory and brings us to one of  
the major outstanding  
questions.

# What is the solar Rossby Number?

*typical velocity*

$$Ro = \frac{v}{2\Omega L} =$$

Rotational Timescale

Convective Timescale

*rotation rate*

typical length scale

What is  $Ro$  in the Sun?

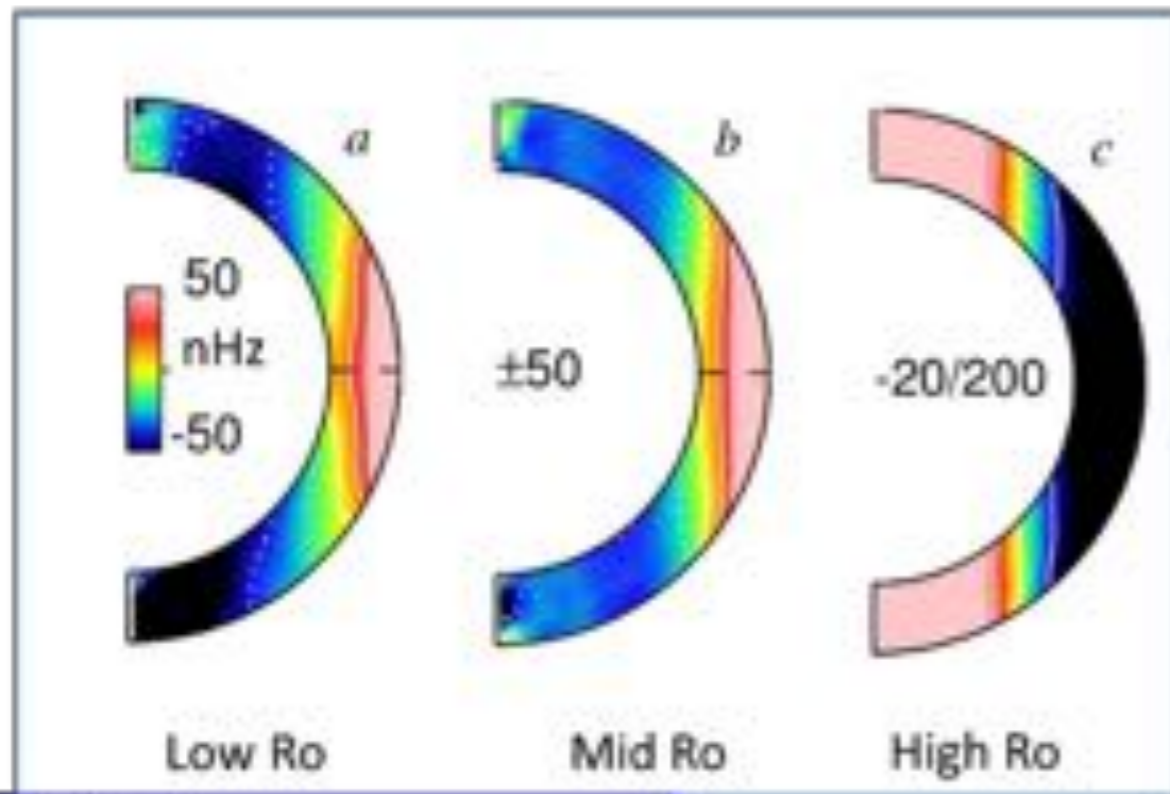
What is  $v$ ?

$Ro$  influences the structure of the convection and so too MANY aspects of the dynamo!

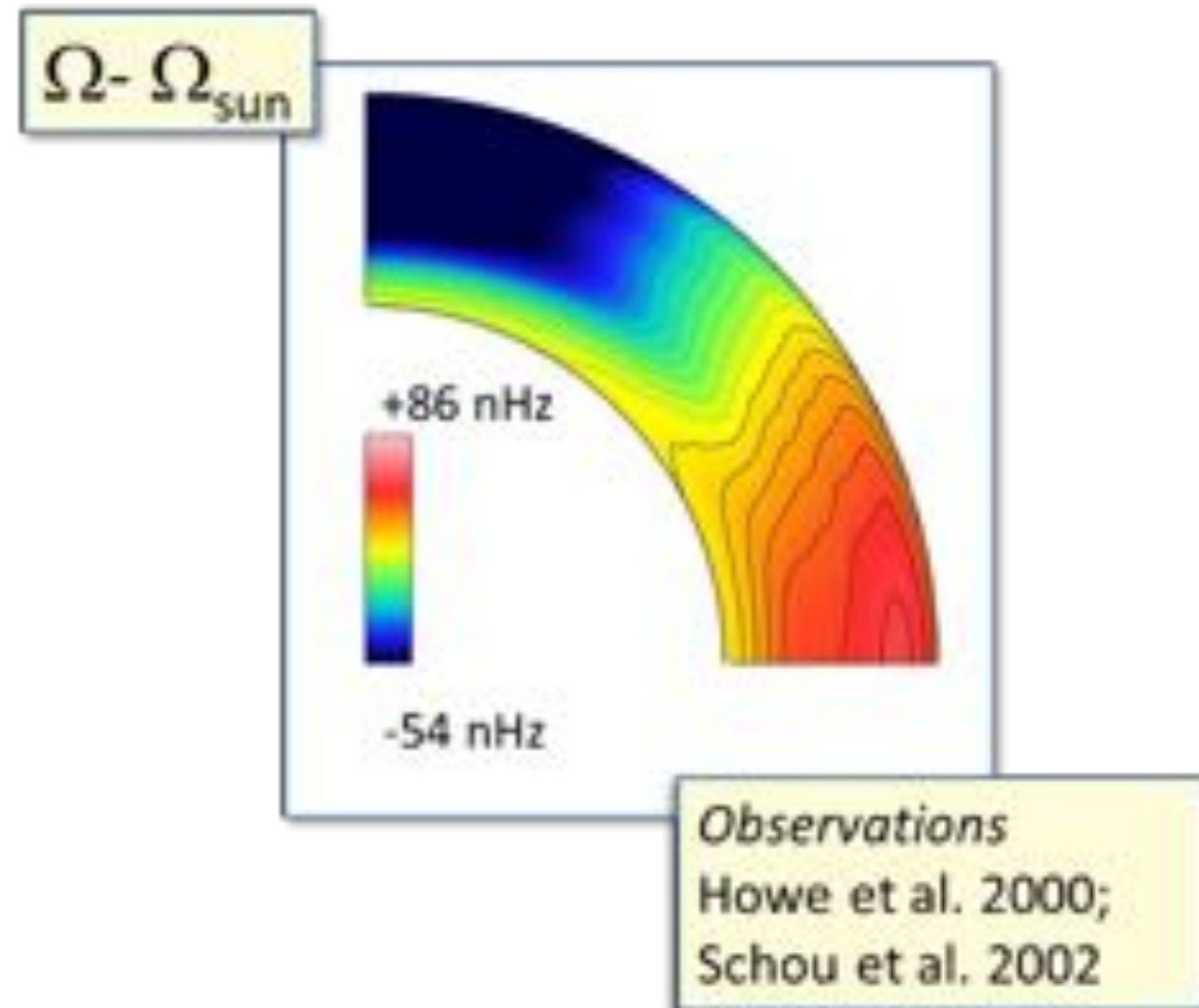
Aside

1. Consider system-scale  $Ro$
2.  $v$  = rms convective flow speed
3.  $L$  = shell depth

# Ro determines differential rotation



*Models*  
Featherstone & Miesch 2015

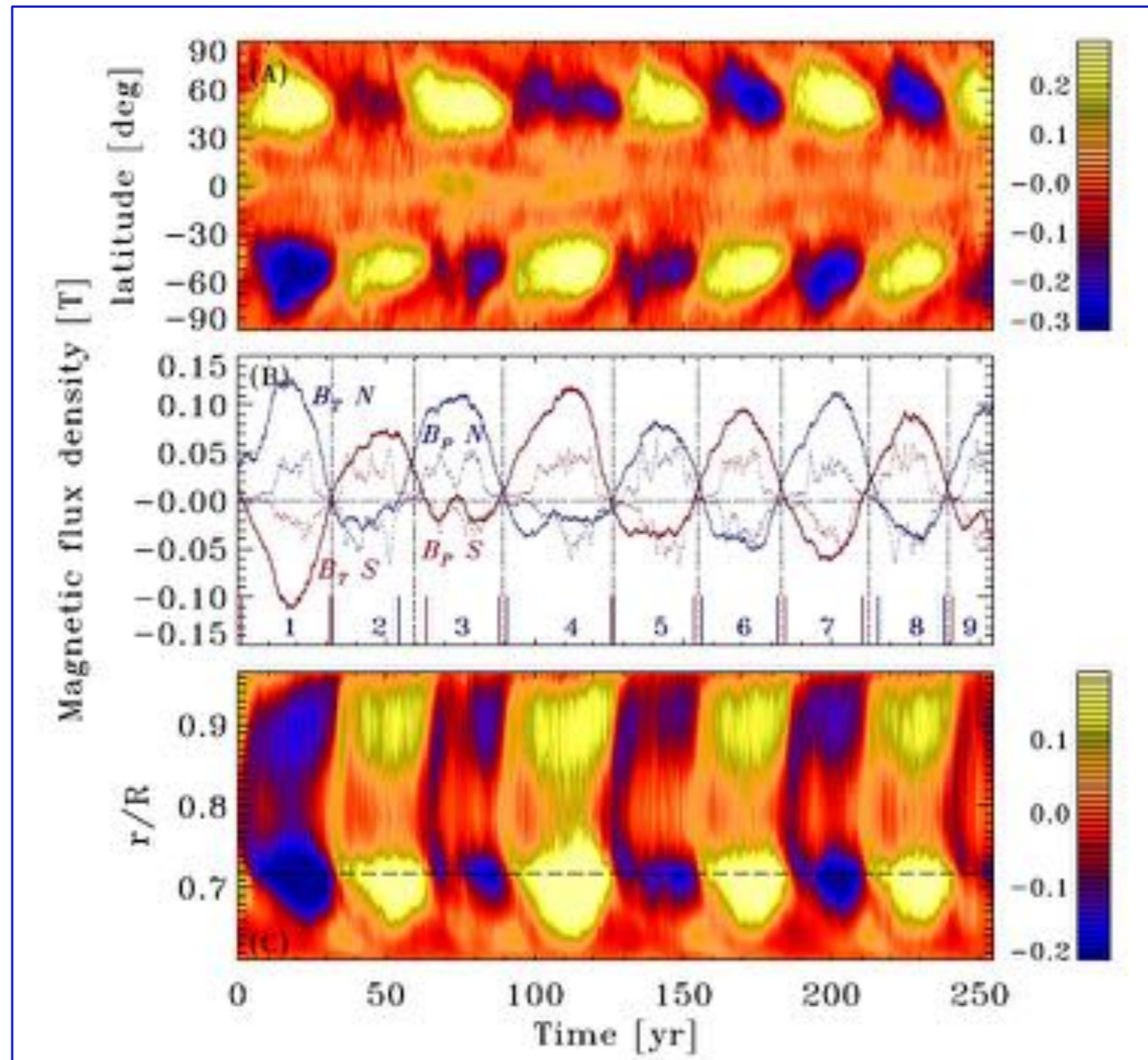


*Observations*  
Howe et al. 2000;  
Schou et al. 2002

*AND:* Glatzmaier & Gilman 1982; Brun & Toomre 2002;  
Gastine et al. 2014; Guerrero et al 2013; Kapyla et al. 2014 ...

**Aside:** differential rotation may be indirect evidence of giant cells, but see tomorrow's discussion!

# Low Ro Promotes Magnetic Cycles (models)

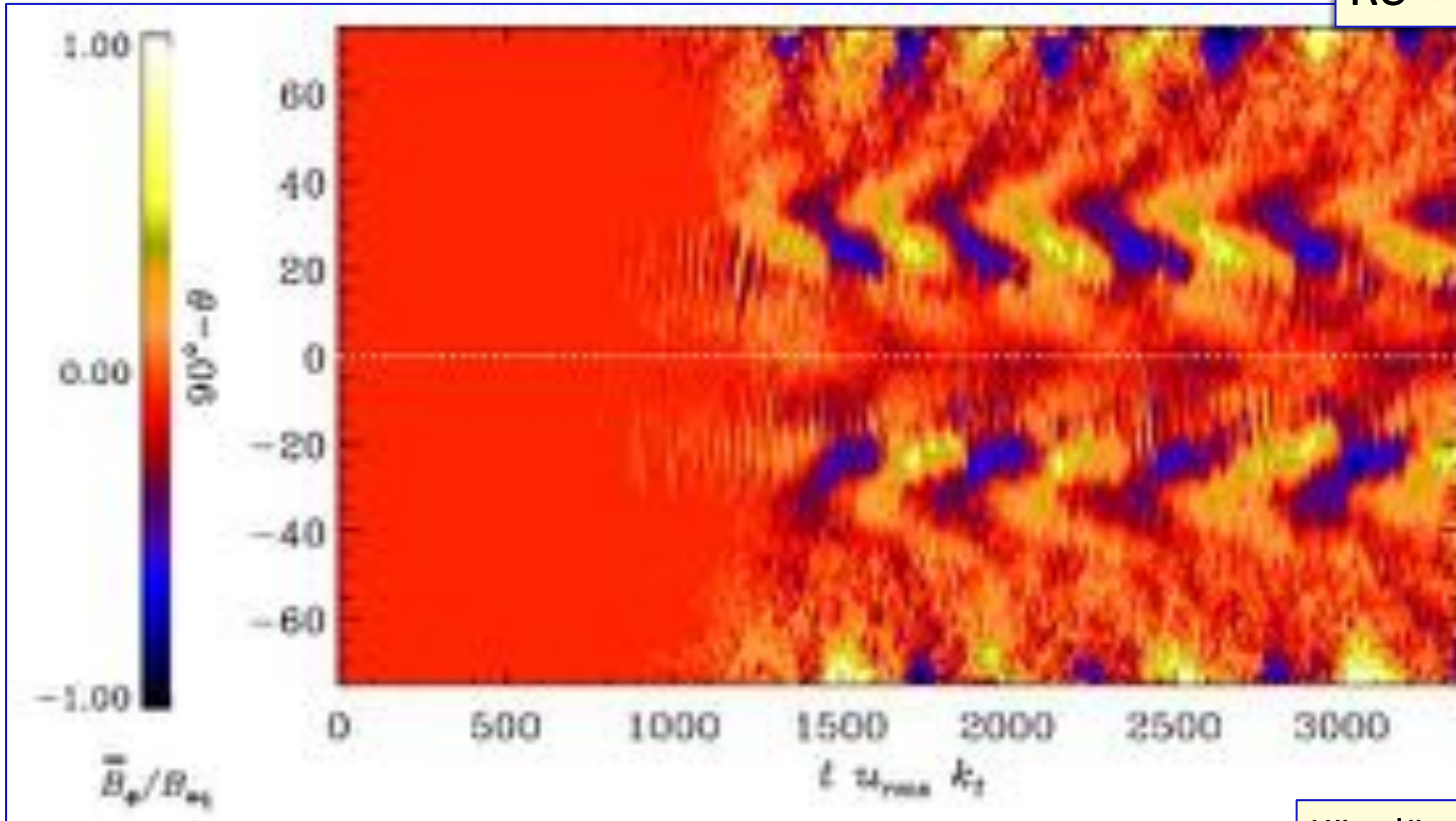


Ro  $\approx$  0.01

Ghizaru,  
Charbonneau  
& Schmolarkiewicz  
2010

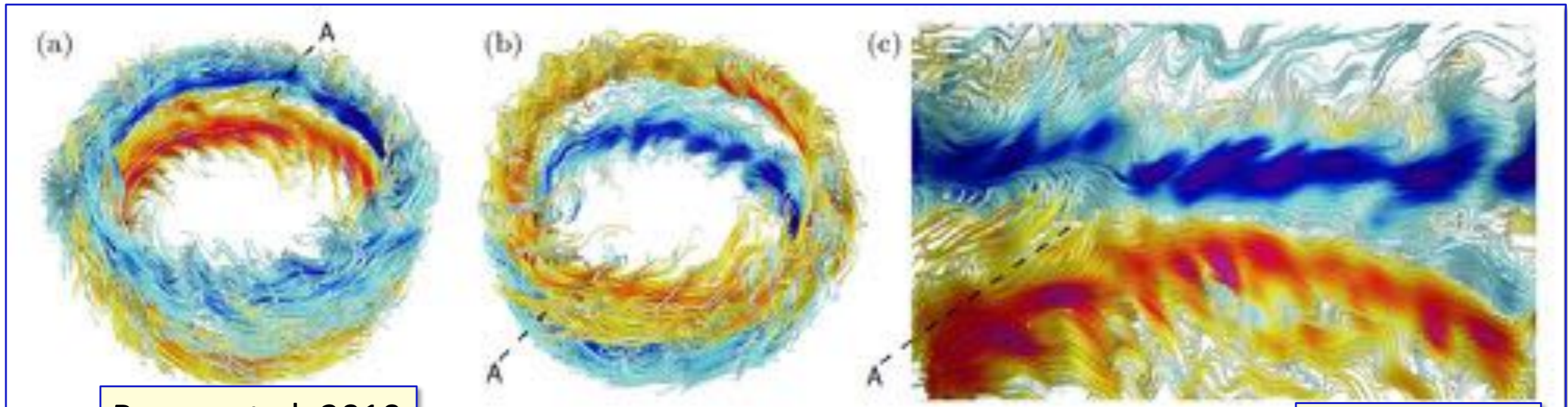
# ... and Equatorward Propagation of Magnetic Features (models)

Ro  $\approx$  0.02



Käpylä et al. 2013

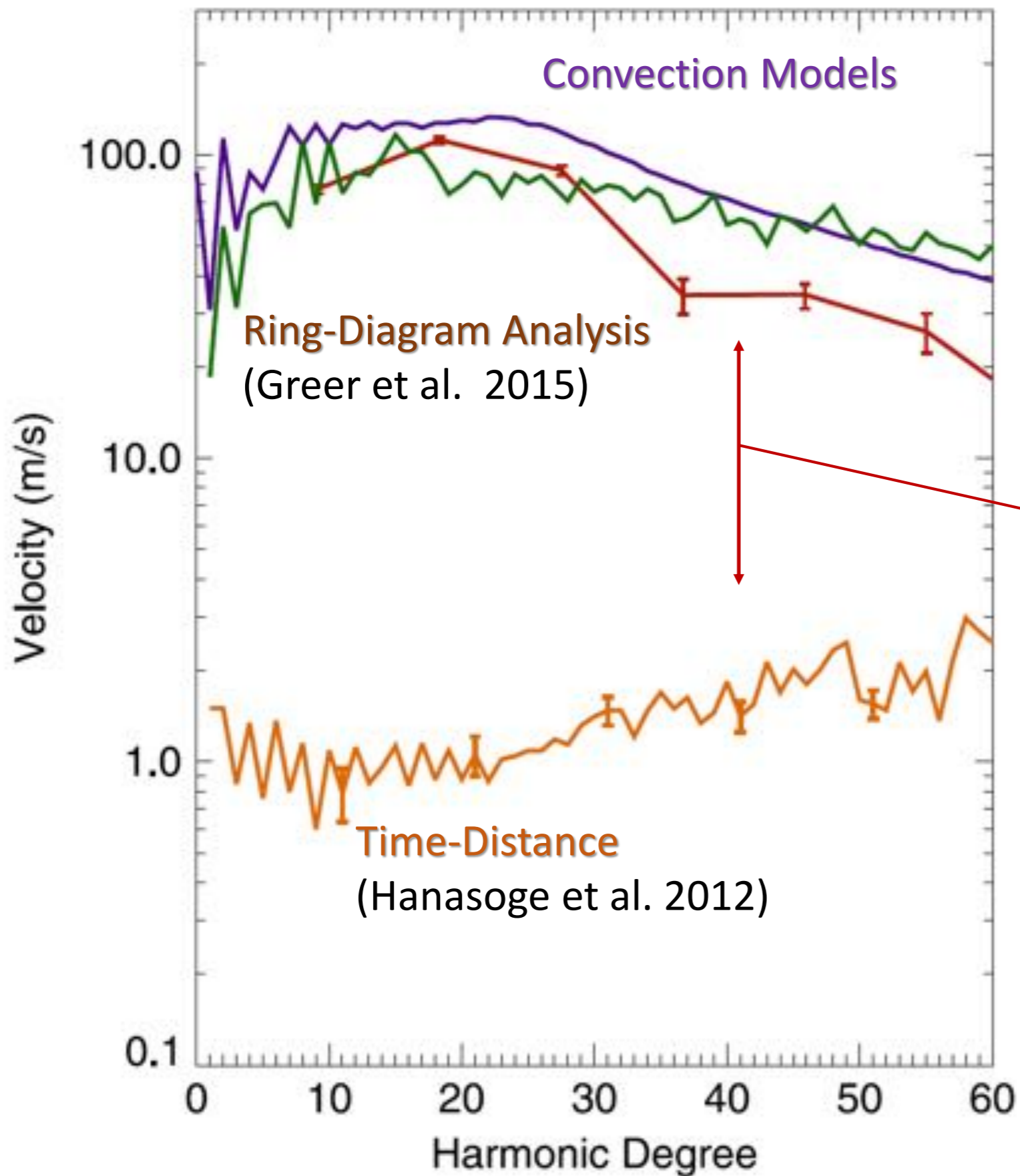
# ... and Large-Scale Magnetic Structure (models)



Brown et al. 2010

“wreathy” dynamos

$Ro \approx 0.03$

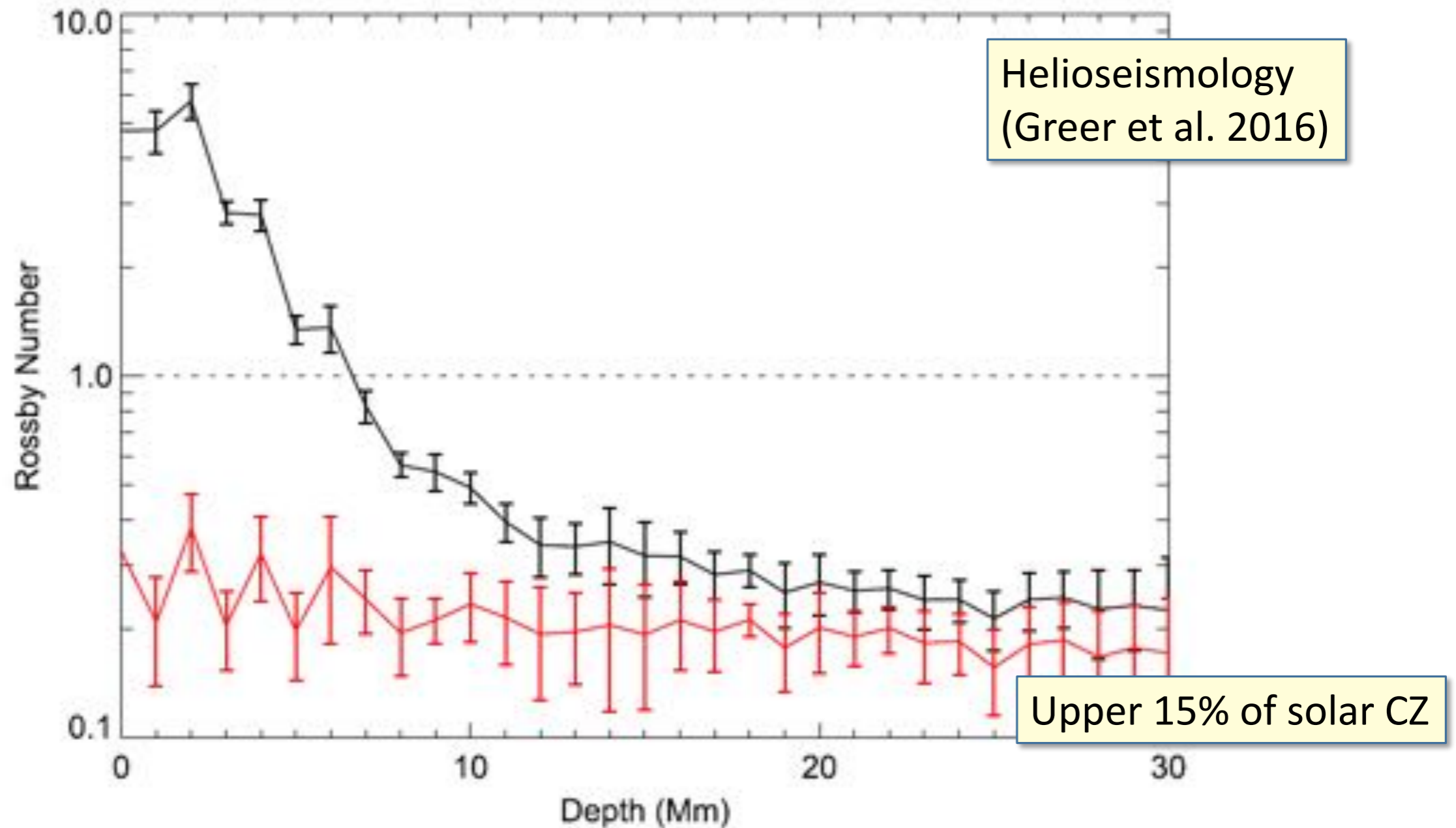


What do  
measurements tell us?

*Disagreeing  
Observations  
( $0.96 R_{sun}$ )*

*Open Question:  
How fast is deep  
solar convection?*

## What we know: at Depth ... $Ro$ is LOW

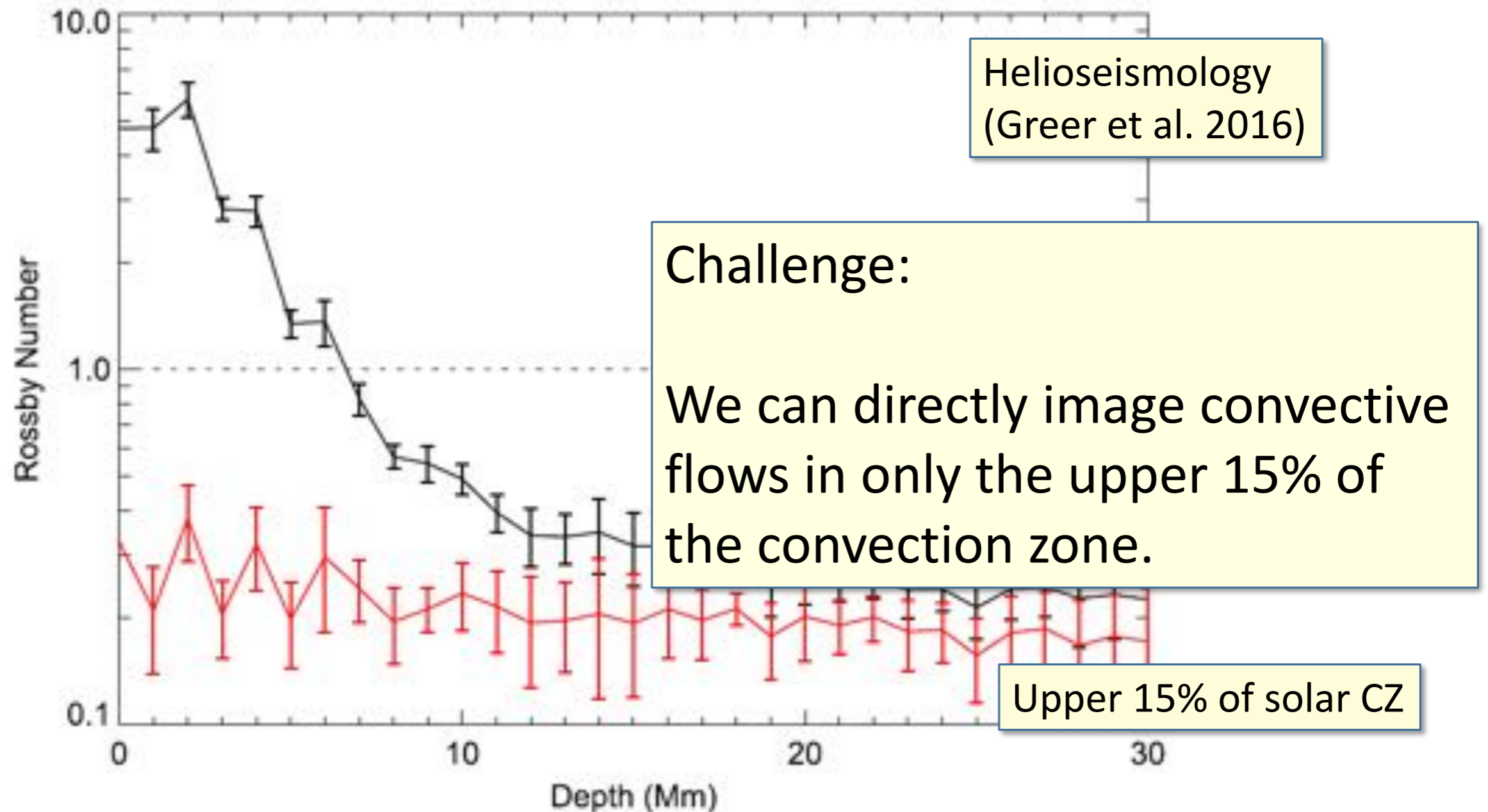


*But how low?  
Open Question!*

*Possibly even lower:  
See non-detection of Hanasoge et al. 2012, PNAS, 109, 11928*



# What we know: at Depth ... $Ro$ is LOW



*But how low?  
Open Question!*

*Possibly even lower:  
See non-detection of Hanasoge et al. 2012, PNAS, 109, 11928*

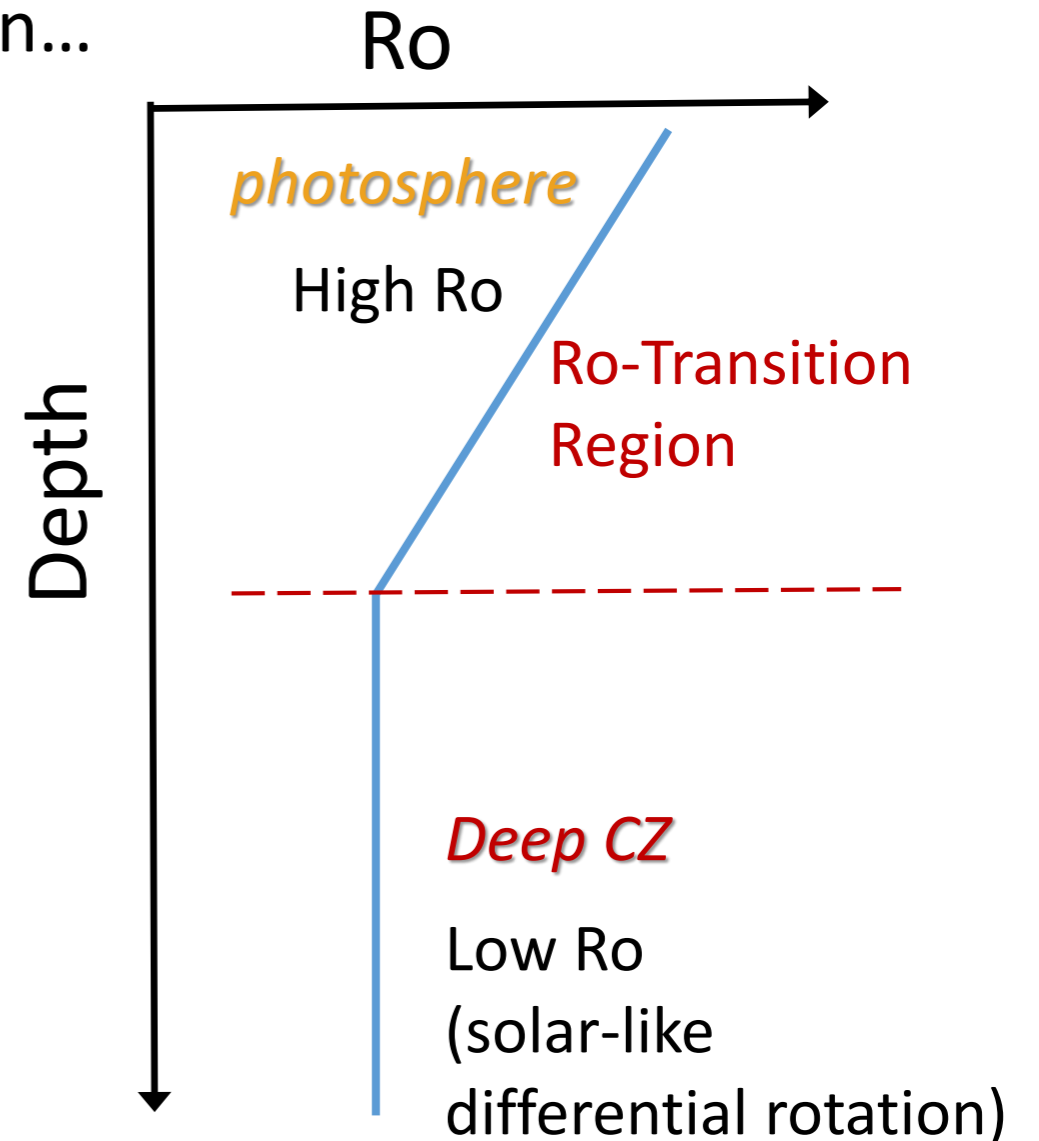
# What do we expect at the solar surface?

We might expect to see two types of convection...

1. Small-scale motions:
  - Near-surface features
  - high-Ro
  - **Spatial-scale depends on Ro-transition depth**
2. Large-scale motions:
  - deep-seated, global
  - low-Ro

Observed:  
30 Mm size  
Ro = 3

Unobserved...



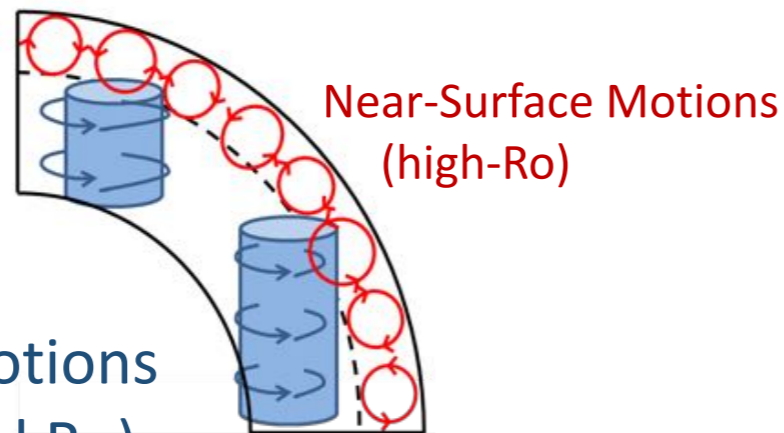
Lack of #2 may be telling us something...

# Deep Motions & Their Spectra

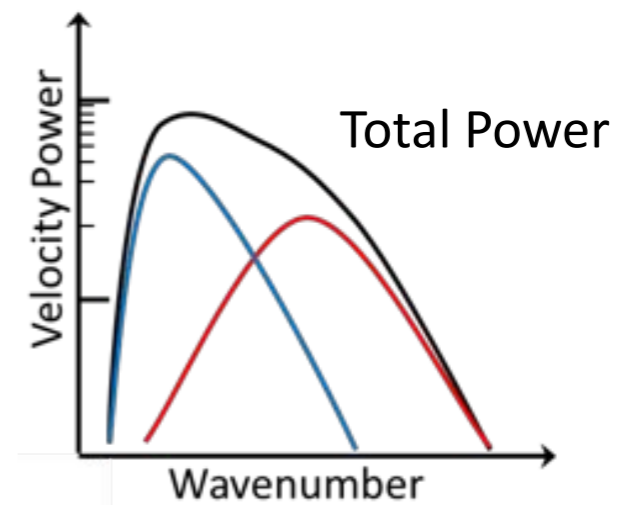
## Cellular Structure

Classic Cartoon  
(not observed)

Deep Motions  
(marginal  $Ro$ )

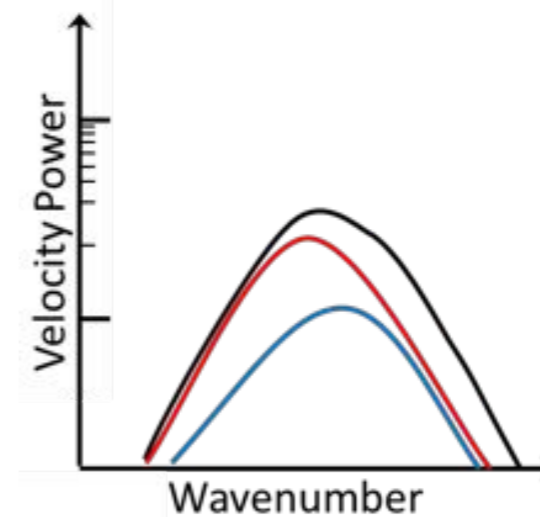
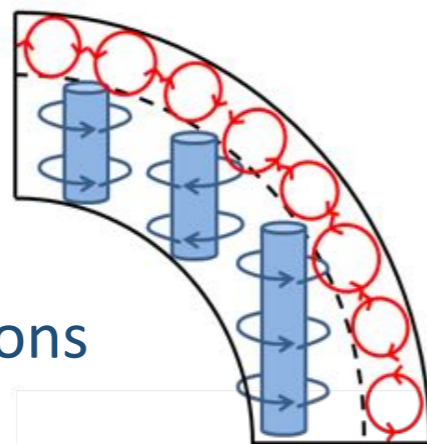


## Photospheric Power



Alternative  
Possibility

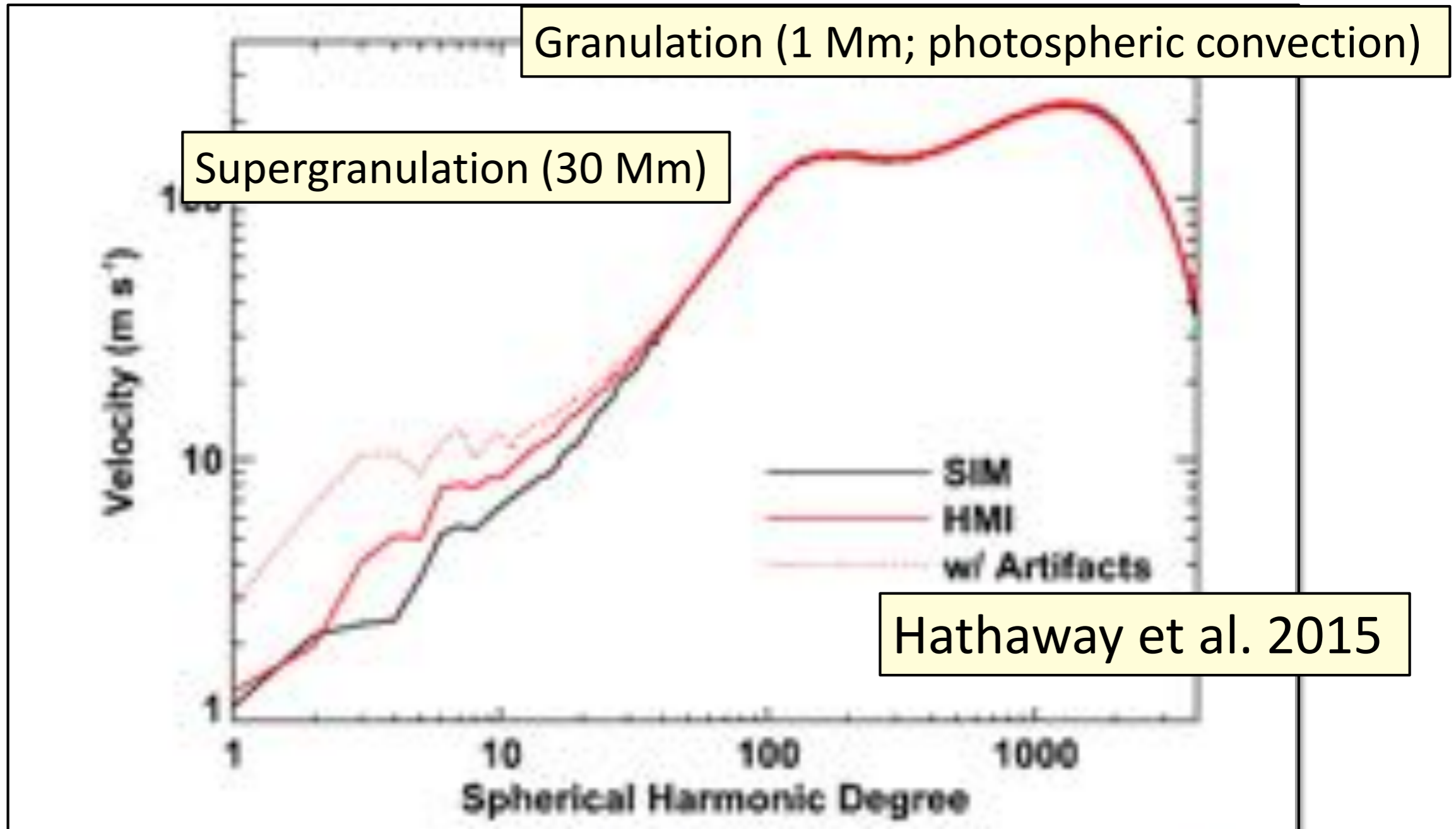
Deep Motions  
(Low-  $Ro$ )



Featherstone & Hindman 2016

# Photospheric Doppler Velocity Spectra

Giant Cells (200 Mm, Not here)

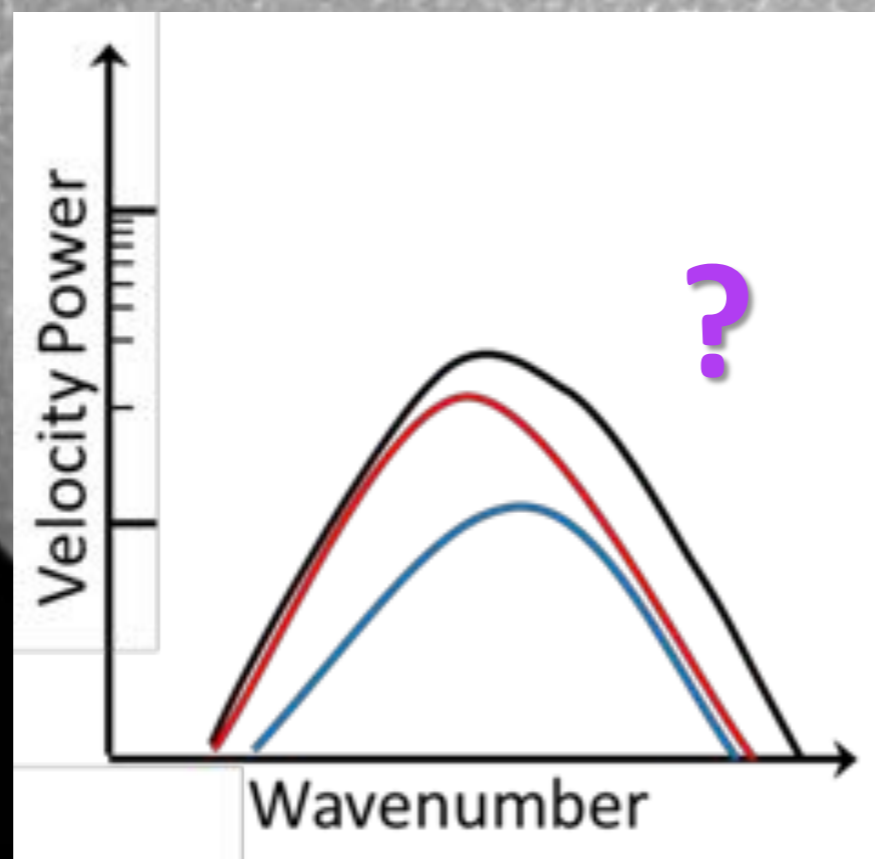


Hathaway et al. 2015

# Supergranulation

The largest, distinctly visible mode of solar convection is not rotationally constrained at the surface.

$L \approx 30 \text{ Mm}$   
 $U \approx 400 \text{ m s}^{-1}$   
 $Ro \approx 2.7$



AIA 1700

The image displays six spheres arranged in two rows of three, illustrating the evolution of solar dynamo activity. The top row shows three spheres with irregular, fragmented patterns of orange, red, and blue, representing early, chaotic stages. The bottom row shows three spheres with increasingly regular, vertical, wavy bands of orange, red, and blue, representing later, more organized stages of the dynamo process.

Where is the Sun?

Until we know this, it is very difficult to make meaningful statements about how the solar dynamo works.